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XVIII CYCLE

Experimental and Numerical Study
of Mild Combustion Processes in
Model Reactors

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# Experimental and Numerical Study of Mild Combustion Processes in Model Reactors

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7) A. Matarazzo, M.de Joannon, P.Sabia, A. Cavaliere Premixed Laminar Flames in Mild Combustion Conditions The Italian section of the Combustion Institute, Combustion and Urban Areas, 28th Combustion Meeting Naples, July 4-6, 2005


9) E. Schießwohl, P. Sabia, M. de Joannon, A. Cavaliere Analysis of Detailed Hydrogen Combustion Mechanisms with Application to Mild Combustion The Italian Section of the Combustion Institute, Combustion and Urban Areas, 28th Combustion Meeting Naples, July 4-6, 2005

10) P. Sabia, M. de Joannon, R. Ragucci, A. Cavaliere Mixing efficiency of jet in cross-flow configuration in a tubular reactor for Mild Combustion studies, European Combustion Meeting, Louvain-la-Neuve, Belgium, April 3-6, 2005


15) P. Sabia, M. de Joannon, A. Cavaliere *Design and fluid-dynamic characterization of a Plug Flow Reactor for Mild Combustion studies* Joint Meeting of The Italian and Greek Sections of The Combustion Institute Corfu, June 17-19 2004


Pollutants main responsible of environmental impact, on global scale (greenhouse effect) and on small scale (health effect, visibility), are species such as nitrogen oxides and particulate matter (fine and ultra-fine) and polycyclic aromatic compounds (PAH) formed during combustion processes. The scientific community interest is focused on the identification of new technologies that would allow achieving more efficient energy production systems, in terms of energy production and of pollutants abatement. In particular the tendency affirmed in these years is the identification of temperature, pressure and mixtures compositions, different from the traditional systems that could permit to reach these targets. In literature it is acknowledged that high temperature (higher than 1800K) favors the production of nitrogen oxides and soot. In this background one of the new combustion “mode”, that forecasts the use of high amount of inert species, such as nitrogen, steam water or exhausts gases, seems to be very promising. As matter of fact, the high dilution level allows enhancing the heat capacity of the system, and consequently to low the adiabatic temperature to values that permit to control the production of nitrogen oxides, soot and PAH compounds. In order to have a working temperature lower than critical values that cause the formation of these pollutants, the mixture composition has to fall beyond the flammability limits. In these operative conditions the oxidation process can evolve exclusively in presence of a pre-heating of reactants that allows reaching inlet temperatures higher than the one that favors spontaneous ignition of the mixture. The combustion process can evolve whether it is used an inlet temperature higher than the auto-ignition temperature of mixtures. In literature such technology is named “mild” (Cavaliere e al., 2001), in relation to the characteristic of the process that will be thoroughly discussed in this thesis.

The Mild combustion gives rise to interests in many applications, from oven for the
raw material processing to turbo-gas, but also as a post-process to as cleaning method of pollutants from industrial plant.

A particular application of Mild combustion is in processes that employ hydrogen as fuel. In fact the highly dilutions, typical of Mild operative conditions, allow to mitigate the hydrogen characteristics such as its high reactivity and the high calorific power, that in a traditional combustion system would imply a very difficult control of the oxidation process since kinetic characteristic times and high working temperatures would be prohibitive.

The high dilution level would consent to moderate the hydrogen reactivity and the flame propagation realizing a controllable combustion. A particular application would be the use of hydrogen in steam water turbines, since the oxidation of this fuel, in presence of oxygen, produces water. Hydrogen can be directly injected and oxidized in the steam flow to over-heat steam in the Rankine cycle. In such a way the efficiency of the over-heating process increases since it is realized without heat exchange surfaces.

Although in literature there are many works on this new combustion “mode”, there is still the necessity to characterize the process by means of basic studies. The lack of fundamental investigations depends on the difficulty to realize a laboratory scale plants able to work with the extreme high inlet temperatures typical of Mild Condition. These extreme conditions imply a difficult choice of materials and problems of sealing of the reactor. These problems can be more easily overcome in pilot or industrial plant.

The thesis concerns the study of the behavior of model reactors in working conditions typical of a Mild Combustion process.

Basic studies are usually carried out on model reactors typical of chemical engineering. The strength of this approach is the opportunity to highlight particular features of combustion process using different elementary configurations. In fact the combustion process is characterized by very short characteristic time, i.e. for instance
reaction time, and by the interaction between fluid-dynamic and chemistry. Model reactions allow simplifying the study of oxidation reactions since they permit to emphasize particular aspects of the process. Furthermore their complementary allow for a global and structured characterization of combustion process. These features justify their wide spread use in the scientific research field.

Moreover the behavior of model reactors has been widely modeled since the equations, such as mass or energy conservation, necessary to describe such systems, in ideal conditions, are function of a unique parameter, such as time or a spatial coordinate. In fact in literature they are also known as zero- or one-dimensional reactors. This aspect has promoted the development of numerous numerical codes able to simulate the behavior of ideal reactors and the development of a modeling activity of the oxidation process.

Hence they allow for a good comprehension of physical and chemical phenomenology and at the same time for a validation and tuning of predictive models supported by experimental data obtained in specific operative conditions.

In this research group in the past contributions on the study of Mild combustion processes have been realized on different configurations, in particular numerical works on batch reactor, opposed flame configuration and perfect flow stirred reactor.

In this thesis the attention has been focused on the continuous stirred reactor (CSTR) and on the plug flow configuration because they allow for an accurate and exhaustive analysis of the chemistry and of the dynamic evolution of the combustion process.

The continuous stirred reactor (CSTR) is used to study the temporal evolution of the oxidation process and to assess the combustion regimes that can establish as function of several parameters such as pressure, composition of mixtures and temperature. In fact the CSTR offers the possibility to locate exactly in the plane of operative parameters the conditions for which the analyzed system evolves through different regimes. The plug flow
reactor is used to study the evolution of the oxidation process as function of a spatial coordinate. Hence, it represents a good configuration for the assessment of kinetic characteristic times.

Indeed both reactors permit studying the evolution of the oxidation process as a sequence of steady states as function of an unique parameter, which is, in the case of the CSTR, the time and, in the case of the plug flow reactor, the axial coordinate, or equivalently the time.

In the case of the former configuration, it has been possible to carry out a thorough experimental campaign since the reactor and the plant were already available. Firstly the experimental facility has been modified in dependence of needs of this study and all the problems, related to the choice of the reactor, i.e. the mixing, and to the operative mild conditions, i.e. high temperatures, have been faced. As matter of fact during the experimental test on the methane Mild combustion a phenomenology never observed experimentally in the past has been detected. The efforts have been hence focused on the characterization of this new behavior. The analyses have been supported also by means of several software able to simulate the behavior of a perfect stirred flow reactor and several methane oxidation mechanisms.

The contribution of this thesis regarding the other configuration has mainly been the design and setting-up of a tubular flow reactor.

In the dimensioning of the tubular flow reactor, three main problems have been faced. The first concerns the necessity to have a full-developed motion of the fluid inside the reactor to avoid a distribution of residence times of fluid control volumes, the second regards the necessity of having an efficient mixing of reactants inside the reactor. In fact diluent and comburent have to be fed separately from the fuel to avoid undesired reaction in the pre-mixing section where reactants reach very high temperature typical of Mild
processes. From the other side they have to mix in a time relatively short in comparison with the ignition time of any mixtures that forms during the mixing.

The last problem concerns the choice of materials to employ in the manufacture of the reactor since the high inlet temperature involved Mild combustion processes.

The design of the tubular reactor has been realized by means of the classical equations of a plug flow reactor considering the need of a configuration that would allow achieving a high-resolution time of the oxidation process and the need to satisfy safety and space requirements. Furthermore the configuration has been designed in view of optical diagnostic analyses, species samplings and temperature measurements, in order to characterize the evolution of the oxidation process in terms of species concentration and temperature profiles along the axial coordinate.

The choice of the mixing configuration has derived from a thorough study of mixing devices used in combustion systems. Finally the mixing section has been identified, the mixing efficiency has been evaluated as function of the parameters characteristic of the configuration by means of numerical simulations, using a computational fluid-dynamic commercial code (Fluent software) and experimental tests based on fluorescence measurements on a simplified configuration working at room temperature.
Chapter I

Mild Combustion and Problem Identification

During last years one of the main targets in energy production systems development has been to obtain a combustion process that allows to reduce pollutants emission, such as NO\textsubscript{x} and particulate matter, to increase the process effectiveness, and consequently to reduce fuel consumption and CO\textsubscript{2} emission. A combustion chamber using a higher range of temperatures than the traditional one, obtained through a pre-heating of reactants, could allow an higher fuel conversion in CO\textsubscript{2} and H\textsubscript{2}O and the possibility to maximize the enthalpy content exhausted gases to pre-heat air and/or reactants coming inside combustion chamber. This operation may need other fuel to feed burners in pre-combustion chamber and could cause a higher production of pollutants emissions that originate greenhouse effect. On the other side, the possibility to raise work temperature is fought by drastic increasing NO\textsubscript{x} production.

Mild combustion presumes using contemporaneously high temperatures and high dilution of reacting mixture with inert gases, in order to exploit temperature positive effects and, at the same time, to keep under control their gradients. In fact dilution allows increasing thermal capacity of the system and thus restrain adiabatic flame temperature of the system in a range that keeps NO\textsubscript{x} emission under control. In order to keep under control the adiabatic flame temperatures reached during combustion process is necessary to use high mixture dilution levels, so that the composition falls out from LFL-UFL (Lower Flammable Limit – Upper flammable limit). To realize the process combustion is hence necessary to keep the pre-heating temperature higher than the auto-ignition temperature of mixture.
In this way the combustion occurs in homogeneous conditions and in combustion chamber uniform concentration and temperature profiles of the chemical species can be realized.

Using high pre-heating temperatures allows various advantages. In fact a reactants temperature increase allows a higher efficiency of oxidation process. This is caused by a higher speed oxidation in the first part of the process of combustion, for liquids and solids fuel, and acceleration in the physical process of atomisation, vaporization and gasification. This means that the use of high initial temperatures implies a higher flexibility in the choice of the fuel.

![Figure 1.1](image)

**Figure 1.1** Production of soot versus temperature in an impact tube (Wagner, 1983).

The work temperatures should determine an important reduction in the production of NO\textsubscript{x} and soot. In the figure 1.1 soot production is reported as function of working temperature during experiments realized in a tube of “impact” for several fuels in pyrolysis conditions (Wagner, 1993). The reported data identify a range of temperature, independently from the type of fuel, in which the production of particulate matter is meaningful. In particular, the maximum value of fuel conversion into soot is obtained for values of temperature of 1800 K while lower values are obtained for temperature lower than 1600 K or higher than 2000 K.
The figure 1.2 shows the dependence of the production of NO\textsubscript{x} from the temperature in a flame in a gas turbine burner (Y. H. Song et al., 1981). In particular it is possible to see how the production of NO is extremely dependent on the temperature.

![Figure 1.2](image.png)

**Figure 1.2**  Concentrations of NO and NO\textsubscript{2} versus the initial temperature in a gas-turbine burner.

Considering temperature values lower than 1000°K, the NO\textsubscript{x} class is represented by NO\textsubscript{2}. Its molar concentration is almost constant as function of the temperature. For temperatures values higher of 1000°K the NO concentration increases abruptly with the temperature.

The production of this class of pollutants goes by through three kinetic mechanisms; the most important of them is the following one:

\[
\begin{align*}
O + N_2 &\rightarrow NO + N \\
N + O_2 &\rightarrow NO + O \\
N + OH &\rightarrow NO + H
\end{align*}
\]

In steady-state the rate of production of NO is expressed by the equation:
\[ \delta(NO)/\delta t = K [N_2][O] \]

Where \( K \) is the kinetic constant end express the dependence of the reaction velocity from the Temperature. A decrease of temperature and of O radicals concentration implies a minor production of NO. The dilution of the system, for example with gas or exhausted gas recycled in the combustion chamber, should bring to an increase of the thermal capacity of the mixture and so to lower temperatures and concentration of the O radicals, limiting the NO production. The figure 1.3 shows the variation of the NO\(_x\) production in a premixed flame in dependence of the feed fuel/combustive \( R \) on curves normalized on the dilution rate \( \alpha_{N_2} \).

![Figure 1.3](image)

Figure 1.3  NO concentration in a premixed flame normalized to of the feed fuel/combustive \( R \) and on the dilution rate \( \alpha_{N_2} \).

The NO production reaches a maximum value in correspondence of the stoichiometric ratio feed \( R = 1 \), that implies the system reaches the maximum flame adiabatic temperature, meanwhile an increase of the dilution degree \( \alpha_{N_2} \) lowers the production of NO\(_x\). In fact, increasing the dilution rate of the system, the thermal
capacity of the system increases and the adiabatic temperature decreases leading to a reduction of NO\textsubscript{x} production.

The heat capacity of the system can be enhanced using inert species, such as hydrogen, or recycling exhaust gases that have a high content of steam water and carbon dioxide. This last solution is very attractive since it assures high dilution level and meanwhile pre-heating of reactants up to temperature necessary to sustain the oxidation process.

**Definition of Mild Combustion**

It is possible to give a thorough definition of the Mild combustion as follows (Cavaliere et al., 2000):

“A combustion process in whatever reactor is named “mild” when the auto-ignition temperature of reactants is lower than the inlet temperature of the principal flow of reactants and higher than the maximum increase of temperature in the reactor”.

In figure 1.4, it is possible to identify the areas in which there are several types of combustion in dependence of the inlet temperature and the increase of temperature during the process.

It is possible to give other definitions of the Mild combustion that stresses the peculiar characteristics of such a process. In particular Peters et al. (2000) has suggested an analytic definition basing on the absence of ignition and of extinction of oxidation process that occurs for highly diluted and pre-heated mixtures.
Figure 1.4  Areas of existence of the several types of combustion (Cavaliere et al., 2000).

In particular the authors speak about a fuel-comburent-diluent system perfectly mixed, in flow and in adiabatic system considering a kinetic of reaction of the first order with a reaction rate defined by the following equation:

$$\omega = \frac{B_0}{W_F} \exp(-E/RT)$$

In a-dimensional terms the representative equations of the system are:

$$\frac{dY}{dt} = 1 - Y - Da \cdot Y \exp\left(-\frac{E}{T}\right) \quad (1.1)$$

$$\frac{dT}{dt} = T + Q \cdot Da \cdot Y \exp\left(-\frac{E}{T}\right) \quad (1.2)$$

where $Y = \frac{Y_{Fu}}{Y_F}$; $Da = Bt$; $T = T/Tu$; $E = E/RTu$; $Q = QY_{Fu}/cpW_F Tu$. 
In these correlations $Y$ represents the mass fractions, $T$ the temperatures, $Da$ is the Damkoehler number. The subscript $F$ regards the fuel while the subscript $u$ concerns about the starting condition of the systems. The behaviour of the system can be characterized on the basis of the time reaction $B^{-1}$ and on the permanence time $\tau = m/M$.

In steady state the following relations represent the solutions of the system:

$$1 - T_s + Da (1 + Q - T_s) \exp(-E/T_s) = 0$$

The figure 1.5 reports the system temperature in dependence of the Damkoehler number on curves parametric in the a-dimensional parameter $E$. The value of the parameter $Q$ in this case graph is 4, $T_u=1$ for $Y=1$ while $T_u=1+Q$ for $Y=0$.

Changing the value $E$ the curve assumes a characteristic “S” shape, hence three solutions can be obtained. The described curve indicates a hysteresis behaviour and the points $Q$ and $I$ are bifurcation points of the system. In particular the $I$ point is an ignition point: for values of Damkoehler number is equal to $Da_I$ the solutions moves up to the superior branch; the point $Q$ is a turn-off point of the reactor and so the solution of the superior branch falls down to the inferior branch.

It possible to analytically find the vertical tangent to the curve by setting the following condition:

$$\delta Da/\delta T_s = 0$$

and the roots of the equation obtained are:

$$TI = (2 + Q)E + [(EQ-4(1+Q)EQ]^{1/2}$$

$$TQ = (2 + Q)E + [(EQ-4(1+Q)EQ]^{1/2}$$

The condition for which the ignition point and the extinction point are the same implies:
\[ E = 4 \frac{(1+Q)}{Q} \]

If it is set the condition \( E \geq 4 \frac{(1+Q)}{Q} \) it is not possible that the two points are real and distinct solutions and so curves like “S” with multiple solutions are not possible solutions. In these conditions it is possible to have ignitions or extinguishments but just a soft passage from the conditions of turn-off reactor to that one of turn-on reactor.

![Figure 1.5](image)

*Figure 1.5  Temperature (a-dimensional) of work in a CSTR in dependence of the Damkoehler number (Peters et al., 2000)*

This is the condition for which the combustion is named Mild. Peters associates the absence of ignition and extinguishment of the oxidation reaction to the peculiar absence of noise of the Mild process. For this particular feature this new combustion process is also referred in literature with the angles axon term “noiseless”.
Characteristics of the Mild Combustion

In the conventional burners the real chemical reactor is the steady front flame that is an area stretched by turbulence, on which radical mechanisms typical of combustion processes occur. The thickness of the front of flame is very limited but it hosts great temperature and species concentration gradients. The stability and the location in the combustion chamber of the front of flame depend on many fluid-dynamics parameters, thus the design of system geometry is very complicated.

If mixture is highly diluted (beyond flammability limits) and heated up to temperatures that allow for mixture auto-ignition, there will not be a front flame but a reaction volume that extends to the whole combustion chamber. Furthermore in these operative conditions, there are no problems related to flame instability, hence this results in a simplification of reactants mixing and flame stabilization devices.

This is what happens in Mild combustion processes. The elevated auto-ignition delay, the relatively low oxygen concentration and the high flow rates, imposed by the high dilution degrees, determine that the concentration of the chemical species and temperatures in the combustion chamber is almost uniform (Milani et al., 2000). The presence of substances beaming as like as H₂O and CO₂ makes the thermal gradient be constricted. The combustion chamber temperature, in a process based on this new combustion mode, is comparable to the average temperature of a traditional combustion chamber; this implies that materials used for combustion chambers are the same of a traditional system but, because of the homogeneity of Mild processes, material will undergo lower thermal stresses.

The uniformity of the temperature assures that exhausted gases coming out from
the combustion chamber have a higher enthalpy content in comparison with traditional systems, that can be used to pre-heat the fresh reactants entering the combustion chamber. The recycling of exhausted gases implies the use of minor amount of fuel, that would be employed to pre-heat the fresh gases, and consequently a lower emission of pollutants and a lower exercise cost; furthermore the minor number of pollutants abatement devices imply a meaningful reduction of plant costs.

**Flameless Combustion**

There have been several experimental studies aimed to characterize the flame and the combustion products by means of optical analyses. In particular Gupta (2000) has investigated the light emission coming flames of several fuels using air pre-heated up to 900°C-1100°C and oxygen concentration comprised between 5% and 21%. The author demonstrated that flame presents several colours in dependence of dilution degree of mixtures: from yellow to blue, from blue to light green, to green and in some conditions the flame does not present any emission in the visible spectrum.

The dimension and the colour of flames depend on several parameters such as the pre-heating temperature, the oxygen concentration and the fuel and diluent nature. In particular, the reaction volume grows up with temperature and with the going-down of oxygen concentration. This trend was confirmed considering the combustion of propane as function of varying the oxygen concentration and temperature. Flames showed a blue colour for temperatures in the range 900°C-950°C and oxygen concentrations between 5% and 15%. For high temperatures around 1100°C and low reactants feed rates the flame emission was too high. At the same temperatures and for an oxygen concentration equal to 21% the flame was completely yellow. At higher temperatures and lower oxygen concentrations (2-5%) flame was green. This colour
indicates high concentration of the compounds C$_2$ in the flame in this condition. When the concentration is lower than 2%, there is not any light emission in the visible spectrum. This condition is denoted as “combustion without flame” and the combustion process is referred as “Flameless Combustion”. The green flame observed for the propane at the low percentages of oxygen has not been identified for the methane. This demonstrates that flames light emission depends also on fuel.

Shimo et al. (2000) showed that the kerosene at high pre-heating temperatures and low oxygen concentration (5%) emits a green flame whether diluted with nitrogen, blue-orange whether diluted with argon and a different colour in presence of CO$_2$. The difference in light emissions is probably due to the different thermal capacities of diluents and to the different interaction with the oxidation process.

**Mild Combustion and Hydrogen**

The achievement of an energetic and economic system based on hydrogen is mainly hindered by its characteristic high reactivity and calorific power that make hard the switch from traditional energy conversion systems to the use of such fuel. In this sense the shift cannot be immediate but intermediate steps should be considered. The high reactivity of hydrogen can be controlled by using Mild Combustion conditions (high dilution level and high inlet temperatures). Here there are reported some example of how Mild combustion processes and the hydrogen use can be coupled toghether.

Hydrogen can be used in steam turbines with several advantages for the process in terms of environmental impact and thermodynamic efficiency. As matter of fact Hydrogen-operated steam turbines can give out clean exhaust emissions and thus
avoid the need of any exhaust gas treatment. In contrast to fossil-fuel operation, hydrogen-operated gas turbine installations do not give any ash particles or other residue production. Thus problems of corrosion or any other deposits on blades are intrinsically avoided.

It is well known hydrogen has a very high calorific power. It means that in the combustion chamber very high temperatures will be reached. The broad temperature difference in principle can be exploited to a point of thermodynamic advantage for electrical power generation. Furthermore the use of pure hydrogen-oxygen/water in place of air permits direct utilization of steam contained in the combustion gas without any boiler, thus it takes away the need to burn other fossil fuels (Kato et al. 1997). This working parameter has to be monitored and controlled in order to avoid great damages to turbines. This target can be reached simply enhancing the heat capacity of the system thus lowering the adiabatic temperature. Hence great amount of diluents such as water can be used as main flow and therefore the system works in conditions typical of “Mild” processes.

The ENEA group has proposed a new technology that forecasts the use of hydrogen in a thermodynamic cycle based on the Rankine and the Joule cycles. In this project oxygen is fed directly into in the combustion chamber where it mixes up with a vapour-hydrogen flow, produced in the first part of the plant by means of a coal gasification process. In this way hydrogen reacts with oxygen producing steam and overheating the flow itself. The heating process efficiency is significantly enhanced since it happens without heat-exchange surfaces. Temperatures reached in the combustion chamber are very high (approximately 1500K), consequently the efficiency of the cycle increases from 38.82% in a conventional cycle to 49.65%. This
efficiency can be still enhanced to 70% by different ways like a combination with a gas turbine and using different pressure values and inlet temperatures.

Hydrogen has several characteristics that make it quite attractive for employment in engines (Karim, 2003). In particular hydrogen has a very wide flammability range and a high flame propagation speed. These features would permit the evolution of the oxidation process also for ultra-lean and highly diluted mixtures. Hydrocarbons cannot be used in the same operative conditions because of their narrower flammability range and lower flames speed. Furthermore hydrogen combustion is a clean process since it produces water and not pollutants typical of hydrocarbons engine such as carbon monoxide, aliphatic and cyclic hydrocarbons compounds.

On the other hand, problems as abnormally high pressure rise, occurrence of pre-ignition in combustion chamber and backfire into the intake manifold, occasional backfire in very lean hydrogen-air mixture or in idling operation are very common (Das, 1996). These undesired phenomena cause the engine to stop and great damage to the system. They are due to hydrogen high flame propagation, its low minimum ignition energy and wide ignition limits.

These problems represent a hurdle in the growth of hydrogen engine and require high technology knowledges to control the combustion process and its burning characteristic times. Many researchers have suggested exhaust gas recalculation (EGR), hence high dilution levels, as an effective method for decreasing the tendency to backfire. This solution has been found to be very useful in doing away with the backfire tendency. Meanwhile the high dilution levels induce a marked reduction of nitrogen oxides emissions (Heffel, 2003).
Hydrogen can be widely used for its characteristics in other fields: it is a common practice to add small amount of hydrogen to mixtures to have fuels with properties more attractive from a practical point of view. For examples in the work of Kumar (Kumar et al., 2002) hydrogen is added to a vegetable oil fuelled compression ignition engine to enhance the performance of the engine. Since hydrogen can be added in any proportion to other fuels (Marinov et al., 1996), their characteristics can be easily adapted to any practical applications. It means there is no need to change technologies on the basis of fuels characteristics but it is possible to change the fuel properties themselves by adding hydrogen.

As matter of fact the possible ideal applications of H₂ as fuel are numerous but many applications have to deal with hydrogen high reactivity.

There are other aspects very relevant in the full understanding of problems related to achieve a productive- economical system based on hydrogen: H₂ can not be strictly defined as an energy source but as an energy vector or carrier since its production comes from other energetic sources (Chen et al., 2003). Although it is the most common element on our hearth it is present in different compounds especially in water but it is not available as molecular hydrogen. It means a production process is required to produce the clean fuel. Nowadays there are several ways such as thermal, electrolytic, or photolytic applied to fossil fuels, biomass or water.

The most common and economical processes are the steam reforming and partial oxidation (http://www.minerva.unito.it, 2003). Unfortunately these processes can not be split from the production of CO₂ since the raw materials are fossil fuels but the research common effort is to have more efficient CO₂ separation processes, for
example by means of membranes (Eklund et al., 2003), or plants that allow for the CO\textsubscript{2} sequestration. Unfortunately the available technologies make H\textsubscript{2} production cost increase

There are other several processes for the production of the clean fuel such as water electrolysis, gasification of coal and gasification or pyrolysis of biomass. There are also methods which represent the trend to produce H\textsubscript{2} using sustainable sources as photo biological or photo electrochemical processes, as for example photovoltaic cells which use the sun energy (http://www.digilander.libero.it, 2003).

Gasification and the other processes based on sustainable energy represent good solutions to the environmental problems and to the fossil fuel depletion but unfortunately also these new technologies need to be improved and their cost is still too high and makes them not competitive with the steam reforming and partial oxidation processes (http://www.minerva.unito.it, 2003). Anyway the trend to develop new technologies or use new fuel states a more sensitive attitude towards the environmental impact problems. The research is trying to improve the existing technologies for the abatement of pollutants from industrial plants and production processes themselves in order to enhance the energy yield with the lowest pollutant production.

As matter of facts the use of hydrogen as an energy carrier or as major fuel requires developments in several industry segments, including production, delivery, storage and conversion.

Hence the affirmation of H\textsubscript{2} is a long-term project. In the phase of transition from a system based from fossil fuel to hydrogen, fuels from gasification of coal or biomass are destined to play a very important role. In particular the use of biomass is a very promising process since it is environmental friendly since biomass is a CO\textsubscript{2}
neutral resource in the life cycle in fact CO$_2$ is consumed by biomass during the growth and just the same CO$_2$ amount is released in the conversion (Chen et al., 2003). Furthermore biomass is quite easily obtainable on the hearth through the rational collection of byproducts from agricultural and forestry industries. Biomass can also reduce the dependence of the energy production and economic system from fossil fuel whose reservoir are decreasing gradually. An example as waste material and biomass have been employed comes from the Advanced Energy Research Corporation (http://www.aercoline.com, 2003). They have developed a gas called TrueFuel mainly composed by a hydrogen(50%)-CO which comes from a process that combines water and carbon waste to develop a hydrogen-CO gas. The carbon waste used as a raw material can include: coal, high sulfur coal, rubber tires, organic waste material, and biomass such as sugar cane waste. The water used as a raw material can include: polluted water, salt water, or even contaminated water from food processor or pharmaceutical companies. The fuel has a quite wide range of application including turbine engine fuel, metal cutting and glass working, piston engine fuel and industrial process heat. Furthermore NOx emission for turbine and hydrocarbon emission for diesel and gasoline engine can be highly reduced.

These kinds of fuels are composed by different light hydrocarbons with relatively high H$_2$ content and a very high diluents content such as water or CO$_2$. These mixtures are themselves in “mild” conditions and thus the combustion of these low calorific gaseous requires a thorough study in order to understand the best conditions in which employ these fuels. Their use allows for the employment of hydrogen since their dilution degree can mitigate the high hydrogen reactivity and, at the same time, they are produced from waste organic materials which allow for a reduction of the dependence of the system from fossil fuels. They seem to be the key
of this transition period. Anyway they have a high content of CO, CO$_2$ and other hydrocarbons. It means a process which employs biofuels will have to deal with CO$_2$ emission. In order to avoid this problem several projects are being investigated. For example ENEA is developing a process in which the coal in presence of water is gasified into H$_2$ and CO$_2$. The H$_2$ is burnt with zero emissions while CO$_2$ is sequestrated by a carbonaceous process and stored in the ground. This process allows the coal to be considered as a almost cleaned fuel with “zero emission”. The whole process is named ZECOTECH (Zero Emission Combustion Technology using Hydrogen) to underline the process does not allow CO2 emission into the atmosphere.

Since these fuels are supposed to have an important role researchers are trying to improve production processes. Several experiments have put in result gasification for waste material can be better if small addictions of oxygen are added to the mix. In particular Jinno (Jinno et al., 2002) run an experiment of gasification of toluene. The aim of their work was to have a comprehensive understanding on thermal destruction behavior of tar components under high temperature. They found out small O$_2$ addiction results in a suppression of tar and soot. This effect is maybe due to the reaction of H$_2$, produced by the gasification process, and the fed O$_2$ which free radicals. It is well known that the oxidation of these compounds is faster and more efficient if it is run in an environment rich in OH, H and O radicals. Furthermore they found out the whole process can be realized at a lower temperature in the case O$_2$ addiction are considered. In fact it allows to reduce the working temperature from 1400K to 1100K with a benefit on other fuel consumption.

These results suggest that small amount of hydrogen and oxygen can be employed in purification processes in order to enhance the efficiency of the process.
The oxidation of compounds as VOCs, PAH and tar is a common practice to lower the emission of these pollutants in atmosphere. It can be realized by a catalytic oxidation or a thermal oxidation. The latter is realized for temperatures comprised in the range 1000-1500K, residence time range from 0.5 to 2 sec, high turbulence and with oxygen excess (Donley and Lewandowsky). Oxidizers will typically achieve efficiencies of over 99% with higher combustion chamber temperatures and longer retention time. Anyway it is well known the oxidation process can be widely improved if the amount of radicals OH is increased. It is also evident from kinetics data provided by Ranzi (Ranzi et al., 2001). In particular in his CH$_4$ oxidation mechanism the oxidation reaction of benzene with O$_2$ has an activation energy of $E_a = 51663$ J/mole whilst the benzene oxidation by OH has a $E_a = -53.6$ J/mole. Several studies were also run about the influence of small H$_2$O$_2$ amount into hot gases on VOCs oxidation (Cooper et al., 1991). H$_2$O$_2$ is an important source of OH radicals which have extremely high oxidation potential and are relatively nonspecific oxidizing agents. Such enhancement might result in lower incineration temperatures, shorter residence times, and higher destruction and removal efficiency (Martinez et al., 1995). Even if the process is quite simple, kinetic studies of the oxidation of PAHs are required since it is still unclear. Brezinsky (Brezinsky, 1986) performed some experiments on aromatic hydrocarbons oxidation at high temperature. He considered some pathways and he underlined how aromatic oxidation is quite different from hydrocarbon oxidation since benzyl radicals produced during the oxidation are themselves oxidized through atypical radical-radical reactions because they are long lived resonantly stabilized species. The study of these processes in diluted condition could relax the oxidation time and be very useful in understanding the whole process.

The OH radical has the same oxidant potential also for soot as it is evident from
experiments by Neoh (Neoh et al., 1980). From simple thermodynamic calculations it was seen that OH radical concentrations is higher than O$_2$ concentration for high temperature and rich condition. Further analyses showed the soot oxidation rate depends straightforwardly on OH concentration and that O$_2$ has a great importance for leaner conditions (Xu et al., 2003). Xu himself suggests additional analyses should be run on effects of pressure, effects of relatively high temperature (2000 K) and on effects of fuel type, especially oxygen-containing fuels that should increase OH concentration at fuel-rich conditions.

### Methane Oxidation in Mild Conditions

Mild combustion is hence characterized by the use of high inlet temperatures and high dilution degree. These working conditions imply, as discussed in the previous paragraph, that the oxidation process occurs in the whole combustion chamber realizing uniform temperature and species concentrations profiles.

The hydrocarbons oxidation occurs in non-standard condition hence it is important to understand the effect that the high inlet temperatures and dilution degree have on the evolution of the kinetic process.

In literature there are several kinetic models that can be used to perform a preliminary analysis of the oxidation of hydrocarbons in Mild condition. In particular de Joannon et al. (2000) studied the oxidation of methane in diluted conditions as function of several parameters, such as the inlet temperatures. The analysis has been realized is a Stirred Flow Reactor, since the homogeneity of combustion in Mild conditions allows to schematise the process, in first approximation, by means of a
The aim of the work was the characterization of the kinetic pathways of methane oxidation process as function of several residence times and inlet temperatures for a mixture characterized by a C/O feed ratio equal to 1 in adiabatic condition. The dilution is realized with nitrogen and the dilution degree of the mixture is 0.85.

The kinetic model used is the oxidation mechanism of the methane of “Warnatz” (1997) and the software used for these simulations was the ChemKin.

It has been recognized three kinetic regimens for oxidation of methane.

The first regimen is the oxidative one, the second is the recombination, and the third is the pyrolysis.

The first regimen concerns work temperature until 1300°k, and the products of reaction are principally CO$_2$ and H$_2$O. The second regimen arrives until 1700°k and considers the formation of species like CO and H$_2$O, compounds of recombination C$_2$ and at the last H$_2$. The pyrolytic regime contemplates the formation of CO and H$_2$ as main product. In this regime we have the breakdown of CO$_2$ and H$_2$O that give rise to oxygen atoms, they can oxidize the C$_2$ species eliminating the precursor of the soot.

Therefore the presence of CO$_2$ and H$_2$O can meaningful the formation of soot.

In this work it has been demonstrated that Mild combustion processes can be more properly schematised by means of several perfectly mixed reactors, each of which with a fixed rate of C/O. In particular the rate C/O change, along a series of reactors, from a value corresponding to a rich condition until to stoichiometric values in the last reactor. In order to change the C/O rate each reactor must have two different feeds, the first composed by the gases coming out from the previous reactor, the second one will be a new oxidant flow inside. An example of this scheme is reported in the figure 1.6. In it is represented a burner fed, in the central area with the
air flow strongly pre-heated (1300°K) and diluted (X_{O_2}=0.05) while the fuel is introduced at the atmosphere temperature and pure at the periphery of the burner.

![Figure 1.6 Scheme of a burner in which there’s the mild combustion process (Cavaliere et al., 1999)](image)

The zones in which oxidation occurs are represented by two series of five reactors fed by an air flow having the same characteristics of the fed air.

A new simulation has studied the distribution of CO in dependence of the reactors in series showing that the yield of methane into carbon monoxide decreases along the series of the reactors. In the last one the CO\textsubscript{2} yield is unitary.

**Aim of the thesis**

The thesis concerns the study of the behavior of model reactors in working conditions typical of a Mild Combustion process. This new combustion “mode” forecasts the use of a high dilution degrees and high inlet temperatures. These operative conditions allow for a reducing of pollutants formation, such as NOx and soot, and save energy. Hence this is a very promising process in the framework of the development of new combustion technologies aimed to reduce the environmental impact of combustion systems.
Although in literature there are many works on this new combustion mode, there is still the necessity to characterize the process by means of basic studies. This depends on the difficulty to realize in a laboratory scale plants able to work with the extreme high inlet temperatures typical of Mild Condition. These extreme conditions imply a difficult choice of materials and problems of sealing of the reactor. These problems can be more easily overcome in pilot or industrial plant.

Basic studies usually carried out by means of model reactors typical of chemical engineering. The strength of this approach is the opportunity to highlight particular features of combustion process using different elementary configurations. In fact the combustion process is characterized by very short characteristic time, i.e. for instance reaction time, and by the interaction between fluid-dynamic and chemistry. Model reactions allow simplifying the study of oxidation reactions since they permit to emphasize particular aspects of the process. Furthermore their complementary allow for a global and structured characterization of the process itself. These features justify their wide spread use in the research field.

Moreover the behavior of model reactors has been widely modeled since the equations, such as mass or energy conservation, necessary to describe such systems, in ideal conditions, are function of just one coordinate. This aspect has promoted the development of numerous numerical codes able to simulate the behavior of ideal reactors and the development of a modeling activity of the oxidation process.

Hence they allow for a good comprehension of physical and chemical phenomenology and meanwhile for a validation and tuning of predictive models supported by experimental data obtained in precise operative conditions.

In this research group in the past contributions on the study of Mild combustion processes have been realized on different configurations, in particular numerical
works on batch reactor, opposed flame configuration and perfect flow stirred reactor. (A. Matarazzo et al., 2005, P. Sabia et al., 2005a; Sabia et al., 2005b).

In this thesis the attention has been focused on the continuous stirred reactor (CSTR) on and the plug flow configuration because they allow for an accurate and structured analysis of the kinetic and the dynamic evolution of the combustion process.

Hence the aim of the thesis has been the characterization of the effect of the high dilution degree and of the high inlet temperature on the evolution of the oxidation process of methane mixtures and the identification of combustion regimes that enstablish in Mild combustion conditions.
Chapter II

Hydrocarbons Oxidation Mechanisms in Combustion Processes

Introduction

Combustion is a chemical process characterized by oxidative exothermic reactions having high activation energies. This definition is quite generic but puts in evidence its principal characteristics.

The process peculiarity is due to its evolution through breaching kinetic reactions. The high system reactivity is due to the presence of very reactive species, named radicals, and (to the presence) of branching reactions that increase their concentration. Indeed radicals coming from a reaction are involved in other reactions in which fuel and comburent compounds lead, through several steps, to the formation of CO\textsubscript{2} and H\textsubscript{2}O. This aspect underlines the autocatalytic nature of combustion processes.

The kinetic mechanism that characterizes a combustion process can be schematized by a sequence of initiation, oxidizing and termination reactions. The first one causes the comburent compound breakdown and the formation of the first radicals. These reactions can be simply thermal decompositions in case of high temperatures oxidation.

The formed radicals evolve through oxidizing reactions that can be propagation or branching ones. The former does not involve an increase of radical concentration while the latter (otherwise) increases radical production so that the system becomes very reactive. This sequential production mechanism implies the short kinetic time of combustion process.

Above s some example of branching reactions are here presented:
\[ \text{H} + \text{O}_2 \rightarrow \text{OH} + \text{O} \]

\[ \text{O} + \text{H}_2 \rightarrow \text{OH} + \text{H} \]

Once fuel and comburent are ended, terminal reactions cause the depletion of radical species leading to the formation of stable compounds. If the temperature is sufficiently high, recombination reactions could lead to the formation of higher molecular weight compounds. As matter of fact, a thermodynamic analysis carried out on the basis of the Francis diagram has shown the several hydrocarbons stability is related to the temperature so that recombining reactions are foreseeable.

Kinetic oxidation pathways of a hydrocarbon compounds depend on the temperature and the pressure and let the fuel-comburent system evolve in different ways involving several phenomenologies. For example, as the inlet temperature increases, a hydrocarbon could cause a slow combustion, cool flames or finally high temperature combustion.

Later on, aliphatic hydrocarbon kinetic oxidation pathways will be shortly described, characterized by a particular complex kinetic. More over, because of these mechanisms involve simple molecules such as hydrogen and carbon monoxide their oxidizing mechanisms will be shown separately.

**H₂-O₂ System**

H₂-O₂ system has been widely studied because of its simplicity and its importance. A limited reaction, kinetic and thermodynamic constant number is to be used to describe the H₂-O₂ system, especially if compared to each other oxidation fuel mechanisms. Moreover, the H₂-O₂ system perfect knowledge results very useful for the understanding of the several kinetic oxidizing pathways of any hydrocarbon because they are supported by H₂-O₂ system radical reactions.
The radical species involved in this mechanism are H, HO$_2$, O e OH. They take place to the several branching and propagation reactions according to the following mechanisms (Westbrook 1984):

\[
\begin{align*}
H + O_2 & \rightarrow O + OH \quad (a) \\
O + H_2 & \rightarrow OH + H \quad (b) \\
H_2 + OH & \rightarrow H_2O + H \quad (c) \\
O + H_2O & \rightarrow OH + OH \quad (d)
\end{align*}
\]

Termination reactions are here reported:

\[
\begin{align*}
H + H + M & \rightarrow H_2 + M \quad (a) \\
b) O + O & \rightarrow O_2 + M \quad (b) \\
c) O + H + M & \rightarrow OH + M \quad (c) \\
d) H + OH + M & \rightarrow H_2O + M \quad (d)
\end{align*}
\]

The radical HO$_2$ is mainly produced by means of the following reaction:

\[
H + O_2 + M \rightarrow HO_2 + M \quad (2.3)
\]

And it is consumed by these reactions:

\[
\begin{align*}
HO_2 + H & \rightarrow H_2 + O_2 \quad (a) \\
HO_2 + H & \rightarrow OH + OH \quad (b) \\
HO_2 + H & \rightarrow H_2O + O \quad (c) \\
HO_2 + HO_2 & \rightarrow H_2O + O_2 \quad (d) \\
HO_2 + O & \rightarrow O_2 + OH \quad (e)
\end{align*}
\]
O + OH + M → HO₂ + M \quad (f)

Moreover hydro-peroxide radical could react with itself and lead to the hydro-peroxide formation by

\[ \text{HO}_2 + \text{HO}_2 \rightarrow \text{H}_2\text{O}_2 + \text{O}_2 \quad (2.5) \]

It is consumed by the following reactions:

\[ \text{H}_2\text{O}_2 + \text{OH} \rightarrow \text{H}_2\text{O} + \text{HO}_2 \quad (a) \]

\[ \text{H}_2\text{O}_2 + \text{H} \rightarrow \text{H}_2\text{O} + \text{OH} \quad (b) \]

\[ \text{H}_2\text{O}_2 + \text{H} \rightarrow \text{HO}_2 + \text{H}_2 \quad (c) \]

\[ \text{H}_2\text{O}_2 + \text{M} \rightarrow \text{OH} + \text{OH} + \text{M} \quad (d) \]

This last reaction involves an increase in radical concentration and makes faster the combustion process. In high temperature combustion of fuels such as hydrocarbons and hydrogen, 2.1-a reaction is the most important branching one. It consumes H radical and leads to the formation of two radical species (O and OH). Oxygen atom could react according to 2.1-b, leading to the formation of a new H radical and a new OH.

An increase of H radicals in the system results in a high the oxidizing global rate because branching reaction 2.1-a will be faster. At the same time, processes reducing H radicals concentration or competitive reactions will inhibit the combustion process.

The propagation reaction 2.3 can have this role subtracting H radicals to the branching reaction. The velocity of this reaction depends on the concentration of the third compound M and on the total system pressure.

The laminar flame speed variation in methane-air systems, CH₃OH-air and C₂H₄-air demonstrates as such a competition conditions the combustion process evolution. In fact, experimental data on laminar flame speed as a function of the pressure have highlighted
that this parameter decreases gradually with the increasing pressure starting from lower values than atmospheric pressure to atmospheric ones. A further rise up to 5 atm causes a stronger reduction in laminar velocity because the two reactions become competitive. Hence, up to an atmospheric pressure value the weak effect of pressure can be observed while, for higher values, there is the effect of the two reactions competition too. In fact, for high values, the reaction 2.3 depends on the velocity of a propagation reaction and no more on a branching one.

The propagation reaction 2.3, coupled with 2.5 and 2.6-d, involves radicals to sustain the combustion process.

Beside a strong pressure dependence, the reaction 2.3 has an activation energy lower than 2.1-a that decreases with the temperature rising. The reaction 2.3 becomes the principal pathway in comparison with the reaction 2.1-a for low temperature values and high pressure ones.

Another example, which underlines that H radicals are important for the combustion process evolution at high temperature, is the variation of oxidation velocity when there are alogenated compounds such as F and Br. These ones indeed can subtract H radicals from the system and raise H$_2$ according to the following steps:

\[
\begin{align*}
HX + H &= H_2 + X \quad (a) \\
X_2 + H &= HX + X \quad (b) \\
X + X + M &= X_2 + M \quad (c)
\end{align*}
\]

In this scheme the species X indicates the alogenated compound. Hydrocarbon reactions with atomic hydrogen are competitive with the branching reaction for temperatures typical of combustion processes.

The tab.2.1 shows radical hydrogen reaction velocity with several hydrocarbons and oxygenated compounds at 1000K. The values are to be compared to the oxidation velocity
of reactions that involve H radicals. From the tab it is evident that the H firstly 
dehydrogenises compounds with carbon atoms, and then, after the depletion of such 
compounds, it realize the oxidation reaction 2.1-a.

<table>
<thead>
<tr>
<th>Reactions</th>
<th>Reaction velocity equation</th>
<th>Velocity at T= 1000K</th>
</tr>
</thead>
<tbody>
<tr>
<td>H + O₂ → OH + H</td>
<td>5.13*10^{16}T^{-0.816} exp(-16507/RT)</td>
<td>4.5*10^{10}</td>
</tr>
<tr>
<td>H + CH₄ → CH₃ + H₂</td>
<td>2.24*10^{4}T^{3} exp(-8750/RT)</td>
<td>2.7*10^{11}</td>
</tr>
<tr>
<td>H + C₂H₆ → C₂H₅ + H₂</td>
<td>5.37*10^{2}T^{3.5} exp(-5200/RT)</td>
<td>1.2*10^{12}</td>
</tr>
<tr>
<td>H + C₂H₄ → C₂H₃ + H₂</td>
<td>1.50*10^{7}T^{2} exp(-6000/RT)</td>
<td>7.3*10^{11}</td>
</tr>
<tr>
<td>H + CH₂O → HCO + H₂</td>
<td>3.30*10^{14} exp(-10500/RT)</td>
<td>1.7*10^{12}</td>
</tr>
<tr>
<td>H + CH₃OH → CH₂OH + H₂</td>
<td>3.00*10^{13} exp(-7000/RT)</td>
<td>8.9*10^{11}</td>
</tr>
<tr>
<td>H + CH₃OH → CH₃ + H₂O</td>
<td>5.25*10^{12} exp(-5340/RT)</td>
<td>3.6*10^{11}</td>
</tr>
<tr>
<td>H + C₃H₈ → iC₃H₇ + H₂</td>
<td>1.46*10^{7}T^{2} exp(-5000/RT)</td>
<td>1.2*10^{12}</td>
</tr>
<tr>
<td>H + C₃H₈ → nC₃H₇ + H₂</td>
<td>9.38*10^{7}T^{2} exp(-7700/RT)</td>
<td>2.0*10^{12}</td>
</tr>
<tr>
<td>H + C₂H₂ → C₂H + H₂</td>
<td>2.00*10^{14}T^{14} exp(-19000/RT)</td>
<td>1.4*10^{10}</td>
</tr>
<tr>
<td>H + C₄H₁₀ → nC₄H₉ +H₂</td>
<td>1.30*10^{14}T^{14} exp(-9700/RT)</td>
<td>9.9*10^{11}</td>
</tr>
<tr>
<td>H + C₄H₁₀ → sC₄H₉ +H₂</td>
<td>2.00*10^{14}T^{14} exp(-8300/RT)</td>
<td>3.1*10^{12}</td>
</tr>
</tbody>
</table>

Tab. 2.1 Velocity of reactions that involve the radical H.

**Oxidation Mechanism of Hydrocarbons**

The first reaction that occurs during the oxidation process of a generic paraffin 
hydrocarbons RH is the formation of an alkyl radical.

In fact, the C-H bond is weaker than the C-C bond; hence it is easier to extract it. At 
the beginning of the oxidation process, the hydrocarbons dehydrogenation is realized by
means of oxygen molecules according this reaction

$$RH + O_2 \rightarrow R' + HO_2 \quad (2.8)$$

The reaction is characterized by high activation energy (>40 Kcal/mole). Therefore at low temperature such a reaction is relatively slow. The radical $R'$ starts chain reactions that lead to an increment of the pool of radicals in the system. Radicals can easily extract hydrogen atoms from the generic hydrocarbon $RH$. The radical $R'$ can react in two different ways:

$$R' + O_2 \leftrightarrow RO_2' \quad (2.9)$$

$$R' + O_2 \rightarrow \text{olefin} + HO_2 \quad (2.10)$$

The former reaction is exothermic and reversible and has an activation energy very low, while the latter is irreversible and has an activation energy significantly high.

Hence, whether the temperature enhances, the equilibrium of reaction 2.9 goes backwards, while reaction 2.10 accelerates. It can be faster then the former reaction.

Both the reaction produce peroxides that are species very reactive that can easily promote extraction reactions of H atoms from any donator present in the mixture, hence the branching mechanism can starts.

The possible reactions are:

$$RO_2' + RH \rightarrow ROOH + R' \quad (2.11)$$

$$HO_2' + RH \rightarrow HOOH + R' \quad (2.12)$$

During the evolution of a such a kinetic mechanism, other radical species, such as aldehydes, that can easily donate H atoms. In fact the C-H bond is woken by the presence of the O atom that has a high electro-negativity.

Since at high temperatures the reaction 2.11 is faster than the reaction 2.12, with
increasing the temperature the HOOH production is enhanced.

The hydro-peroxides can decompose giving rise to branching reactions with the production of two radicals.

\[
\text{ROOH} \rightarrow \text{RO}^' + \text{OH}^' \quad (2.13)
\]

\[
\text{HOOH} \rightarrow \text{OH}^' + \text{OH}^' \quad (2.14)
\]

These two reactions are very important for the kinetic evolution of the system and are responsible of the auto-catalysis that characterizes the combustion processes.

At low temperatures the branching reaction 2.13 can sustain the oxidation process but the system will evolve through a slow combustion regime. It is characterized by a slow monotonic increase of temperature until a stationary value of temperature and species concentration.

With increasing the temperature the reaction 2.10 becomes less and less fast and as well as the reaction 2.13, while the reaction 2.14 accelerates. This situation implies that the main product is the species \( \text{H}_2\text{O}_2 \). Anyway for temperature lower than 750K this reaction can be neglected since still too low in comparison with the other branching reaction. Indeed the ignition mechanism is still related to reaction 2.13. At the same time, as the temperature increase, the system reactivity becomes slower, in fact if the temperature is lower than 750K, the hydrogen-peroxide can not decompose and hence it can not sustain the oxidation process since it can not provide OH radicals.

This kinetic mechanism explains in a simplified but efficient way the cool flame phenomenology and the negative temperature coefficient (NTC) behavior (Lignola et Reverchon, 1987).

As matter of fact, during experiments on hydrocarbons oxidation in a flow reactor, in non-adiabatic condition, it happens that, when the reaction 2.14 becomes significantly
high, the mean reaction velocity of the system decelerate, and the temperature of the system can lower for the heat exchange to the environment, for the non-adiabatic condition or for the continuous flow inside the reactor. This results in temperature oscillations, this phenomenology has been named “cool” flame.

The negative temperature coefficient implies that increasing the inlet temperature the reactor temperature is increasingly slower.

In fact, a higher temperature means that the reaction 2.14 is faster than reaction 2.23. It implies that the reactor temperature will be lower, since the exothermicity of the system is always less high.

The radical \( \text{RO}' \) can later decompose producing aldehydes and an alchilic radical with a lower molecular weight.

\[
\text{RO}' \rightarrow \text{aldehyde} + Q' \quad (2.15)
\]

The radicals \( \text{RO}' \) e \( \text{OH}' \) can still extract H atoms from the RH hydrocarbon producing alcohol species and water. Such radicals give rise to secondary branching reaction producing again the alchili radical \( R' \).

The termination reactions transform the reactive species to less reactive species. Such reactions can be mainly the following ones:

\[
2 \text{ RO}' \rightarrow \text{prodotti stabili}
\]

\[
\text{RO}' + \text{HO}_2' \rightarrow \text{ROOH} + \text{O}_2 \quad (2.16)
\]

\[
2 \text{ HO}_2' \rightarrow \text{HOOH} + \text{O}_2
\]

In particular these reaction are important in the temperature field of the cool flame. As the temperature increases it can happen that the hydrogen peroxide decomposes and in this case the system evolves trough a high temperature combustion.

A further increase of the temperature implies that the ignition mechanism is to be
attributed to the branching reactions of the system H\textsubscript{2}/O\textsubscript{2}. In fact, for temperature higher than 900K, HO\textsubscript{2} radicals from the production of H\textsubscript{2}O\textsubscript{2} are mainly produced from the propagating reaction already discussed in the previous paragraph.

\[ H + O_2 + M \rightarrow HO_2 + M \] (2.17)

This reaction, together with the decomposition of H\textsubscript{2}O\textsubscript{2}, insure radicals to sustain the combustion process.

For T>1000K this mechanism is in competition with the branching reactions here reported:

\[ H + O_2 \rightarrow OH + O \] (2.19)

\[ O + H_2 \rightarrow OH + H \] (2.20)

These two reactions insure a very high amount of radicals thus a very high reactivity of the system.

**Methane Oxidation Mechanism**

Methane can react firstly through a thermal decomposition reaction (2.21) or through a reaction of extraction of an H atom by the molecular oxygen (2.22), since at the beginning it is the only species available.

\[ CH_4 \rightarrow CH_3 + H \] (2.21)

\[ CH_4 + O_2 \rightarrow CH_3 + OH \] (2.22)

The reaction 2.21 has a lower activation energy in comparison with the one of reaction 2.22. Radicals that form from the former reaction take part in the branching reaction scheme of the system H\textsubscript{2}/O\textsubscript{2}.
The secondary initiation reaction can happen through these reactions:

\[
\begin{align*}
\text{CH}_4 + \text{OH} & \rightarrow \text{CH}_3 + \text{H}_2\text{O} \quad (2.23) \\
\text{CH}_4 + \text{H} & \rightarrow \text{CH}_3 + \text{H}_2 \quad (2.24) \\
\text{CH}_4 + \text{O} & \rightarrow \text{CH}_3 + \text{OH} \quad (2.25) \\
\text{CH}_4 + \text{HO}_2 & \rightarrow \text{CH}_3 + \text{H}_2\text{O}_2 \quad (2.26)
\end{align*}
\]

Then the methyl radical can act in several ways, depending on the temperature and on the availability of the chemical species:

\[
\begin{align*}
\text{CH}_3 + \text{O}_2 & \rightarrow \text{CH}_2\text{O} + \text{OH} \quad (2.27) \\
\text{CH}_3 + \text{HO}_2 & \rightarrow \text{CH}_3\text{O} + \text{OH} \quad (2.28) \\
\text{CH}_3 + \text{O} & \rightarrow \text{CH}_2\text{O} + \text{H} \quad (2.29) \\
\text{CH}_3 + \text{OH} & \rightarrow \text{CH}_3\text{OH} \quad (2.30) \\
\text{CH}_3 + \text{OH} & \rightarrow \text{CH}_2(\text{S}) + \text{H}_2\text{O} \quad (2.31) \\
\text{CH}_3 + \text{CH}_3 & \rightarrow \text{C}_2\text{H}_6 \quad (2.32)
\end{align*}
\]

The recombination reactions of the methyl radical are very important. The oxidation of methane differs from the oxidation of hydrocarbons with a higher molecular weight since the first radical produced is the methyl radical which is hard to oxalate (Westbrook, 1984). The oxidation of CH₃ by means a reaction with O₂ is very slow, at the same time a thermal decomposition of CH₃ requires to high temperatures. In this framework, the recombination reaction covers a very important role in comparison with recombination reaction of hydrocarbons with a higher molecular weight.

The only fast reaction that involves the methyl radical is its oxidation to form CH₃O₂, but it quickly decomposes to form again CH₃ and O₂. Studies realized on the methyl
peroxide reactions in slow combustion regimes of methane and ethane (A.A.Nantashyan et al., 1981), have shown that the methyl peroxide could react with a methyl radical or another molecule of methyl peroxide to form more reactive species such as CH$_3$O, in accordance with the reaction reported below.

\[
\text{CH}_3\text{O}_2 + \text{CH}_3 \rightarrow \text{CH}_3\text{O} + \text{CH}_3\text{O} \quad (2.33)
\]

\[
\text{CH}_3\text{O}_2 + \text{CH}_3\text{O}_2 \rightarrow 2\text{CH}_3\text{O} + \text{O}_2 \quad (2.34)
\]

Such reactions insure the presence of radicals, hence the development of the chain mechanism typical of combustion processes. Furthermore the radical CH$_3$O$_2$H, produced by means of other reactions of the methyl peroxide, could act produce OH and CH$_3$O in accordance with this reaction:

\[
\text{CH}_3\text{O}_2\text{H} \rightarrow \text{CH}_3\text{O} + \text{OH} \quad (2.35)
\]

The oxygenated and the aldehydic compounds can be start dehydrogenation reactions, in fact they have lower activations reaction in comparison with the reaction reported above in the same paragraph. The formation of these compounds strongly contributes to accelerate the combustion process. They can be dehydrogenation reactions or thermal decompositions. The radical CH$_3$O can decompose in presence of a third body or can react with molecular oxygen producing formaldehyde:

\[
\text{CH}_3\text{O} + \text{M} \rightarrow \text{CH}_2\text{O} + \text{H} + \text{M} \quad (2.36)
\]

\[
\text{CH}_3\text{O} + \text{H} \rightarrow \text{CH}_2\text{O} + \text{H}_2 \quad (2.37)
\]

\[
\text{CH}_3\text{O} + \text{O}_2 \rightarrow \text{CH}_2\text{O} + \text{HO}_2 \quad (2.38)
\]

The formaldehyde is a intermediate species in the oxidation kinetic mechanism of hydrocarbons. Hence there have been realized a lot of studies on the kinetic reaction of this species. Its oxidation to the radical HCO can happen mainly through dehydrogenation
reactions in presence of H, O and HO2 radicals but in particular with OH radicals.

\[
\begin{align*}
\text{CH}_2\text{O} + \text{OH} & \rightarrow \text{CHO} + \text{HO}_2 \quad (2.39) \\
\text{CH}_2\text{O} + \text{O} & \rightarrow \text{CHO} + \text{O}_2 \quad (2.40) \\
\text{CH}_2\text{O} + \text{H} & \rightarrow \text{CHO} + \text{H}_2 \quad (2.41)
\end{align*}
\]

The formylic radicals is oxidized to CO, in presence of a third body, trough a thermal decomposition, which is in competition with the oxidation reaction by means of O2:

\[
\begin{align*}
\text{CHO} + \text{M} & \rightarrow \text{CO} + \text{H} + \text{M} \quad (2.41) \\
\text{CHO} + \text{O}_2 & \rightarrow \text{CO} + \text{HO}_2 \quad (2.42)
\end{align*}
\]

The reaction 2.41 is important since it frees a huge amount of H radicals necessary to sustain the branching reaction of the system H\textsubscript{2}/O\textsubscript{2} at high temperature.

All these reactions feed the chain radical mechanism, since the products of any reaction react with the other species in the kinetic mechanism of methane.

Oxidation reactions of carbon monoxide are relatively simple (Westbrook et al, 1984):

\[
\begin{align*}
\text{CO} + \text{O} + \text{M} & \rightarrow \text{CO}_2 + \text{M} \quad (2.43) \\
\text{CO} + \text{O}_2 & \rightarrow \text{CO}_2 + \text{O} \quad (2.43)
\end{align*}
\]

The velocity of these two reactions is relatively low for the temperatures reached during an oxidation process, thus the conversion to CO\textsubscript{2} is low. Anyway the oxidation mechanism interacts with the system H\textsubscript{2}-O\textsubscript{2} in according with this two reactions:

\[
\begin{align*}
\text{CO} + \text{OH} & \rightarrow \text{CO}_2 + \text{H} \quad (2.45) \\
\text{CO} + \text{HO}_2 & \rightarrow \text{CO}_2 + \text{OH} \quad (2.46)
\end{align*}
\]
The reaction 2.46 does not cover an important role, except for very high temperatures and at the beginning of an oxidation process since, in the initial moment of the combustion process the concentration of HO₂ radicals is high in comparison with the concentration of the other radicals (H, O, OH).

The CO oxidation depends on the amount of radical OH. These show a higher tendency to react with methane and the intermediate compounds until the carbon monoxide, than with the monoxide itself. Therefore CO, during the hydrocarbons oxidation, is produced and tends to accumulate, until the methane and the intermediate compounds are consumed. After these compounds depletion it is oxidized to CO₂.

**Pyrolysis of natural gas**

The formation of hydrocarbons from the elements may be written per C atoms:

\[
C + \frac{1}{n} \frac{m}{2} H_2 \rightarrow \frac{1}{n} C_nH_m
\]

The standard free energy of formation of some hydrocarbon is shown in fig. 2.1.
The energies are related to a carbon atom to facilitate the comparison. The Gibbs energies of formation (ΔG°) of each hydrocarbon molecules reflect its relative stability in terms of its element in comparison with another hydrocarbon. At a given temperature, the most stable compounds correspond to the lowest Gibbs energies of formation.

The hydrocarbons are unstable at high temperature and the only product would be C and H₂ if the reaction time were long enough. Methane is particular stable at lower temperature compared to the other hydrocarbons and that the thermal decomposition of methane requires high temperatures. The conversion of methane into ethyne is made possible by the fact that, at high temperatures, the free energy of formation of ethyne is lower than that of methane (and other saturated hydrocarbons). However, ethyne is still unstable relative to carbon and hydrogen.

Equilibrium calculation indicated that the thermal decomposition of methane leads to the formation of ethene, ethyne, benzene and hydrogen as main products provided that the reaction can be stopped before carbon is formed. The yield of these species mainly depends on the temperature.
Figure 2.2  Mole fraction of 14 species in gas-phase equilibrium calculated from thermodynamic data. Total pressure =1bar, H/C=4.

Figure 2.2 shows the mole fraction of 14 species in phase equilibrium calculated from thermodynamic data (Gueret C., 1993). The total pressure is equal to 1 bar and the mixture is characterized by a H/C ratio equal to 4. The figure shows that at the equilibrium ethyne yield is low below 1373K, but it increases strongly with increase temperature. The figure shows also that the yield of ethene is low at all the temperatures. Such equilibrium yield has been calculated to be less than 5% over the whole temperature range (Rokstad et al, 1992). From thermo-dynamical consideration it is, therefore, not likely that high yields of ethene can be obtained from the pyrolysis of methane.

Dilution of methane feed with hydrogen has been found to be especially effective in suppressing carbon formation. Hydrogen dilution has a very strong effect on the equilibrium yield of benzene, in fact the yield decreases with increasing hydrogen dilution. The effect of hydrogen on the equilibrium yield of ethene and ethyne is much less pronounced (Rokstad et al, 1992) (Brown and Parkins, 1991).
The overall reaction in the thermal coupling of methane maybe described as a stepwise dehydrogenation at high temperature:

\[ 2\text{CH}_4 \rightarrow \text{C}_2\text{H}_6 + \text{H}_2 \rightarrow \text{C}_2\text{H}_4 + \text{H}_2 \rightarrow \text{C}_2\text{H}_2 + \text{H}_2 \rightarrow 2\text{C} + \text{H}_2 \]

The formation of products is explained by a free radical mechanism, where the primary reactions are now clearly defined. However, details of the later stages (higher conversion) and the formation of carbon (coke) are not yet fully understood.

The initiation step and the primary formation of ethane and hydrogen are described by the following reactions:

\[ \text{CH}_4 \rightarrow \text{CH}_3 + \text{H} \quad (1) \]
\[ \text{CH}_4 + \text{H} \rightarrow \text{CH}_3 + \text{H}_2 \quad (2) \]
\[ 2\text{CH}_3 \rightarrow \text{C}_2\text{H}_6 \quad (3) \]

Reaction (1) is the rate determining step and the only primary source of free radicals. The unimolecular decomposition leading to methyl radicals has been extensively studied (Stewart P.H. et al., 1989).

The secondary reaction of ethane are described by the following reaction:

\[ \text{C}_2\text{H}_6 + \text{H} \rightarrow \text{C}_2\text{H}_5 + \text{H}_2 \quad (4) \]
\[ \text{C}_2\text{H}_6 + \text{CH}_3 \rightarrow \text{C}_2\text{H}_5 + \text{CH}_4 \quad (5) \]
\[ \text{C}_2\text{H}_5 \rightarrow \text{C}_2\text{H}_4 + \text{H} \quad (6) \]

The formation of ethyne maybe described by the following secondary reactions of ethene:

\[ \text{C}_2\text{H}_4 + \text{H} \rightarrow \text{C}_2\text{H}_3 + \text{H}_2 \quad (7) \]
\[ \text{C}_2\text{H}_4 + \text{CH}_3 \rightarrow \text{C}_2\text{H}_3 + \text{CH}_4 \quad (8) \]
\[ \text{C}_2\text{H}_4 \rightarrow \text{C}_2\text{H}_2 + \text{H} \quad (9) \]

At high temperatures (>1350K), the radical chain reaction sequence above described
is the dominating one for the formation of ethyne both at high and low conversion. At lower temperatures and higher residence time, reaction pathways involving the methylation of ethene should also be considered (Chen C.J. et al, 1976).

Using hydrogen dilution, the reaction involving hydrogen radicals become more important than the reactions involving methyl radicals (Olsvik et al, 1995).

The production of propene can be explained by the following reactions starting from the methylation of ethene:

\[
C_2H_4 + CH_3 \rightarrow n-C_3H_7 \tag{10}
\]

\[
n-C_3H_7 \rightarrow C_3H_6 + H \tag{11}
\]

The main gases produced during pyrolysis of methane are hydrogen, ethane, ethene and ethyne. In addition to propene, as shown above, small amounts of C3H4 (allene and propyne) as well as unsaturated hydrocarbons are formed.

Reaction 13 has been shown to be the most important in the formation of C4 hydrocarbons:

\[
C_2H_3 + C_2H_2 \rightarrow C_4H_5 \tag{12}
\]

Depending on the reaction conditions, benzene may also be a main product. High selectivities of benzene formation are usually accompanied by coke formation.

Different mechanisms have been proposed for the formation of benzene but here they will not be reported since this goes beyond the aim of this paragraph.

Anyway, just to complete the scheme, it seems that the most important reaction for the benzene formation is the following reaction:

\[
C_2H_2 + C_4H_5 \rightarrow C_6H_6 + H \tag{13}
\]

**Effect of temperature and residence time**

Temperatures in excess of 1400K are required in order to obtain practical conversion
of methane to C₂ hydrocarbons. The hydrocarbons are thermodynamically unstable at high temperatures and the only products would be carbon and hydrogen if the reaction time were long enough.

![Graph showing yield of ethyne from pyrolysis of methane under different conditions.](image)

**Figure 2.3** Yield of ethyne from pyrolysis of methane under different conditions. CH₄/H₂=1/1, pressure = 100mmHg; continuous line reactor i.d. = 7 mm, cold finger quench; dashed line reactor i.d. = 10 mm, direct water quench.

Fig 2.3 shows the conversion of methane conversion for a system with a CH₄/H₂ feed ratio equal to 1 and a pressure equal to 100mmHg. In particular the continuous line refers to a flow reactor with a inner diameter equal to 7 mm where the quench of the reaction is realized by means of a cold finger, while the dashed line refers to a reactor with an inner diameter equal to 10 mm where the evolution of the process has been stopped by means of a direct water quench (Holmen et al., 1976). Fig.2.4 shows the corresponding yields of ethyne as a function of the residence time at different temperatures (Holmen et al., 1976).
Figure 2.4  Yield of ethyne from pyrolysis of methane under different conditions. 
\( \text{CH}_4/\text{H}_2=1/1, \text{ pressure } = 100\text{mmHg}; \text{ continuous line reactor i.d.} = 7 \text{ mm, } \text{cold finger quench; dashed line reactor i.d.} = 10 \text{ mm, direct water quench, from Holmen et al.}\)

It is possible to see that the yields in ethyne is more than 85% for temperatures higher than 2000K and reaction time less than \(10^{-2}\) sec as illustrated in fig.5.

At lower temperatures the maximum obtainable yield of ethyne decreases sharply with decreasing temperatures, but the yield of ethene and benzene increases only slightly as shown in fig.2.5. The yields of ethene and benzene show broad and low maxima between 1200°C and 1300°C. The data are relative to a flow reactor with a mixture characterized by a \(\text{CH}_4/\text{H}_2\) feed ratio equal to 2 and at atmospheric pressure (Olsvik et al., 1995).
Figure 2.5  Maximum yield of products obtained from methane pyrolysis as a function of temperature. \( \text{CH}_4/\text{H}_2=2 \), pressure=1 bar, from Olsvik et al.

The conversion of methane at 1400°C is shown in figure 2.6 as function of time.

Figure 2.6  Conversion of methane to products as a function of time at 1400°C. Feed \( \text{H}_2:\text{CH}_4 = 2:1 \).

With increasing residence time ethyne becomes the dominating hydrocarbon product. Benzene starts to from after ethyne but before coke. At higher residence time coke becomes the dominant product.
Effect of hydrogen addition

The influence of hydrogen addiction has been studied in a flow tubular reactor and an inlet temperature equal to 1573K for several hydrogen-methane mixtures (Olsivik et al., 1995). Figure 2.7 reports the methane conversion as function of the residence time on curves parametric in the mixture compositions.

![Figure 2.7: Methane conversion as a function of residence time and hydrogen dilution. Temperature = 1573K](image)

The conversion curves take a S-form and the conversion decreases increasing the hydrogen dilution. As matter of fact, the conversion of methane after 0.1 s was found to decrease from 34% to 16% by increasing the H₂/CH₄ ratio from 1 to 4 at 1300°C. Inhibition by hydrogen may be explained by the reverse of the following reaction:

\[ \text{CH}_4 + \text{H} \rightarrow \text{CH}_3 + \text{H}_2 \]

Hydrogen converts methyl radical into methane, thus decreasing the methane conversion.

The influence of hydrogen addiction on the pyrolysis of methane was analyzed by means of a thermodynamic analysis using the thermodynamic equilibrium of complex
system model (Guéret et al, 1997). Figure 2.8 shows the methane conversion and the yields in acetylene, ethene and benzene as function of the temperatures for mixture characterized by a H/C ratio equal respectively to 4, 6 and 8 at a pressure of 1 atm.

It was observed that the increase in the H/C ratio (greater dilution by hydrogen) caused a decrease in methane decomposition at a given temperature. By contrast it was favored the formation of ethylene and acetylene and decreased the formation of benzene.

Furthermore hydrogen dilution decreases the selectivity of benzene and increases the selectivities for C\textsubscript{2} compounds. The effect of hydrogen depends on the temperature and hydrogen dilution and it becomes more important at high working temperatures. Since hydrogen strongly depresses carbon formation, dilution with hydrogen increases the yield of ethyne.
Effect of pressure

The influence of pressure on the pyrolysis of methane was analyzed by means of a thermodynamic analysis using the thermodynamic equilibrium of complex system model (Guéret et al, 1997).

Figure 2.9 Molar fraction of CH₄ (a), C₂H₄ (b), C₂H₂ (c), and C₂H₆ (d) at thermodynamic equilibrium for different pressure for a system H/C=4.

The analyzed pressure were 0.1, 1 and 10 atm for a system characterized by a C/H ratio equal to 4. Figure 2.9 reports the molar fraction of CH₄ (a), C₂H₄ (b), C₂H₂ (c), and C₂H₆ (d) as function of temperature for the different pressures.

It may be observed that increasing the pressure does not change the general shape of the diagrams, but it causes a shift in the equilibrium curves towards higher temperatures. Increasing the pressure also decreases the decomposition of methane, as well as the formation of low-hydrogen compounds (C₂H₂, C₂H₆). The case of benzene is slightly more complex in so far as the pressure effect is not uniform, but is reversed at around 1200°C.
On the contrary, a pressure increase favors the formation of ethene. This appears to indicate that the splitting of the C-C and the C-H bonds is more difficult at high pressure.

**Effect of the nature of the diluent**

In literature there are few works on the effect on the nature of the diluent on the evolution of the oxidation process of hydrocarbons in Mild conditions.

The most of works present in literatures concerns studies, principally numerical, on a class of pollutants called NO\(_x\) (Jeong Park et al, 2004, Dong-Jin et al., 2004, Seung-Gonet al. 2002). In particular in these works they have studied the thermal and chemical contribution of added H\(_2\)O or CO\(_2\) on flame structures and NO emission in hydrogen or methane counter-flow flames.

These numerical works on H\(_2\)/N\(_2\) flames showed that the CO\(_2\) addiction leads to a reduction of the temperature, because of the higher carbon dioxide heat capacity respect to nitrogen, and also because the CO\(_2\) break-down produces relatively populous hydrocarbons that inhibits chain branching reactions. As matter of fact in literature it is known that the rate of such reactions, in particular the reaction H + O\(_2\) \rightarrow O + OH, is considerably less than those between the radical (H, OH, O) and hydrocarbons.

In particular it has been shown that the breakdown of added CO\(_2\) was more vigorous than the conversion of CO to CO\(_2\). Furthermore it was observed that the path CH\(_2\)O\(_3\)_CH\(_3\)OH_CH represents the main pathway after the carbon dioxide breakdown. Moreover the C\(_2\)- branch reactions are negligible.

The addiction of water induces a decrease of the temperature, if just the thermal effect is considered, but it induces an increase of the temperature because of its chemical effect. In fact the breakdown of water contributes to the formation of chain carrier radicals, and branching reaction can be augmented considerably.
Recent researches (Kim et. Al, 2002; Park et al., 2002) have shown that the mole fraction of H and O radicals decreases, but that of OH, appositively, increases due to chemical effect of added water. Then the important features of overall reaction rate must be, essentially, dependent upon the behavior of the key reaction such as principal chain branching; \( H + O_2 = OH + H \), and principal recombination reaction, \( H + O_2 + M = HO_2 + M \).

In particular Park et al. (2004) performed a numerical study on a system composed by hydrogen and air in mild conditions in a counter-flow configuration. Steam water was added to the system both from the oxider and fuel side. Results showed that steam addiction to the system \( H_2/Air \) system results in a temperature increase. This is due to a remarkable mole production of OH radicals via the reaction step here reported:

\[
O + H_2O \rightarrow OH + OH.
\]

Hwang et al. (2004) realized a numerical analysis on flame structure and NO formation in \( CH_4/O_2/N_2 \) counter-flow flame diluted in \( H_2O \). They confirmed the role of reaction reported above.

Rasmussen et al. (2004) have carried out an experimental study on the formation of polycyclic aromatic hydrocarbons and soot in fuel-rich oxidation of methane in a laminar flow reactor. Their results were then compared with numerical simulations. They studied also the effect of water on the oxidation of methane focusing their attention on soot formation. They hypothesized that water can affect soot formation by means of a thermal effect and a chemical effect. The thermal effect is due to the large heat capacity of water vapor, which reduces the flame temperature. The chemical effect was attributed to changes in radical pool by the presence of water vapor. In fact it enhances formation of hydroxyl radicals through the reaction

\[
H + H_2O \rightarrow OH + H_2
\]
They analyzed the oxidation process in term of methane conversion and species production as function of water amount. The influence of water addiction was studied for a premixed mixture composed by CH₄, O₂ (1%, 0.6%) diluted in N₂ and an inlet temperature equal to 1673K. Nitrogen was substituted by steam in several concentrations from 0 up to 10%.

They found out that the concentration of CO increases with increasing water vapor concentration up to 1%. Above this value, CO decreases with increasing water level. The CO₂ concentration increases steadily increasing steam percentage. Furthermore the concentration of methane in outlet from the laminar flow reactor increased as function of the concentration of steam. Contrary to this trend, they observed that C₂H₂ and C₆H₆ decreased with increasing water amount, and that for steam percentage higher than 6% benzene was not detected at all. The concentrations of C₃H₄ and C₂H₆ do not significantly change with water addiction.

They performed further experimental test on the same system changing both the temperature (from 1050K to 1850K) and the H₂O concentration. The results confirmed the tendency of water in reducing CO, C₂H₂ and C₆H₆ concentration while enhancing considerably CO₂ concentration. The methane conversion slightly increases as steam concentration increases.

Numerical simulations confirmed the trend of species concentrations found out experimentally.

Therefore they performed a reaction flow analysis in order to understand the reactions responsible of such concentrations trend. The numerical simulations suggested that the influence of water vapor on acetylene conversion is a result of an increased hydroxyl formation from water vapor between 1500K and 1850K. Hydroxyl radicals forms mainly by the reaction \( H + H₂O \rightarrow OH + H₂ \) and subsequently acetylene can by oxidized
through these two reactions.

\[ \text{C}_2\text{H}_2 + \text{OH} \rightarrow \text{HCOH} + \text{H} \]

\[ \text{C}_2\text{H}_2 + \text{OH} \rightarrow \text{CH}_2\text{CO} + \text{H} \]

Both reactions produce H radicals, which may contribute to further enhancement OH radicals. The enhancement

Meanwhile the increase of OH radicals is responsible of CO\(_2\) concentration increase and CO concentration decrease on the basis of this reaction:

\[ \text{CO} + \text{OH} \rightarrow \text{CO}_2 + \text{H} \]

They explained also the increase of methane concentration in presence of steam water in according with this scheme:

\[ \text{CH}_2\text{CO} + \text{H} \rightarrow \text{CH}_3 + \text{CO} \]

\[ \text{CH}_3 + \text{H} + \text{M} \rightarrow \text{CH}_4 + \text{M} \]

\[ \text{CH}_2\text{O} + \text{CH}_3 \rightarrow \text{CH}_4 + \text{HCO} \]

Therefore they found out that water vapor addiction limits soot formation due to a chemical influence. It affects the oxidation chemistry of acetylene and reduces or even eliminates formation of soot above 1500K. They believe that formation of OH radicals from water vapor accounts for these changes in acetylene chemistry.
Chapter III

Methodologies for the Study of Mild Combustion Processes

Introduction

The thesis concerns the study of the behavior of model reactors in working conditions typical of a Mild Combustion process. This new combustion “mode” forecasts the use of a high dilution degrees and high inlet temperatures. These operative conditions allow for a reducing of pollutants formation, such as NOx and soot, and save energy. Hence this is a very promising process in the framework of the development of new combustion technologies aimed to enhance the efficiency and reduce the environmental impact of combustion systems.

Although in literature there are many works on this new combustion “mode”, there is still the necessity to characterize the process by means of basic studies. This lack depends on the difficulty to realize in laboratory scales plants able to work with high inlet temperatures typical of Mild Condition. These extreme conditions imply a difficult choice of materials and problems of sealing. These problems can be more easily overcome in pilot or industrial plant.

Basic studies are usually carried out on model reactors typical of chemical engineering. The strength of this approach is the opportunity to highlight particular features of combustion process using different elementary configurations. In fact the combustion process is characterized by very short characteristic time, i.e. for instance reaction time, and by the interaction between fluid-dynamic and chemistry. Model reactions allow simplifying the study of oxidation reactions since they permit to emphasize particular aspects of the process. Furthermore their complementary allow for a global and
structured characterization of combustion process. These features justify their wide spread use in the research field.

Moreover the behavior of model reactors has been widely modeled since the equations, such as mass or energy conservation, necessary to describe such systems, in ideal conditions, are function of a parameter such as the time or a spatial coordinate. In fact in literature they are also known as zero- or one-dimensional reactors. This aspect has promoted the development of numerous numerical codes able to simulate the behavior of ideal reactors and the development of a modeling activity of the oxidation process.

Hence they allow for a good comprehension of physical and chemical phenomenology and meanwhile for a validation and tuning of predictive models supported by experimental data obtained in precise operative conditions.

In this research group in the past contributions on the study of Mild combustion processes have been realized on different configurations, in particular numerical works on batch reactor, opposed flame configuration and perfect flow stirred reactor (A. Matarazzo et al., 2005, P. Sabia et al., 2005a; Sabia et al., 2005b). In this thesis the attention has been focused on the continuous stirred reactor (CSTR) on and the plug flow configuration because they allow for an accurate and structured analysis of the kinetic and the dynamic evolution of the combustion process.

The continuous stirred reactor (CSTR) is used to study the temporal evolution of the oxidation process and to assess the combustion regimes that can establish as function of several parameters such as pressure, composition of mixtures and temperature. In fact the CSTR offers the possibility to locate exactly in the plane of operative parameters the conditions for which the analyzed system evolves trough different regimes. The plug flow reactor is used to study the evolution of the oxidation process as function of a spatial coordinate. Hence, it represents a good configuration for the assessment of kinetic
characteristic times, such as the reaction time. Furthermore it gives the advantage to change the resolution of the oxidation phenomenon just by acting on the residence time.

Indeed both reactors consent to study the evolution of the oxidation process as a succession of steady states as function of an unique parameter, which is in the case of the CSTR, the time and, in the case of the plug flow reactor the axial coordinate, or equivalently the time.

Furthermore both the configurations are suitable to study the oxidation process in Mild operative conditions. In fact the uniformity of temperature and concentration profiles typical of Mild combustion process allow to schematize, in first approximation, the process by means of a perfect stirred reactor.

As discussed in Chapter I a Mild combustion process may be more exactly schematized by means of a series of CSTR. In literature it is renown that a series of CSTR is equivalent to a plug flow reactor, whether the number of CSTR in series tends to infinite. Each reactor of the series represents a differential state of the plug flow reactor. Since the operative conditions of the process in Mild conditions imply high dilution degree, the characteristic time of the oxidation reaction, in other terms the differential states, hence it is not necessary an infinite number of reactors. Therefore the assumption to schematize an infinite series of reactor with a plug flow reactor assumes a higher validity.

The choice of the CSTR implies some problems linked to the necessity of realizing a perfect mixing of reactants. The mixing of reactants is not separable from the process itself. Hence if the perfect mixing is not achieved all the oxidation process is affected. It represents a meaningful limit for the employment of this reactor in fact it allows to study chemical processes that have characteristic reaction time longer than the mixing time. Furthermore in this configuration it is not possible to observe the evolution of the oxidation process of the fresh mixture, since reactants are fed in a environment already “polluted” by
radical species and products of the combustion process that inevitably conditionate the chemestry of the system. CSTRs are commonly used for testing and developing chemical reaction mechanisms, in fact they allows more precisely the study of networks of reactions.

These inconvenients are overcome in plug flow reactors. The problem of mixing reactants is bordered in the first part of the system where an appropriate geometry has to be chosen in order to mix reactants and minimize the mixing time.

Other model reactor would be suitable for the study of Mild Combustion. In order to analyze the process in terms of diffusivity and spatial evolution of the oxidation process another interesting tool could be the counter-flow configuration. But this reactor has not be taken in consideration in this thesis since it represents a more difficult way to analyze the process, since the fluid-dynamic and the kinetic evolution of the oxidation interact. In the future this configuration will be considered but it is more convenient to start the exploitation of the new working conditions with the simplest possible configurations, hence the CSTR and the plug flow reactors.

In this chapter all the tools used to perform the study of these new operative conditions have been presented. In particular, in the first part of this chapter, the experimental facilities, the diagnostic instruments and the analyses procedures have been described. In the other part, the software employed to perform numerically the study are presented and discussed in their general aspects.

**Experimental set-up and measurements methodologies**

The first experimental plant that will be presented is the one relative to continuous stirred reactor. The experimental set-up is shown in figure 3.1.

The reactor represents the core of the plant. Its characteristic will be presented in the next section. It is located inside an oven composed by ceramic fiber semi-cylindrical brick.
Figure 3.1 Sketch of the plant

Gases are fed inside the reactor trough lines and their flow rates are set and monitored by means flow meter-controllers positioned along the feed lines and interfaced with a computer. Nitrogen and the hydrocarbons are stored in pressurized reservoirs up to 200bar, while air comes from an alternative compressor (Atlas-Copco model 1230) at 8bar. All the lines are provided with valves that reduce the pressure down to 3bar. The air compressor line is also provided of a filter.

Furthermore the plant has been modified in order to allow experiments on Mild combustion condition in systems diluted in steam water. Hence the plant is provided with a system composed by a distilled water tank, a peristaltic pump and an oven, again composed by two ceramic fiber semi-cylindrical bricks. Air and water mix and than they pass trough a spiral coil located inside the oven, where the water is vaporized and the flow is then heated up to 450°C.
The plant is provided with thermocouples K and R that allow for the monitoring and measurements of temperatures in several sections of the plant.

Furthermore, in the outlet section, it is present a line that allows for the sampling of the exhaust gases.

**Continuous Flow Stirred Reactor and Facilities**

The CSTR is a continuous flow reactor with a perfect mixing of reactants. In this configuration the temperatures and the species concentration are equal in any point of the reactor and the outlet flow has the same intensive characteristics. The CSTR configuration can be used to study the evolution of a chemical reaction as a succession of steady states reached in the system. By this way it is possible to observe the different evolution states of the oxidation process on a temporal scale and to change the evolution of the process by acting on the residence time. Furthermore the uniformity of temperature and concentrations allows splitting physical factors from the chemicals ones, to avoid propagation of the reactions and to realize species sampling in controlled conditions.

Another advantage is the possibility to identify in the plane of operative parameters the condition for which different regimes establish. At the same time the perfect mixing represents a practical limit for the employment of this reactor. This means that such reactors allow for the study of chemical processes that have characteristic times higher than the mixing time.

In literature there are different typologies of continuous stirred reactors, they differ for the system used to make homogeneous the reacting volume. In particular, it is possible to mix reactants by means of a mechanical stirring or by means of a proper fluid-dynamic configuration.

In mechanically stirred reactors, there are problems relative to the motion
transmission of the stirrer, to the presence of mechanical parts in motion, and at last but not least sealing problems. Working pressures higher than the atmospheric and high temperatures make more difficult the solutions of these problems.

Nevertheless they are overcome in the second reactor typology, commonly known as Jet Stirred Flow Reactors (JSFRs). Mixing is realized by means of a proper choice and design of nozzles that feed reactants inside the reactor. The JSFRs have some disadvantages respect to the first category of reactors. In fact for a fixed diameter of the nozzles there is a limited range of residence times that satisfies the condition of perfect mixing.

In this thesis the JSFR reactor has been preferred because of the very high inlet temperatures typical of Mild processes. The reactor used in our experimental tests was already present in a laboratory of this institute.

The study has been carried out in spherical Jet Stirred Flow Reactor with volume of about 0.1 dm$^3$. The choice of the material is not a trivial since it should have low conductibility and low thermal expansion coefficient, and should be inert and resistant in oxidant environment. Quartz responds to these requirements and allows working with high temperatures up to 1500K. Figure 3.2 shows a picture of the reactor and of the geometry of the mixing device. Oxygen/nitrogen mixture and methane were separately fed into the reactor through the lines 2 and 3 respectively. They mix in the pre-mixing section (5) where the fluid-dynamic conditions inhibit the occurrence of any chemical reaction. The mixture is then introduced in the reactor by means of four jet nozzles (6), outlined in the sketch reproduced in the Figure 3.2. Each jet is differently oriented, as shown by the arrows, so that the direction and velocity of gas flow at the jet outlets assure well-mixed conditions in a relatively wide range of residence times (Matras, Villemaux, 1973; David, Houzelot, Villemaux, 1979). The exhaust gases flow through the line 4 before to be
discharged.

1. Thermocouple duct
2. Oxygen/Nitrogen inlet
3. Fuel inlet
4. Exhaust outlet
5. Reactant premixing section
6. Four jet nozzle

Figure 3.2: Sketch of the Jet Stirred Flow Reactor.

The JSFR presents four nozzles arranged in such a way to form a cross. They are located in planes diametrically opposed and each plane has two nozzles oriented in opposed orthogonal direction. This devise is located in the center of the reactor.

The well-mixing of the reactor was verified in the past by means of a pulse tracer experiment following a procedure described by Levenspiel (1999). Therefore, using methane as tracer in a nitrogen flow, the obtained Residence Time Distribution (RTD) function E was analyzed by means of the “Tanks-in-series” model. The results suggested that jet reactor behaves as a well-mixed reactor for residence time lower than 0.6 sec.

The residence time used in our experiments was thus fixed to 0.5 sec.

The well mixing of the reactor was verified also by means of two-dimensional visualization system. In fact during the experimental tests a significant temperature oscillation phenomenology was detected and in correspondence of this phenomenology luminous emissions were identified. In order to collect the spontaneous light emitted from the reacting volume an intensified CCD camera, sensible in a wide spectral range, was
An example of images collected during oscillations obtained for an inlet temperature of 1125 K and a C/O ratio of 0.3 were reported in Figure 4.3.

Figure 3.3.a represents an image of reactor detected in correspondence of the minimum temperature acquired during the oscillation of 1135 K, i.e. 10 degrees higher than $T_{inlet}$. It shows that in this condition no luminous signal can be detected in the wavelength range here considered.

The reactor image detected in correspondence of the maximum oscillation temperature of 1458 K was reported in Figure 3.3b. It shows that the luminous signal can be detected from the whole reactor volume and it is uniformly distributed. The same results were obtained in the most of the experimental conditions here considered thus testifying that the system works in well-mixed conditions.

![Figure 3.3. Jet stirred reactor images at C/O=0.3 and a dilution level of 90%.](image)

**Oven**

The reactor was located inside a cylindrical electrically heated, ceramic fiber wall oven. Two semi-cylindrical ceramic fiber wall bricks with a power equal to 1100K compose it. The oven can reach a maximum temperature of 1300 K and it is equipped with a temperature controller. The two heating fiber bricks are disposed in series and the
potential difference is regulated by means a transformer.

The power of the system assures an adequate thermal flux to keep constant the temperature in the oven and to reach the wanted temperature in a reasonable time.

A recirculation air system provides for a homogeneous temperature distribution in the oven.

**Flow Meter-Controllers**

Flow rates are set up and controlled by means of BRONKHORST HIGH-TEC instruments. A flow rate meter-controller, properly calibrated in dependence of the gas that passes into the line, is located on each line of the plant. They have been interfaced with a PC and managed by means of a program realized by means of the software LABVIEW.

The nitrogen and methane controllers can handle flow rates up to 10 lt/min, while the methane one up to 4 lt/min. Plant has been provided with by-pass lines to use in case of breakdown of flow meters-controllers.

**Acquisition data instruments**

The reactor temperature measurements and monitoring have been realized by means of a homemade thermocouple Pt-Pt/13%Rh (type R), with a diameter equal to 25 μm that allows for a respond time of about tens of milliseconds.

The temperature has been acquired on a multi-channel recorder LR 4120E YOKOGAWA and on a PC with a frequency equal to 50Hz.

**Experiment procedure**

The start up procedure of reactor consists in feeding the different species in sequence up to reach the desired mixture composition. Therefore, nitrogen is firstly fed to the reactor in order to flush the volume by the residues of the previous test. Then, the nitrogen flow rate is set at a value equal to the overall flow rate chosen for the experimental test. In this condition, the temperature measured by thermocouple in the reactor is assumed as T_{inlet}.
Hence, the nitrogen flow rate is set to the value chosen for the experimental test and at the same time, fuel or oxygen is fed to the reactor at the corresponding flow rate. Finally, the last reactant is added at a rate proper to reach the desired C/O ratio. The goal of this work is to perform an extensive study on the phenomenology occurring during methane oxidation in a well-stirred reactor. Therefore, the experimental analysis aims also to verify the existence of multiple steady states corresponding to the same inlet conditions. This behavior is well known in literature and it is referred as hysteresis. In particular, during the experimental tests it was found that, in a well-identified range of temperature and C/O ratio, the sequence used in adding the reactants, i.e. fuel at first and then oxygen or vice-versa, leads to different reactor temperatures. In particular, if the methane is fed before the oxygen, the system reaches a working temperature higher than the temperature obtained in the other case. Due to this evidence, both of start-up procedures were performed for each initial condition.

Heat transfer coefficient

A very important parameter for the definition of the system is the global heat transfer coefficient U. In JSFR reactors the parameter U, as explained in a previous paragraph, depends on the fluid-dynamic conditions imposed by the flow rates of gases injected in the reactor, hence on the global flow rate. It depends also on the oven and reactors temperatures, and on the mixing in the oven that hosts the reactor.

The need of calculating the value for the coefficient U, in the operative conditions chosen in the experimental tests, has come out in particular when the numerical simulations, realized to model the behavior of the system, have required the assessment of the reactor parameter.

For the particular geometry of the reactor and for the difficulty of stating the real working parameter in the oven, there have not been found correlations among the
parameters in literature that would have helped to calculate the heat transfer coefficients and hence U.

Nevertheless the assessment of the global coefficient has been realized by means of these equations:

\[
Q_{\text{loss}} = U*A*(T_o - T) \quad (3.1)
\]

\[
Q_{\text{loss}} = W*cp*(T - T_i) \quad (3.2)
\]

where \(Q_{\text{loss}}\) is the heat loss by the reactor, \(A\) is the reactor surface, \(T_o\) the oven temperature and \(T\) the reactor temperature, \(W\) is the flow rate of the fed gas, \(cp\) the heat calorific power and \(T_i\) the inlet reactor temperature, finally \(T\) the output gas temperature. In this configuration the inner reactor and the output temperatures are the same.

Any parameter in the equations 3.1 and 3.2 is known since temperatures can be measured by means of thermocouples present in the system, the reactor surface and the gas physical properties are easily calculated. Equalizing the two equations it is possible to assess the parameter \(U\).

The test has been realized in this way: nitrogen is fed into the reactor with a flow rate corresponding to a residence time of 0.5 sec for a fixed reactor temperature. The oven temperature has been set to the right value that allows the reactor temperature to reach the wanted value. The calculations have been realized for different reactor temperatures in the range of interest.

The mean value of the coefficient \(U\) is about \(2*10^{-3}\) cal/cm\(^2\) K sec.

**Tubular Flow Reactor**

The other configuration chosen for the study of Mild Combustion processes, as explained in a first section of this chapter, is the tubular flow reactor.

At the moment the major priority is the designing and the realization of this
configuration since, once this target will be reached, the tubular flow reactor has high potentiality of applications. They can be identified in two main categories:

1) The water diluted oxidation of light hydrocarbons and mixture of hydrocarbons and hydrogen in very diluted conditions.

2) The use of hydrogen in order to purify a waste gas.

The first point is related to the study of the Mild Combustion as clean technology. The other point aims to understand the potentiality of Mild application as cleaning process.

**Description of the plant**

The plant is shown in figure 3.4. The plant is divided into three different zones. In the left side fuels, comburents and diluents are shown. Light hydrocarbons such as methane are stored in cylinders. Hydrogen is produced by a H₂-O₂ Generator. Distilled water is fed to the instrument that provides to produce H₂ and O₂ in the stoichiometric ratio 2:1 by an electrolytic process. The flow rate can be monitored by setting the wanted value on a control device that regulates the electric power. There are several flow meters to control the flow of each fuel. Fuels run first into a mixer that provides to achieve a good mix degree, and then fuels are injected into the reactor. The oxiders used are air and pure oxygen. The former comes from a alternative compressor, the latter from a cylinder. This additional oxygen is used to supply the oxygen produced by the H₂-O₂ Generator when lean mix are desired. At the same time, if rich conditions are required, a part of the produced oxygen can be discharged into a hood (hood1). Oxygen and air are then mixed with diluents. These are H₂O, N₂ and CO₂. Water vapor is generated from a Vapor Generator at 5 bar and 150°C. After the mixing, two heaters provide to enhance the temperature until the desired value. The first heater has a high power and can reach 1300K. The high temperature iron chrome-aluminum (ICA) heating elements wires furnish the
required power. The second one is provided with molybdenum or CSi resistances that can easily work at higher temperature until 1800K. Both the heaters have temperature control devices. After reaching the wanted inlet condition the main stream is fed inside the plug flow reactor that is well isolated with ceramic panels. Fuel is fed as well, and the oxidation process takes place.

![Diagram of experimental plant](image)

**Figure 3.4** Experimental plant.

At the center the Plug Flow Reactor is showed. A description of the reactor is presented in the following paragraphs. On the right of the scheme there is the equipment for carrying on analyses. The plant offers different possibilities: it is possible to analyze a sample, or to condense all the flow first by means of a heat exchange in controcurrent with water at environment temperature, later by a ice trap. In both the situations gases and liquids are dispatched to measurement instruments. The third possibility is just cooling all the flow by a water flow in a cooling tower. Since it is possible to have some oxygenate
compounds in the output flow it is diluted with air and then discharged into a hood. Two valves on the output line from the reactor provide to dispatch the output flow to the right direction in accordance with the wanted analysis.

**Reactor configuration choice**

The core of the plant is the reactor because it yields a realistic simple process respect to mild processes in more fluid-dynamic pattern. In fact a plug flow reactor has been chosen for our experiments. In an ideal configuration and in a full turbulent regime each small control volume has the same velocity but the ones very close to lateral walls for the adherence boundary condition. Each volume has the same residence time and it can be described just as small batch reactors with no interaction. No radial differences in concentration and/or temperature are allowed and the configuration can be fully described by means of just a parameter: a spatial coordinates which usually is the axial coordinate. Therefore the advantage of using such a configuration for our aims is to describe combustion processes as a function of a length and have a resolution of the oxidation adaptable to our requirements just by changing the residence time. For example if there is a deflagration process in a PFR the flame front can be spanned on a certain length of the reactor increasing the velocity of inlet gas. In this way the flame front can be ideally split into different stages and analyzed by means of suitable techniques as function of the axial coordinate.

This is allowable for an ideal configuration but in the practice there are several problems due to mix different gas, to have a flat profile, which means a turbulent regime is fully developed, and to neglect the axial and radial dispersion effects.

The problem of mixing reactants is bordered in this PFR configuration in the first part of the system where an appropriate geometry has to be chosen in order to inject fuels and minimize the mixing time. It is a quite delicate problem since the mixing time is to be
compared with the autoignition and reaction time. The other possible ideal configuration is a perfect stirred reactor (CSTR) in which there are no spatial gradients in concentrations of species and temperature and the inside concentrations and temperature are equal to the output ones. The way to describe the process is by means of another parameter: the time. In this configuration the mixing of reactants is not separable from the process itself. Hence if the perfect mixing is not achieved all the process is affected. The PFR configuration offers the advantage to separate the mixing from the process and the possibility to act on it.

**Reactor design**

The reactor design is very important to have a reactor configuration which allows for a good study of oxidation process. As it has been underlined above, a flat velocity and temperature profile and a high-resolution time are desired. The former request allows to describe the phenomenology occurring in the reactor as function of the axial coordinate or time, the latter one allows to spread all the process on a wider axial length and so provides a thorough study of the stages of the process itself. Figure 3.5 shows conditions and the logical steps used to design the reactor. To have a flat profile a turbulent regime must be realized. This constraint suggests the Reynolds number should be higher than 3000. Reynolds number is equal to $\rho vD/\mu$ where $\rho$ and $\mu$ are the gas density and the viscosity. Both of them are function of temperature. The density and viscosity decreases and increase respectively as the system temperature increases.

It means the higher the temperature is, the smaller the Reynolds number is. This suggests Reynolds number should be assessed for a good design at the highest temperature where more severe working conditions occur. In order to have a quite small reactor for lab space requirements, the axial dimension has been fixed to 1 meter. In the meantime since a high resolution time is required, the residence time has been fixed equal to 0.01 seconds.
Figure 3.5  Conditions and logical steps for the PFR reactor design.

The inlet velocity has been chosen as well, it is equal to 100 m/s. This value takes into account the velocity should be lower than 0.3 Mach in order to avoid undesired compressibility effects (http://iris.ingfo.unibo.it, 2003). These could affect the resolution of the oxidation process since the axial coordinate and time would lose their biunivocity. The sonic velocity through a certain gas is expressed by this formula $v_s = \left(\frac{\gamma RT}{M}\right)^{1/2}$ where \(\gamma\) is the \(\frac{C_p}{C_v}\) ratio, \(R\) the universal gas constant, \(T\) the temperature in Kelvin and \(M\) the species molecular weight. For polyatomic molecules \(C_p = 4R\) and \(C_v\) comes from Mayer equation (\(C_p = C_v + R\)). Hence, from easy calculations, at \(100^\circ\text{C}\) the sonic velocity in vapor water is 475 m/s. Therefore the condition to avoid undesired effect is satisfied. For our working condition the temperature is higher but also the sonic velocity is higher in accordance with the sonic velocity formula.

Moreover there is another condition to consider. Since the reactor has to be quite small and has a limited power for safe requirements, the power of the reactor should be more or less equal to 1KW.

These requirements lead to assess the diameter of the cylindrical duct following a logical procedure described in the lower part of fig 3.6. At the highest working temperature
a value of the diameter $D$ is hypothesized. Hence it is possible to calculate the flow rate $Q$ and the Reynolds number $Re$. Once the flow rate is known also the power $P$ can be easily assessed. If the diameter $D$ satisfies both the conditions ($Re$ and $P$) the diameter value has been found otherwise the logical steps have to be followed again.

Obviously the power $P$ might be assessed for the lowest temperature in which experiments have to be realized since the mass flow rate, and hence the reactor power, increases if the temperature decreases. But it is not a stringent condition since, as shown on the table 1, the power is anyway low and close to 1 KW.

The experiments in mild conditions will range from 1000K to 1800K. In order to assess the higher working temperature the ChemKin Plug Application in adiabatic condition has been used. The table 3.1 shows working temperatures, flow rates, Reynolds number and plant power values for a system composed by $H_2$ and $O_2$ in stoichiometric condition and $H_2O$ as diluent for different inlet temperatures. The dilution degree is 90%. The temperature at which the logical steps have been followed is 2100K (this is the working temperature for a inlet temperature equal to 1800K), and the found diameter $D$ is 1 cm. This mixture has been chosen to run these calculations since the hydrogen has the highest heating value among fuels thus this system will work in more severe conditions. In particular, Reynolds numbers have been assessed for a wide range of inlet temperatures at which experiments will be run. One can see as Reynolds is a function of temperature and it decreases as $T$ increases. For 2100K Reynolds number is quite satisfying in fact it is 3600 if an increase of velocity, due to the temperature enhancement for the oxidation reaction, is taken into account.

In order to verify the goodness of the operative conditions the parameters such as the Peclet number and the Graetz number have been assessed. In particular the first a-dimensional number takes into account the axial dispersion which characterizes the retro-
mixing effect due to the turbulence in the system. In fact there could be retro-mixing effect due to different velocities in the cross section of a duct or for the molecular and turbulent diffusion. It is obvious that the higher is this effect, the farther the system is from the ideal condition of a plug flow.

<table>
<thead>
<tr>
<th>( T_{\text{inlet}} ) (K)</th>
<th>( Q_{\text{tot}} ) (Nm/min)</th>
<th>( Q_{H_2O} ) (Nm/min)</th>
<th>( Q_{H_2} ) (Nm/min)</th>
<th>( Q_{O_2} ) (Nm/min)</th>
<th>( Re )</th>
<th>( T_{\text{final}} )</th>
<th>( \text{Plant power} ) (KW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1000</td>
<td>128.58</td>
<td>115.72</td>
<td>8.57</td>
<td>4.29</td>
<td>10093.8</td>
<td>1357</td>
<td>1.84</td>
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<tr>
<td>1100</td>
<td>116.89</td>
<td>105.20</td>
<td>7.79</td>
<td>3.90</td>
<td>7952.7</td>
<td>1465</td>
<td>1.67</td>
</tr>
<tr>
<td>1200</td>
<td>107.15</td>
<td>96.44</td>
<td>7.14</td>
<td>3.57</td>
<td>6834.3</td>
<td>1557</td>
<td>1.53</td>
</tr>
<tr>
<td>1300</td>
<td>98.91</td>
<td>89.02</td>
<td>6.59</td>
<td>3.30</td>
<td>5801.0</td>
<td>1649</td>
<td>1.41</td>
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<td>82.66</td>
<td>6.12</td>
<td>3.06</td>
<td>5149.9</td>
<td>1741</td>
<td>1.31</td>
</tr>
<tr>
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<td>77.15</td>
<td>5.71</td>
<td>2.86</td>
<td>4604.2</td>
<td>1833</td>
<td>1.22</td>
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<tr>
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<td>3313.6</td>
<td>2086</td>
<td>1.02</td>
</tr>
</tbody>
</table>

*Tab.3.1* Final (numerical) temperatures, plant power, flow rate (Nm/min) and Reynolds number values for different inlet temperatures for a stoichiometric \( H_2-O_2 \) mixture diluted with water at 90%.

The Peclet number is equal to \( D/uL \) where \( D \) is the axial dispersion coefficient, \( u \) is the mean velocity and \( L \) the length of the duct.

In particular if:

\( D/uL \rightarrow 0 \) dispersion is negligible, hence plug flow condition.

\( D/uL \rightarrow 0 \) dispersion is high, hence the reactor is far from the ideal condition.

In literature (Octave Levenspiel, 1999) there are several diagrams for the calculation
of this number.

In turbulent conditions \( D/\nu_d \) ranges from 0.2 to 0.5. Hence the Peclet number is equal to \( 2\times10^{-3} \) or \( 5\times10^{-3} \). In order to avoid undesired retro-mixing effect Pe should be less than 0.01. So even in the worst condition the system is not so far from an ideal plug flow reactor.

Anyway once the system will be ready, following a procedure well known for the characterization of plug flow reactor (Levenspiel, 1998), a pulse tracer experiment will be realized in order to assess the function of the distribution of residence time (RTD) that can assess the entity of dispersion effect in our configuration.

The other dimensionless number is the Graetz number (Gr). It gives the ratio between the axial heat transport for convection and the radial heat transfer for conduction. The Graetz number is equal to \( uDcpL/KD \) or \( (Re)(Pr) D/L \) where \( \rho \) is the density of the mass flow, \( u \) the velocity, \( cp \) the heat capacity, and \( K \) the thermal conducibility, \( L \) is the length of the pipe and \( D \) the diameter. It has been valued at \( T=1000K \), \( T=1400K \) and \( T=1800K \) for a system composed just by vapor water. Graetz is respectively equal to \( 1.194\times10^{-2} \), \( 4\times10^{-2} \) and \( 9.1\times10^{-2} \). As it can be seen for all these temperatures the convective term is higher than the conductive one. It means that if there are temperature and velocity gradients along the radius of the pipe the system will not be able to make the profile flat and it insures that the small batch volumes in which the flow can be subdivided will not affect each other. It is an ideal condition since in this way any batch reactor in which the system can be split will preserve independently its vicissitude.

At the same time it is possible to assess also the ratio between the axial convective mass transfer and the radial diffusive mass transfer. In this case the value is given by \( vR/D \) where \( D \) is the diffusivity of a species in vapor water. If there is methane in the vapor water flow, the diffusivity of methane in vapor steam is of the order of magnitude of \( 10^{-3} \).
m²/s at the working temperatures characteristic of Mild Conditions, and hence Graetz will be about 25. It means that if there is a radial gradient in concentration the thermal diffusivity will not affect the concentration profile since the diffusivity term is too small.

Hence even if there are concentrations or temperature or velocity gradients along the radius of the duct any volumes of the system will be independent from the other volumes.

**Velocity profiles**

The first requirement for a plug flow reactor is that the velocity profile has to be flat. In order to verify this condition several calculations have been done.

Turbulent flows are chaotic and are characterized by rapid, apparently random fluctuation in the flow variables. These fluctuations mix transported quantities such as momentum, energy, and species concentration, and cause the transported quantities to fluctuate as well.

Hence it is very difficult to study a field motion in turbulent condition. The most fruitful approach is to recognize that in many application only in average quantities are interested, and thus it is possible to obtain relations defining the average behavior over a time scale that is long compared to the time characteristic of fluctuation. With thin approach it is possible to derive the Navier-Stokes and the continuity equations and resolve the velocity field (Denn, ).

Before presenting the equations used to calculate the time-averaged axial velocity Vz it is better to introduce several variables commonly used for the study of turbulent flows.

In particular the *friction velocity* U* defined as:

\[ U* = \langle V_z \rangle (f/2)^{1/2} \]

where \( \langle V_z \rangle \) is the average velocity defined as the flow rate divided by the pipe-cross sectional area and f is the friction Fanning factor.
The time-averaged axial velocity is made dimensionless with respect to the friction velocity:

\[ U_+ = \frac{V_z}{U_*} \]

Distance from the wall is made dimensionless with respect to the friction velocity:

\[ y_+ = y \left( \frac{\rho U_*}{\mu} \right) \]

The dimensionless pipe radius, \( R_+ = R \left( \frac{\rho U_*}{\mu} \right) = \text{Re} \left( \frac{f/8}{\mu} \right)^{1/2} \).

For the turbulent core the equation for the assessment of the time-averaged axial velocity is:

\[ U_+ = 2.5 \ln(y_+) + 5.45 \]  \hspace{1cm} (1)

It has to be noted that if this equation is extended to the centerline region it does not give a zero gradient.

The maximum dimensionless time-averaged axial velocity is given by the logarithmic equation:

\[ U_+ = 2.5 \ln \left( \text{Re} \left( \frac{f/8}{\mu} \right)^{1/2} \right) + 1.37 \]  \hspace{1cm} (2)

Anyway equation (2) is not expected to provide a very good value for the centerline velocity.

For the viscous sub-layer the equation is:

\[ U_+ = y_+ \]  \hspace{1cm} (3)

With several mathematical passages it is also possible to assess the dimensionless viscous sub-layer \( \delta_{v_+} \). It is equal to 11.6.

In literature there are other correlations for the velocity profile in tube for fluid motion in transient conditions. In particular turbulent velocity profiles are often correlated empirically by power equation of the form:

\[ V_z = 0.5 \left( m+1 \right) \left( m+2 \right) \left( \frac{y}{R} \right)^{1/2} \]  \hspace{1cm} (4)

where \( m \) is usually in the range \( 1/10 < m < 1/6 \), with a value of \( m = 1/7 \) often used to
approximate behavior over several decades of Reynolds number.

In this case the exponent \( m \) can be linked to the Fanning friction factor \( f \) with this relation:

\[
m = 2f^{-}
\]  \hspace{1cm} (5)

where \( f \) comes from the Blasius equation for fluid motion in transient condition:

\[
f = 0.0079 \text{ Re}^{-1/4}
\]  \hspace{1cm} (6)

Equation 4) can be written in terms of turbulence dimensionless variables introduced above. Through several mathematical passages an analytic expression of the dimensionless viscous sub-layer can be written. In this case the viscous sub-layer thickness \( \delta_{vs+} \) is equal to 12.6.

The two values for \( \delta_{vs+} \) are comparable and they lead to good results for the calculation of the viscous sub-layer thickness.

The calculations have been realized for temperatures corresponding to \( T = 1000K \), \( T = 1400K \) and \( T = 1800K \). The values of Re for a system composed just of vapor water are respectively 10000, 5200 and 3300. The Re numbers indicate the system is in transient conditions. The results are reported in figure 3.6. Figure 3.6a) is relative to the logarithmic equation, figure 3.6b) is relative to the power equation. Even if in figure 4a) it has been reported the equation in terms of dimensionless variables the velocity reported in the diagram is the time-averaged axial velocity \( V_z \). It is plotted as function of the radial position. The radius of the duct is 0.5 cm.

The profiles for both the equations are in general quite parabolic and both the equations are not so sensitive to radical change of the Re numbers analyzed in these calculations. In the case of the power equation there is a more pronounced difference among the velocity profiles. The maximum values of the mean velocity \( V_z \) are for the three temperatures (1000K, 1400K and 1800K) respectively 128, 130 and 132 m/s.
In the case of equation 1) the profiles are less parabolic than the ones predicted by equation (4), the maximum mean velocities $V_z$ are very close to 125 m/s.

Using equation 2) it comes out that the maximum value does not depend so much on the Re number and the values are very close to 115 m/s. But as told above, equation 2) is not very good in predicting the value of the centerline velocity.

Furthermore it can be noted that the equations are not able to predict a flat profile of the velocity at the centerline.

![Figure 3.6](image.png)

*Figure 3.6 Velocity profiles obtained using the logarithmic equation (a) and the power equation (b).*

Another value to assess is the thickness of the viscous sub-layer. As matter of fact the very small dimension of the duct and the not so high Re values induces to think that its dimension must be relatively high and that it can not be neglected in comparison with the diameter. It is important to assess this parameter since it is necessary to estimate the portion of the diameter in which it can be assumed there is a fully developed fluid motion.

Both the logarithmic and the power equation give an analytic expression for the dimensionless viscous sub-layer thickness. From the literature the dimensionless $\delta_{uv}$ is
respectively equal to 11.6 or 12.6. For the three analyzed cases the value is $1.8 \times 10^{-2}$, $3.2 \times 10^{-1}$, $4.8 \times 10^{-1}$ mm for the logarithmic equation and $2 \times 10^{-2}$, $3.6 \times 10^{-2}$, $5.2 \times 10^{-1}$ mm for the power equation. It means that, in the worst condition, it will be the 10% of the whole diameter.

The equations found out in literature represent a useful tool to perform a quick but good study of the velocity field in a duct. Nowadays there are Computational Fluid Dynamics (CFD) codes that allow performing a more thorough analysis of the fluid motion in turbulent or laminar regimes.

Hence the CFD package software FLUENT 6 (www.fluent.com) has been used to perform further analyses. FLUENT 6 software includes the solver (FLUENT) and the preprocessor for geometry modeling and mesh generation (GAMBIT). Fluent is a general purpose package for modeling fluid flow, heat transfer, and chemical reaction. It can simulate two/three-dimensional, steady/unsteady, compressible/incompressible flows. Gambit is an integrated preprocessor for CFD analysis.

The simulations have been run enabling the Energy Equation, in order to take into account the right values of physical properties of vapor water at high temperature, and two turbulence models: the Standard $\kappa-\omega$ model and the Shear-stress transport (SST) $\kappa-\omega$ model (Silvio V. et al., 1999).

The choice of the turbulent model has a non-trivial relevance for the goodness of the numerical results in particular way in the region near walls. In fact turbulent flows are significantly affected by the presence of walls (www.fluent.com).

The $k-\omega$ models have been chosen since they are opportunely designed to be applied throughout the boundary layer, provided that the near-wall mesh resolution is sufficient.

The chosen models are “two equations” model so they are robust, economical in term of memory and CPU computational time, but at the same time they are accurate in
predicting the behavior of the fluid in the near-wall region.

The numerical simulation have been run in the three cases analyzed above with the literature equations. The results are presented in figure 3.7.

![Figure 3.7 Velocity profiles for vapor water for different temperatures using the Standard κ–ω and the SST κ–ω models.](image)

In this figure it is possible to see that velocity profile becomes more parabolic as the temperature, and hence the Re number, increases. For T=1000K the profile is almost flat and the velocity is very close to 100 m/s.

There is not a big difference between the two models of turbulence employed for the numerical simulations except for T=1400K. In fact for this condition the velocity profiles does not coincide and the value of the axial velocity are quite different. It is 119 m/s for the Standard κ–ω model and 125m/s for the shear-stress transport (SST) κ–ω model. In the other two cases the maximum velocity at the center line of the pipe are similar, for T=1000K the maximum temperature is 105 m/s and for T=1800K it is 128 m/s.

In the case of numerical profiles the viscous sub-layer thickness seems to be high, in fact it is almost 1 mm on both the sides of the duct. But this result strongly depends on the
mesh of the duct as it is possible to note in fig.3.8. In this figure the profile obtained for T=1000K is compared with a velocity profile for the same condition but with a coarser mesh of the cylindrical duct. In both the cases the model used is the standard $\kappa-\omega$.

![Graph](image)

*Figure 3.8* Comparison between the numerical velocity profiles obtained for a vapor water at 1000K using the standard model k-w and two different meshes.

The mesh density has also some influence on the velocity profile since, although the two profiles are in both the cases flat, there is a difference between the maximum values. For the denser mesh it is 105 m/s, in the other case it is 114 m/s.

Hence while the velocity profile is more acceptable in the case of numerical simulations, the relations found in literature are more suitable for a good estimate of the viscous sub-layer thickness.

A further numerical simulation has been run in order to see if there is any improvement in the velocity profile using a duct with a bigger diameter but with the same inlet velocity in order to keep constant the residence time and hence the resolution time of the oxidation process in mild condition.
The diameter of the new pipe was chosen equal to 1.4 cm. It means that the flow rate is doubled, since it changes with the square of the diameter of the duct, and the reactor power does as well. The simulation has been run condition for an inlet temperature T=1800K, hence in the worst condition. The results suggested that the velocity profile showed a slight improvement that does not justify the choice of a bigger diameter.

**Jet mixing into a cross-flow cylindrical reactor**

Jets in a confined cross-flow are widely used to mix different gases. Understanding the fundamental processes within the mixing zone plays a crucial role thus several works have been published on cylindrical ducts. Parameters such as orifice geometry, number of orifices and jet to stream mass flow ratio have been widely investigated.

An optimum mixer is defined by Hatch (Hatch et al.,1992) as one that produces an uniformly mixed flow field, without a persistent unmixed core or circumferential regions by the X/R=1.0 plane where X is the axial coordinate and R is the radius of the cylinder duct. It has been found a very important parameter in mixing degree is the jet to stream mass flow ratio J. It is defined as follow: J= \( \rho_j v_j^2/\rho_s v_s^2 \). They run some experiments varying the J values in a simple geometry with eight round equally spaced orifices displaced on the perimeter of the cylindrical duct. Changing J the penetration of the jet changes in particular increases if J increases. The results suggested there is a optimal penetration value to reach an optimum mix degree.

Overpenetration is undesired since the cross-flow gas tends to accumulate at the center of the duct instead of disperse and mix with the main flow in other words high jet penetration can cause impingement of the opposite jet at the center line which results in a central core of gas injected. On the other hand jet underpenetration decreases the maximum jet-main flow surface area of mix because a portion of the jet is bounded by the wall of the
duct resulting in the formation of a circumferential region.

In particular they found the increase of J improves mixing at the initial plane, since the penetration is higher, but degrades the overall mixing downstream the injection plane.

In general the effects of decreasing the momentum-flux ratio of increasing the number of orifices around the perimeter of a cylindrical duct is similar to the effects of increasing the number of orifices around the perimeter of a can (Holdeman et al., 1996). In fact increasing the numbers of holes decreases the jet penetration and allows more of the injected flow to pass through the center of the cylinder (Leong and Samuelsen, 1997). As the number of orifice increases, individual jets merge into a single structure that interacts differently with the main-stream flow. A configuration with more jets causes a faster dilution of the cross-flow gas and produces a more uniformly mixed flow structure toward the outer section of the mixing section. Hence it is generally advantageous to have an orifice configuration with a higher number of holes. For round holes, several investigation have determinated a jet penetration depth that leads to a better mixing. For example Talpallikar (Talpallikar et al., 1992) suggests the optimum mixing occurs when the jet penetrates to the mid radius. Holdeman indicates the optimal penetration radius as the radius which devises the duct into two equal area. The spacing between jets centerlines on the half area radius \( R_{1/2} = \frac{R}{\sqrt{2}} \).

In particular he found out that similar jet penetration is obtained over a range of momentum flux ratios when the orifice spacing \( S \) and the square root of the momentum flux ratio are inversely proportional. Holdemann defined a parameter \( C = (S/R)\sqrt{J} \) and he found out that for a single side injection, the jet centerline profiles approach a good mixing degree in the minimum downstream distance when \( C = 2.5 \). Value of \( C \) which are a factor of 2 either lower or higher than the optimum value correspond to underpenetration or overpenetration respectively. The spacing \( S \) between jet centerline is defined on the half
area radius: $S=2\pi R^{1/2}/n$ where $n$ is the number of holes. Holdeman derived the appropriate number of round holes as: $n=\sqrt{2J/C}$. The number of optimal number of holes hence is $n_{opt}=1.78\sqrt{J}$ or alternatively the optimum flux ratio $J_{opt}$, for a given number of round holes, is $J_{opt}=0.32 n^2$.

Other parameters were investigated in particular the geometry of holes; in the case of a slot geometry the slot aspect ratio and the slanted slot angle. The jet for a slot hole interacts in a different way with the main flow. In fact a jet from a round flow forms two counter rotating vortices of equal strength (Moussa et al., 1977). The jet penetrates directly towards the center of the duct, and the jet cross section is stretched as $J$ increases. In contrast the slanted slot initially forms a pair of counter rotating vortices which are of unequal size and strength. The asymmetry of the orifices with respect to the main flow direction promotes the development of one vortex of the pair, but suppresses the other (Holdeman, 1992). It means it is produced a swirl component which improves the circumferential mixing.

For a fixed momentum flux ratio and number of orifices, the smaller aspect ratio slots penetrate further into the cross stream. The larger aspect ratio on the other hand, produces a stronger swirl component and enhances the circumferential mixing. Holdeman (Holdeman et al., 1994) run some experiments comparing round holes and slot configuration. At the distance of $X/R=1/2$ the two systems exhibit roughly the same mixing, although the optimum $J$ for round holes is less then that for slant slots. It follows from the discussion in the previous section the optimum spacing for slanted slots would be greater than for round holes for the same momentum-flux ratio.

Hatch (1995) found out that increasing the slot angle the jet penetration to the center decreases but the swirl component and the circumferential mixing improves by the increase in the slots angle.
In analysis on a rectangular duct Holdeman investigated the effect of convergent walls on mixing. It was found the profiles for symmetric convergence are more uniform than the corresponding straight duct wall. Although a detailed analysis was not run, Holdeman (1984) hypothesized that the enhanced mixing that was observed in converging sections could result from stretching of the strong dual vortices that are typical of jet-in-crossflow. It was noted by Stevens and Carrotte (1987) that this effect could also be due to the axial velocity does not decay as rapidly in a converging duct, and thus the production of vortices to negate that of the jet structure is minimized and enhanced mixing is obtained.

In order to realize a very short mixing time all these results have to be taken into account. It has been found high momentum flux ratio improves the mixture uniformity at the inlet plane even if penalizes the uniformity of the mixing in the hole mixing area. Since the hydrogen-oxygen system is very reactive maybe a configuration that foresees a high $J$ is to be chosen. To enhance $J$ one can increase the jet velocity to the highest value possible taking into account that the pressure drop and the sonic velocity of the gas injected are quite stringent bundles. In particular it has been thought a cylindrical duct in which the first zone has a bigger diameter in order to lower the main stream velocity and enhance the parameter $J$. After the injection a restriction of the diameter is suitable, by this way the diameter is equal to the desired value and, at the same time, the mixing can enjoy the benefit of a convergent duct.

Several calculations have been realized by using the Holdeman equation to assess the optimal number of orifices. The main stream is water, the cross-flow one is hydrogen. Water vapor density was estimated at 1400K which is the medium temperature in which our experiments will be performed, hydrogen density at 300K. The following logical steps have been followed to calculate the optimal injection geometry:

$$v_j \Rightarrow J \Rightarrow C=0.25 \Rightarrow S \Rightarrow n \rightarrow d_i$$
A certain $v_j$ value has been chosen, it allows to calculate $J$ since all the parameters needed to calculate $J$ are available. In order to enhance $J$, $v_s$ (Stream velocity) is set equal to 50 m/s considering a cylindrical duct with a diameter equal to 1.4 cm. After the injection the duct converges and the $D$ will become 1 cm. Now it is possible to assess the value $C$ which allows to calculate $S$ and so $n$. Since $n$ is a discrete number it will be approximated to the closest discrete value for excess or defect. At this point the $J_{\text{opt.}}$ can be easily calculated since $J_{\text{opt}}=0.32 \ n^2$, which means $C=0.25$ hence $v_j$ and $d_t$ can be finally estimated. This set of parameters optimizes the injection system. Since our aim is to have the highest possible $J$ the ideal system is the one with 12 round orifices, a inlet velocity of 471 m/s and $J=46$ and $d_t=0.035 \ mm$. The obtained velocity is enough lower respect to the sonic velocity in hydrogen that, at ambient temperature, is 1300 m/s. This configuration allows for a good mixing for $X/R=1$, it means the mixing time will be 100 $\mu$sec.

![Possible scheme for the mixing part.](image)

A preliminary analysis has been realized in order to see if the ignition times were compatible with the mixing time. In order to perform this analysis the Plug Application of ChemKin software was used. The $H_2$-O$_2$ kinetic mechanism used was the one provided by Marinov (1996). The simulations were run in adiabatic condition. The results are summarized in figure 3.10. Figure 3.10.1 and 3.10.2 are relative to a $H_2/O_2/H_2O$ stoichiometric mixture with a dilution degree equal to 90%. Figure 1) shows the numerical axial temperature profiles for different inlet temperatures. Figure 2) shows the $\tau$ ignition
and the $\tau$ reaction time for the same system.

![Figure 3.10 Numerical temperature profiles and characteristic times.](image)

In Figure 3.10 the numerical temperature profiles for a $\text{H}_2\text{O}_2$ stoichiometric mixture with different dilution degrees (from 90% to 98%) are plotted. In figure 3.10.4) it is possible to see how the ignition time changes as function of this parameter. It plays a very important role for making ignition and reaction time comparable and compatible with the mixing one.

The same analysis has been repeated more thoroughly for the system $\text{CH}_4/\text{O}_2/\text{N}_2$ and $\text{CH}_4/\text{O}_2/\text{H}_2\text{O}$. The results are reported in the next sections.

**Numerical Tools**

**CHEMKIN**

ChemKin is a software designed by SANDIA NATIONAL Laboratories to facilitate the formation, solution, and interpretation of problems involving elementary gas-phase
chemical kinetics. It provides a flexible and powerful tool for incorporating complex chemical kinetics into simulations of fluid dynamics. The ChemKin Gas-phase Utility package consists of two major software components: an Interpreter and a Gas-Phase Subroutine Library. The Interpreter is a program that reads a symbolic description of a user-specified chemical reaction mechanism. The mechanism includes species information, as well as reaction path and rate descriptions. Output from the Interpreter forms a link to the Gas-Phase Subroutine Library, which may then be accessed from a CHMKIN Application. The subroutine library is a collection of more than 100 modular FORTRAN subroutines that may be called to return information on equations of state, thermodynamic properties, and chemical production rates.

ChemKin-based simulations are used widely in the development and optimization of combustion and other chemical processing systems. In addition, CHMKIN includes capabilities for treating systems that are not in thermal equilibrium, such as plasmas, where reactions may depend on multi-fluid temperatures associated with electrons or ions.

**AURORA**

Continuously stirred tank or well-mixed reactor models have been in use for many years in the study of chemistry within a unit process for a variety of applications. For thermal (neutral) systems, perfectly stirred reactor (PSR) models are a common method for testing and developing chemical reaction mechanisms. Such reactor models are widely employed in combustion research. Well-stirred reactor modelling that includes detailed surface reaction mechanisms is applicable to thermal chemical vapour deposition (CVD) systems, as well as many other materials and catalytic processes. In the plasma simulation for microelectronics processes, global or well-mixed reactor models are used to predict average electron energies and electron densities for a variety of power-deposition
The AURORA model allows simulation of both dynamic and steady-state reactor systems. For dynamic systems, the user may specify reactor conditions that vary as a function of time. For steady-state systems, AURORA can compute a series of steady-state conditions varying one or more parameters, such as heat-loss or pressure, between simulations. The AURORA program also includes an option to represent multiple stirred tank reactors that are connected in series. Each stirred tank reactor can have different temperatures, heating rates, volumes, and surface areas, for example.

PLUG

PLUG simulates the behavior of plug-flow chemical reactors. More specifically, the program is designed to model the non-dispersive, one-dimensional flow of a chemically reacting, ideal-gas mixture in a conduit of essentially arbitrary geometry. PLUG solves the set of differential/algebraic equations describing the reactor using the implicit numerical software DASSL the set of differential/algebraic equations describing the reactor.

Tubular flow reactors have long been used throughout the chemical process industries. The tube flow configuration is a natural choice for processes that are carried out in a continuous fashion. For this reason, such reactors are usually operated at steady state. Traditional applications have included both homogeneous reactions (carried out in an empty tube) and fluid-solid heterogeneous reactions in packed beds. More recently, tubular reactors have been used extensively to deposit thin solid films via chemical vapor deposition (CVD). While this is technically a batch process with regard to the solid deposit, the reactor still operates essentially at steady state for extended periods of time. PLUG is a general model for the steady-state tube flow reactor that can be used for process design, optimisation, and control.
Because the general equations for chemically reacting flow involve transport phenomena in addition to kinetics and thermodynamics, rigorous reactor models are by necessity multidimensional. However, there are often practical as well as mathematical reasons for considering idealized models of reduced dimensionality. In the case of tube flow, the accepted ideal is the plug-flow reactor, in which it is assumed that there is no mixing in the axial (flow) direction but perfect mixing in the direction(s) transverse to this. It can be shown that the absence of axial mixing allows the achievable reactant conversion to be maximized. Likewise, the lack of transverse gradients implies that mass-transfer limitations are absent, once again enhancing the reactor performance. Along with these practical advantages, the plug flow reactor is computationally efficient since it is modelled using first-order ordinary differential equations (ODE.s), and no transport properties are needed.

SPIN

The SPIN program computes species, temperature and velocity profiles, as well as deposition rates in a steady-state, one-dimensional rotating disk or stagnation-point flow chemical vapor deposition (CVD) reactor. The program accounts for finite-rate gas-phase and surface chemical kinetics and multi-component molecular transport. The governing differential equations form a two-point boundary value problem.

After discretization by a finite difference procedure, the resulting non linear algebraic equations are solved by a modified Newton algorithm. The Newton algorithm is implemented in a software package called TWOPNT. SPIN also runs in conjunction with the CHEMKIN, SURFACE CHEMKIN and TRANSPORT. In a rotating-disk reactor a heated substrate spins (at typical speeds of 1000 rpm or more) in an enclosure through which the reactants flow. The rotating disk geometry has the important property that in certain operating regimes the
species and temperature gradients normal to the disk are equal everywhere on the disk. Thus, such a configuration has great potential for highly uniform chemical vapor deposition (CVD), and commercial rotating disk reactors are common, particularly for materials processing in the microelectronics industry.

**DSMOKE**

DSMOKE is a program developed to simulate a variety of flame and combustion processes. This code can deal with ideal reactors, complex networks of ideal reactors and dynamic JSR. The program accepts only sequential schemes (i.e. no recycle streams). It is composed by a chemical interpreter, that allows to read the kinetic mechanism and the thermodynamic properties of the species, and by the reactor model.

Several parts of this package are directly taken from the experience developed in the pyrolysis and combustion modeling. The numerical solution is performed by assuming the reaction classes BzzOde developed in C++ (E.Ranzi, 2001).

The CSTR model allows simulation of both dynamic and steady-state reactor systems. For dynamic systems, the user may specify reactor conditions that vary as a function of time. The set of equations describing the transient behavior of the JSR is reported elsewhere (T.Faravelli et al., 1998).

**FLUENT**

Fluent is a commercial computational fluid dynamic (CFD) software. It is used for simulation, visualization, and analysis of fluid flow, heat transfer, chemical reactions, turbulence and multi-phase problems. It is based on the finite volume method. Mesh and geometry definition are created using pre-processor Gambit and Tgrid.
Chapter IV

Experimental Results

Choice of working Parameters

The study of the oxidation process of Mild conditions has been realized in the JSFR reactor. The choice of working parameters, such as the hydrocarbon, residence time and inlet temperature, responds to determinate practical and theoretical requirements.

The chosen hydrocarbon is methane. As matter of fact, since the aim of the work is to examine the kinetic behavior of the oxidation process in new working conditions, the study has to be realized for the simplest possible condition. Methane is the simplest hydrocarbon and it notoriously exhibits a kinetic behavior less complex in comparison with higher molecular weight hydrocarbons.

Nitrogen has been chosen as diluent since it is an inert species. In such a way, the kinetic behavior of methane has been studied in absence of species that could have altered the kinetic pathways of the methane. Two different diluent levels of the mixture have been set during the experimental tests. They are 85% and 90%.

The feed fuel-comburent ratio, identified with the parameter C/O, has been changed in a range that goes from values very close to zero to 1.5. Since the fuel-comburent ratio C/O in stochiometric condition is equal to 0.25, in the experimental tests both lean (C/O < 0.25) and rich mixtures (C/O > 0.25) have been analyzed.

The choice of the residence time $\tau$ responds to theoretical and practical requests, in fact, as reported in chapter III, the analysis of the mixing degree of the JSFR reactor suggested the use of values lower than 0.55 seconds. As matter of fact, for values lower than this threshold, the reactor behaves, with reasonable approximation, as a perfect stirred
flow reactor. Hence the residence time has been set equal 0.5 seconds.

The temperature range in which the kinetic behavior of methane has been studied is comprised between 825K and 1250K. This range has been set considering that, for lower temperatures the system does not react for any values of the C/O feed ratio and, for temperature higher than 1250K the oxidation reaction would have led the system to overcome the limit temperature of quartz inducing high thermal stresses and the softening of the reactor itself. The experimental tests were realized any 25K covering all the temperature range.

The pressure value has been set equal to 1.17 atm. This value allows the exhaust gases to overcome the pressure drop in the plant.

The tab.4.1 reassumes the chosen working conditions:

<table>
<thead>
<tr>
<th>Reactor</th>
<th><strong>Jet Stirred Flow Reactor (JSFR)</strong></th>
</tr>
</thead>
<tbody>
<tr>
<td>Residence time $\tau$</td>
<td>0.5 sec</td>
</tr>
<tr>
<td>Temperature Range</td>
<td>825K-1250K</td>
</tr>
<tr>
<td>Dilution Degree</td>
<td>85%, 90%</td>
</tr>
<tr>
<td>Pressure</td>
<td>1.17 atm</td>
</tr>
</tbody>
</table>

*Tab. 4.1 Chosen working conditions for Mild Combustion studies.*

**Experimental Ignition Map**

The experimental study performed on methane Mild oxidation was focused on the identification of the system behavior as function of the inlet temperature (Tin.), C/O ratio and dilution levels. During the set of experiments, the temporal temperature profiles, recorded by means of a facility well described in chapter III, suggested that the oxidation of methane in conditions typical of Mild processes, gives rise to a complex dynamic
behavior and the attention has been focused mainly on the characterization of this new phenomenology. It has only partially identified in the past in methane oxidation by means of a numerical study (Lignola, Minale, Rotondi, 1997; Basevich, Kogarko, 1983, Maione N., et al. 2000). On the other hand, the experimental studies reported in literature, that evidenced the oscillatory behaviors in methane oxidation, were performed at lower temperatures and in batch conditions (Vanpée, 1956; Vanpée, 1993, Egret J. et al, 1965).

The first approach to this problem was the partition of the working conditions for which the system evolves through stable combustion or oscillating regimes.

![Bifurcation Map](image)

**Figure 4.1** $T_{inlet}$-C/O bifurcation map obtained for a dilution level of 90%, $\tau=0.5$ sec.

Since the residence time $\tau$, the pressure and the dilution level have been fixed, the only parameters to set up are the inlet temperature and the carbon-oxygen feed ratio C/O. In order to have a descriptive indication on possible stable or periodic states, the results were resumed in bifurcation maps of the system by using $T_{in}$ and C/O ratio as continuation parameters for the two dilution levels considered. Any point of the $T_{inlet}$-C/O plane represents an inlet condition, and it has been classified on the basis of the system stability.
The experimental bifurcation map obtained for a dilution level of 90% and a residence time of 0.5 sec is reported in Figure 4.1. In correspondence of these experimental settings, regions associated with un-reactive, stable combustion and dynamic conditions have been identified.

The region where no ignition is detected extends from 825 K and C/O=0.6 up to 975 K and very low C/O ratio and is represented with a white region in Figure 4.1.

All the other C/O and temperature values on the map identify reactive conditions. In particular, the widest region corresponds to stable combustion where a single step ignition leads the system to a steady working temperature. Depending on the Tin. and C/O ratio, one or two different steady reactor temperatures can be reached for the same inlet conditions. The former case, i.e. a single measured working temperature, is identified by the “stable combustion” area in the Figure 4.1. In contrast, the “hysteresis” region, where two different reactor temperatures (TR1 and TR2) can be reached for the same inlet conditions according to the procedure described in the experimental section, is represented by the dotted and the dashed areas. The dotted area represents the region where the two steady states correspond to un-reactive (T_{in.} = TR_1) and stable combustion (TR_2 > T_{in.} = TR_1) conditions respectively. On the other hand, the dashed area identifies the C/O and Tin. in correspondence of which two different reactive conditions are reached. In this case TR_2 > TR_1 > T_{in.}. Moreover both of the steady states are stable, such as shown by the response of system to an induced displacement from the steady state itself. It was shown that a pressure perturbation makes the system slightly shift to the steady state for a while and then it reaches again the same state. The hysteresis region extends from C/O=1.4 down to 0.2 and from T_{in.}=825 K to T_{in.}=975 K.

As described so far, the steady combustion is the only phenomenology occurring in the region of richest C/O ratios down to 0.55 in the whole temperature range analyzed. At
lower C/O ratios and T\textsubscript{in.} higher than 1020 K a region where dynamic behavior occur was also recognized. For C/O=0.55 temperature oscillations occur in a range of 50K, from T\textsubscript{in.} = 1150K up to 1200K. The oscillating temperature region enlarges by decreasing the C/O ratio thus covering the temperature range between 1025 K up to 1275 K in correspondence of the leanest C/O ratios.

### Temporal Temperature Profiles

The area relative to the dynamic behavior has been subdivided in several sub-region in according to the temporal temperature profiles.

In this paragraph the temporal temperature profiles characteristic of any kind of oscillations experimentally detected will be presented.

Figure 4.2 shows the oscillations detected for an inlet temperature equal to 1075K and a carbon/oxygen ratio equal to 0.2. Hereafter this oscillation will be named “cusp”. In this case the temperature jump is of about 75K, and the frequency is 0.15 Hz. During an oscillation the temperature first increases relatively slowly but then there is an abrupt jump until the peak of the oscillation, followed by a repentine decrease of the temperature. This oscillation is, hence, characterized by two different phases.

![Figure 4.2](image)

**Figure 4.2** “Cusp” oscillation detected for T\textsubscript{in.}=1075K and C/O=0.2.
Figure 4.3 shows the oscillations collected for an inlet temperature equal to 1125K and a carbon/oxygen ratio equal to 0.5. The shape of this oscillation reminds a bell hence hereafter it will be named “bell” shaped. The amplitude of the oscillation is almost one hundred Kelvin degree and the frequency is 0.2.

Figure 4.3  “Bell” oscillations detected for Tinl. =1125K and C/O=0.5.

Figure 4.4 shows the oscillations detected for an inlet temperature equal to 1175K and a C/O feed ratio equal to 0.4. Hereafter, this oscillation will be named “triangular high amplitude”. The oscillations appear to be symmetric. In this case the temperature jump is 40K and the frequency is 1Hz.

Figure 4.4  “Triangular high amplitude” oscillations detected for Tinl. =1175K and C/O=0.4.
If it is considered a mixture at the same inlet temperature but with a C/O feed ratio equal to 0.1 it is possible to see that the system evolves through a triangular oscillation but in this case the oscillation amplitude is very small, in fact is 2-3K. At the same time, it has a very high frequency it is equal to 3.2 Hz.

The triangular oscillation presents the same characteristic, in fact it is symmetric, but in order to differentiate the two oscillations this one is named “triangular”.

![Figure 4.5](image1.png)

**Figure 4.5** “Triangular” oscillations detected for Tinl. = 1175K and C/O = 0.1.

Figure 4.6 shows the oscillations detected for an inlet temperature equal to 1200K and a carbon/oxygen ratio equal to 0.3. Hereafter this oscillation will be named “double”.

![Figure 4.6](image2.png)

**Figure 4.6** “Triangular” oscillations detected for Tinl. = 1200K and C/O = 0.3.

As matter of fact, it is possible to distinguish two different temperature peaks that
alternate each other. The former is higher than the latter. The amplitude of the oscillation, in this case, is very small, just 5K and the frequency, considering the oscillation composed by the two oscillations, is 1Hz.

The last typologies of oscillation is the irregular one. Figure 4.7 shows the oscillations detected for an inlet temperature equal to 1200K and a carbon/oxygen ratio equal to 0.2. Hereafter this oscillation will be named “irregular”. In this case it is not possible to distinguish a temperature amplitude or frequency.

Figure 4.7 shows just an example of irregular oscillations but they can appear also with other temporal temperature profiles. Anyway, the common characteristic is that in this kind of oscillation it is not possible to recognize an amplitude and/or a frequency value.

All these kinds of oscillations have been resumed in figure 4.8. Here the axes values are not reported since this figure has the aim to identify and resume the several typologies of oscillations experimentally detected. Once again, the figure 4.8 presents again the bell-shape oscillations (a), the cusp shaped oscillations (b), the triangular (c) and finally the double ones (d).
Figure 4.8  Waveform typologies recognized during dynamic regimes.

The oscillations cataloguing can be used to split the dynamic region in several sub-regions on the basis of the waveform shape. The ignition map is shown in Figure 4.9.

Figure 4.9  Experimental map of stability obtained for methane oxidation in diluted conditions.
The bell-shape oscillations, related to the waveform of Figure 8a, occur for C/O between 0.55 and 0.25 in a narrow temperature range, from 1125K up to 1175K.

The cusp-shape oscillations are represented by the temperature profile Figure 4.8b. They show the typical profile of two-step ignition process due to the first slight temperature increase followed by a second one, very sharp with respect to the former. They occur for C/O between 0.4 and 0.05, from \( T_{\text{inlet}} = 1025K \) to \( T_{\text{inlet}} = 1175K \). At the right side of cusp-shape and bell-shape oscillation zones, the triangular oscillations region can be identified. They are associated to the waveform reported in Figure 4.8c and occur in a temperature region that covers the whole temperature range analyzed. This zone extends between 1175K and 1275K for C/O higher than the stochiometric value (C/O=0.25) whereas it enlarges towards lower temperatures for lower C/O ratios. Inside the region of triangular oscillations, a zone of double or irregular behavior is present. The temporal temperature profiles obtained in this region generally show a double or multi-peak waveform such as shown by the temperature temporal profile reported in Figure 4.8d.

**Analysis of Frequency**

The oscillation frequency depends on the temperature and C/O values considered. In Figure 4.9 the frequency profiles have been reported as function of temperature for different C/O values. For C/O = 0.01 the frequency increases with temperature from 1.8Hz at 1100K to about 7Hz at 1200K. The same trend can be detected for higher C/O ratios using the inlet temperature as continuation parameters, at the same time for a fixed temperature the frequency decreases when C/O increases.
This behavior occurs in the whole temperature range for C/O ratios lower than 0.4. In fact, the frequencies measured in this case for T > 1200K are higher than the ones obtained for C/O=0.3. As matter of fact, for C/O=0.4 and for a temperature higher than 1200K the oscillation typology is “triangular” while, for C/O=0.3 and for an inlet temperature comprised between 1175K and 1250K, they are “high amplitude triangular”. As underlined above, the triangular oscillations have a lower amplitude, respect the high amplitude triangular oscillation, but an higher frequency.

The dashed line is relative to the irregular and double oscillations, hence, in this case, it is not possible to identify a frequency value.

**Effect of the Residence Time**

The effect of residence time $\tau$ on system behavior was experimentally analyzed for several inlet conditions. Fig.4.10a shows the temperature temporal profiles collected at
$T_{\text{inlet}}=1150\text{K}$ and C/O=0.2 for different $\tau$. This parameter was changed from 0.5 sec down to the minimum value of 0.35sec; it could not be further lowered because the reactor temperature could have become too high. For 0.5sec, the system allows for the detection of a double oscillation. The first temperature peak is quite smooth. In contrast, the second one is very sharp and the system reaches its highest temperature of about 1390K. For $\tau=0.45\text{sec}$, the oscillation typology is the same although the first peak is less pronounced and the second peak reaches a higher temperature of 1450K. A further $\tau$ decrease to 0.4 sec merges the two double oscillation peaks into a single peak which reaches a maximum of about 1500K. The single peak feature is held for 0.35 sec where $T_R$ reaches about 1540K.

![Figure 4.10](image)

*Figure 4.10  Temperature temporal profiles at C/O=0.2 (a) and C/O=0.4 (b) and $T_{\text{inlet}}=1150\text{K}$ for different residence times.*

A similar trend of bell-shaped oscillations versus $\tau$ at C/O=0.4 can be discerned in
In this case too, the temperature reached during oscillation increases as $\tau$ decreases although the shape features are held up to 0.35 sec where the system achieves a steady temperature.

**Effect of the Dilution Degree**

Because the aim of the present work concerns also the study of the dilution and mixture composition on the dynamic behavior of the system, the experimental analysis at different dilution level was focused in the region where oscillation phenomenology was found. In Figure 4.11 the bifurcation map obtained for a dilution level of 85% was reported for a temperature range from 975 K up to 1275 K and C/O varying from 0 up to 1.

The general behavior pointed out at lower dilution level is substantially the same with respect to the one obtained at 90%. However, a decrease in dilution level slightly reduces the extension of the region where oscillations occur. This is more evident at higher temperatures where the triangular oscillation area that delimits the oscillation region on the right side of the map at 90% of dilution disappears at the lower dilution level analyzed.

![Figure 4.11](image_url)  
*Figure 4.11*  
$T_{\text{inlet}}$-C/O bifurcation map for a dilution level of 85%, $\tau$=0.5 sec.
Furthermore, high amplitude triangular oscillations are no longer detected and they are partially substituted by the double oscillation region that enlarges up to $C/O = 0.3$. At higher $C/O$ ratios they damp after a time that depends on working conditions and the system reaches a steady state temperature. An example of a temperature temporal profile collected in these conditions is reported in Figure 4.12.

![Figure 4.12](image)

**Figure 4.12**  *Damped oscillation temperature profile at 85% of dilution.*

### Effect of Hydrogen Addiction

The Mild Combustion of natural gas pointed out the insurgence of complex dynamic behaviors due to thermo-kinetic temperature oscillations. In practical applications such instabilities strongly reduce the efficiency of combustion processes.

Furthermore from a practical point of view, the presence of such instabilities could give rise to high frequency oscillations in combustion chambers, generally responsible of efficiency decrease and of serious damages in gas turbine burners. Such dynamic behavior is hidden in conventional processes involving methane by the relatively fast oxidation kinetic that characterizes traditional gaseous fossil fuels.

Moreover, the activation of different kinetic pathways hypothetically responsible of oscillations could induce an increase of pollutants formation.

On the other hand hydrogen has been declared the energy vector of the future. But the available systems of production, storage and transport of hydrogen are not still ready to
allow for managing this clean fuel in a proper way. Moreover, its high reactivity and its very high calorific power make hydrogen combustion quite difficult to control. Hence the establishment of an economical and energetic system based on hydrogen technologies still requires some improvements. In the meantime hydrogen has been used in several ways such as “fuel enhancer” (Fotache C.G. et al. 1997; Ju Y. el al., 1995; Karim G.A et al., 1996, Bade et al., 1996) to promote ignition of low calorific power fuels or in engines characterized by a high level of recirculation (EGR) of exhaust gases (Allenby et al., 2001).

These features are very close to the Mild Combustion conditions that use high dilution and high pre-heated reactants. As matter of fact these working conditions moderate the hydrogen high reactivity and allow for a more controlled use of this fuel. Mild Combustion (Cavaliere A. et al., 2004) represents a good trade-off in the passage between an energetic system based on fossil fuel towards hydrogen.

Hence the effect of hydrogen addition to the methane combustion in Mild conditions has been studied, with particular focus on the phenomenological effect that hydrogen has on the dynamic behavior found out during experimental tests realized in the past on the methane oxidation in Mild processes.

The study of the oxidation of methane-hydrogen mixtures in Mild condition has been realized in the Jet Stirred Flow Reactor well described in the chapter III.

Experimental tests were carried out at atmospheric pressure for different inlet temperature and mixture composition. In particular, the carbon/oxygen (C/O) feed ratio was changed from values close to zero up to 1.2 and hydrogen concentration was fixed equal to 0.25%, 0.5%, 0.75% and 0.9% for a constant dilution and residence time (t). Hence, nitrogen volumetric fraction was fixed at 90% of the inlet flow, whereas CH₄, H₂ and air fractions were changed simultaneously to keep t at a constant value of 0.5s. For
each C/O ratio and H$_2$ percentage, $T_{in}$ was changed from 970 K up to 1300 K.

![Ignition map](image)

**Figure 4.13**  Experimental ignition map for the system CH$_4$/O$_2$/N$_2$.

First of all the experimental tests carried on for system CH$_4$/O$_2$/N$_2$ were repeated in order to confirm the previous results and have a new database to properly compare the result obtained with the system CH$_4$-H$_2$/O$_2$/N$_2$. This was necessary since the oscillations come from the interaction between the kinetic and the exothermicity of the system, the system is very sensible to any variable that influences this interaction. Hence also the air temperature, which depends on the environmental factor, can lead to different results. Anyway the main features of the methane oxidation in Mild Condition and in particular way the dynamic regimes have been detected again although the extension of the map, where oscillations have been found out, is slightly reduced. These results show that the experiments are quite well reproducible

Fig 4.13 represents the ignition map obtained for a system in which methane and oxygen are mixed and diluted up to the 90% with nitrogen and fed to the reactor with a residence time equal to 90%. The temperature range analyzed is comprised between 925K
and 1325K, while the C/O feed range has been changed from values very close to 0 to 1.2. The pressure is again 1 atm.

The experimental results have been resumed in the $T_{in}$-C/O plane reported in fig.1. Each point in this map represents inlet conditions. In the $T_{in}$-C/O plane for very low temperature and C/O ratios the map shows a “no ignition” region where there is not a significant increase of temperature in the reactor. Again it is shown the inlet conditions, hence the temperature and C/O feed ratios for which the system evolves through a steady or a dynamic regime.

A thorough description and analysis of the map relative to the oxidation of the methane is reported in chapter V. The only difference with the map reported in such a chapter is that here a small area where damped oscillations is present.

Anyway in this new experiments the attention has been focused on the study of the hydrogen addiction effects on the system $CH_4/O_2/N_2$, hence some analyses, i.e. the hysteresis of the system or the frequency study, has not been repeated.

![Figure 4.14a](image)

*Figure 4.14a  Experimental ignition map for the system $CH_4-H_2/O_2/N_2$.}*
The experimental analyses carried out varying the hydrogen inlet percentage have led to four ignition maps, reported in fig.4.14, respectively corresponding to a molar fraction percentage equal to 0.25 (a), 0.5 (b), 0.7 (c) and 0.9 (d).

The first ignition map is relative to a mixture CH₄-H₂/O₂/N₂ with a molar hydrogen molar fraction equal to 0.25%. In the figure clearly it is shown the regions where the system evolves through a steady combustion regime or a dynamic regime. Furthermore this last region has been divided in two parts. The clearer one corresponds to damped oscillations. They have been reported since after a transitory the system is able to work in steady conditions without the presence of oscillations.

The dynamic region extends from 1040K to about 1270K and for a C/O feed ratio that goes from values very close to zero to 0.4.

![Ignition map](image)

*Figure 4.14b Experimental ignition map for the system CH₄-H₂/O₂/N₂.*

The damped oscillations develop for inlet conditions comprised in a temperature range that goes from 1170K to 1270K and a C/O feed ratio that goes from 0.05 to 0.4. Hence the region relative to this kind of oscillation mainly develops for lean mixtures and
it interests inlet conditions on the left side of the whole dynamic region.

The figure 4.14b is then relative to the same system but with a total hydrogen molar concentration equal to 0.5%.

Similar considerations apply for this new case. For the most of the conditions the system evolves through a steady combustion regime. For temperature comprised between 1004K and 1260K and C/O feed ratios comprised between 0.05 and 0.4 a dynamic regime is established. Furthermore it is evident that the region relative to damped oscillation widens. In particular it mainly develops in the left side of the dynamic region but for this hydrogen percentage a small area for an inlet temperature equal to 1075K and a C/O feed ratio equal to 0.1 develops.

![Experimental ignition map](image)

**Figure 4.14c**  Experimental ignition map for the system CH\(_4\)-H\(_2\)/O\(_2\)/N\(_2\).

Figure 4.14c is relative to a system CH\(_4\)-H\(_2\)/O\(_2\)/N\(_2\) where the hydrogen is fed with an inlet concentration equal to 0.75%. More or less the dynamic region widens for the same inlet temperatures and C/O feed ratios but the damped oscillation region become increasingly more important and covers a very wide region of the dynamic area. The region that, for the previous case, develops for low temperature and C/O feed ratios
enlarges significantly. The same considerations apply for the last analyzed hydrogen concentration (H$_2$=0.9%).

Also in these further cases it was possible to recognize the same dynamic phenomenology. Furthermore hydrogen addition does not affect significantly the oscillations typologies detected for the CH$_4$/O$_2$/N$_2$ system and previously described, thus the dynamic region was subdivided into the same sub-regions.

The typologies of the several kind of oscillations experimentally detected are presented again in figure 4.15.

![Figure 4.14d](image)

*Figure 4.14d  Experimental ignition map for the system CH$_4$-H$_2$O$_2$/N$_2$.  *

Hence again there are bell-shaped (a), cusp-shaped (b), irregular (c), double (d), triangular (e) and damped (f) oscillations.

In this case there are not the high amplitude irregular oscillations since, as shown in the chapter V, the only differences with the triangular ones are the amplitude and the frequency but the shape remains equal.
Figure 4.15  Several kind of oscillations experimentally detected for the system CH$_4$-H$_2$/O$_2$/N$_2$.

Also in this figure it has been reported a profile relative to irregular oscillations, but it is worth reminding that there is not a standard profile and that the main feature of these oscillations is the impossibility of identifying an amplitude and/or a frequency value.

Figure 4.16  Experimental ignition maps corresponding to a hydrogen molar fraction respectively equal to 0%.
On the basis of the oscillations shapes it was hence again possible to split the dynamic region obtained for the system CH₄/O₂/N₂.

Figure 4.16 shows the division of the experimental ignition map of the system CH₄/O₂/N₂.

The same analysis has been realized for the systems CH₄-H₂/O₂/N₂ with various hydrogen concentrations and the results are shown in fig.4.17.

In particular, for a hydrogen percentage value equal to 0.5%, it is possible to recognize a small “damped” oscillations region, in correspondence of T_in equal to about 1070K and C/O of about 0.1.

Figure 4.17  Experimental ignition maps corresponding to a hydrogen molar fraction respectively equal to 0.25% (a), 0.5 % (b), 0.7 % (c) and 0.9 % (d).

As the hydrogen concentration increases, the region relative to damped oscillation
extends and for a hydrogen molar fraction percentage equal to 0.9% it interests a \( T_{in} \) range comprised between 1050 and 1150K and a C/O range going from values very close to zero to 0.2.

The same effect concerns the “double and irregular” oscillations zone that becomes wider as the hydrogen inlet percentage increases. In absence of hydrogen it is possible to find this oscillations typology in the \( T_{in} \) range of 1100K-1270K and in the C/O range of 0.1-0.4. In presence of hydrogen the whole dynamic behavior zone reduces itself, but the relative importance of the “double and irregular” oscillations increases. As matter of fact, for \( H_2 \) equal to 0.25%, this region extends from \( T_{in} \) equal to 1050 to 1250K and C/O range from 0.15 to 0.35 while for the mixture containing 0.9% of hydrogen. \( T_{in} \) goes from 1050 to 1200K and C/O goes from 0.05 to 0.4.

Furthermore, cusp-shaped oscillations disappear from a \( H_2 \) value of 0.75%, and the triangular oscillations region becomes evidently smaller.

**Bifurcation diagrams**

In order to extensively describe the phenomenology detected in diluted oxidation of mixture of hydrogen and methane it is useful to analyze reactor temperatures in different conditions. To this aim experimental bifurcation diagrams obtained by fixing one of the continuation parameters considered above were represented in Figure 4.17, where reactor temperatures \( (T_{R1}) \) measured for C/O ratios of 1, 0.7, 0.4 and 0.1 were reported as function of \( T_{in} \).

For C/O=1 the reactor temperature is very close to the isothermal line until an inlet temperature equal to 1025K. After this value the system evolves trough a dynamic regime, as the dashed lines show. The maximum working temperature is reached for an inlet temperature equal to 1050K, but increasing the value of the continuous parameter the mean reactor temperature decreases and the system reaches a steady solution for \( T_{in} \) equal to
1200K. Then the temperature increment (ΔT) remains almost constant and it is of about 20K. In the previous experimental analysis, realized on the same system with the same operative conditions, this value was of about 50K. As explained above, it is due to the high sensitivity of the system to the working parameters but it is anyway worth noting that the main features of the bifurcation diagrams remain.

![Bifurcation diagram](image)

**Figure 4.17** Bifurcation diagram for the system CH₄-H₂/O₂/N₂ for an hydrogen global percentage equal to 0%.

In figure 4.17 the bifurcation diagram for the system CH₄/O₂/N₂ is reported on curves parametric in the C/O feed ratio.

For C/O=0.4, hence in reach conditions, for very low inlet temperatures, relatively to the temperature range analyzed, the temperature increment is very low but then it increases until the system, for Tᵢₙ=1125K, starts oscillating. The temperature increment firstly increases, reaches a maximum but then it decreases and the system gains a steady combustion regime for Tᵢₙ>1125K.

However the difference between the reactor temperature and the inlet one is of about 20K and this ΔT remains constant in the whole remaining part of the temperatures...
analyzed.

For C/O=0.7 the system encounter just steady combustion regimes, but also here the temperature increase increases reaches a maximum and then drops towards the isothermal line.

This behavior has already been detected in the previous experiments on the same system and it was named “temperature drop”.

In figure 4.18 it is shown the bifurcation diagram relative to a system CH₄-H₂/O₂/N₂ with an hydrogen percentage equal to 0.25%.

For C/O=0.1 the working temperature is relatively close to the isothermal line for very low inlet temperatures, in fact the temperature increment is of about 20K, then increasing the continuous parameter the system starts oscillating and the temperature increment is relatively small. From Tₐ of about 1185 K the system evolves trough a stable regime but the temperature increment is of about 15K.

![Bifurcation diagram for the system CH₄-H₂/O₂/N₂ for an hydrogen global percentage equal to 0.25%](image)

Figure 4.18  Bifurcation diagram for the system CH₄-H₂/O₂/N₂ for an hydrogen global percentage equal to 0.25%.

For C/O=0.4 the reactor temperature increases as much the inlet temperature is
increased, but it starts oscillating for an inlet temperature equal to 1100K. The amplitude of oscillations decreases increasing the inlet temperature but the average temperature decreases. In this case the system reaches the highest working temperatures. For $T_{in}=1225K$ the reactor temperature is just 15K higher than the inlet one. Increasing the inlet temperature the systems does not experiments higher temperature but the temperature increment becomes nearly constant.

It is evident that increasing the C/O feed ratio the inlet temperature range for which the dynamic region is established becomes smaller.

For C/O=0.7 the reactor temperature increase increasing the inlet temperature, then it reaches a maximum. Afterwards it decreases and for values of the continuous parameter higher than 1225K it becomes just 50K higher than the inlet temperature.

![Figure 4.19 Bifurcation diagram for the system CH$_4$-H$_2$O$_2$/N$_2$ for an hydrogen global percentage equal to 0.5%](image)

The same considerations apply to the case C/O=1. In this case the working temperatures are very close to the temperatures of the system with a C/O feed ratio equal to
0.7 but for tin higher than 1050K they become lower. Again the temperature, after a maximum value, drops towards the isothermal line. This behavior has already been recognized in the experimental tests realized on the methane oxidation in Mild combustion conditions.

Figure 4.19 shows the bifurcation diagram for an inlet hydrogen concentration equal to 0.5%.

The reactor temperature has been plotted as function of the inlet temperature on curves parametric in the C/O feed ratio. The C/O feed ratios analyzed are again 1, 0.7, 0.4 and 0.1. For C/O=0.1 and inlet temperature lower than 1025K the system evolves trough a steady combustion. The temperature increment is of about 20K. Then the system starts oscillating and the temperature amplitude is very small. For T_{in} higher than 1150K the system evolves trough a steady combustion but the difference between the working and inlet temperature (ΔT) is again 11K.

![Bifurcation diagram](image)

**Figure 4.20** Bifurcation diagram for the system CH₄-H₂/O₂/N₂ for an hydrogen global percentage equal to 0.75%.

For C/O=0.4 the system evolves trough a steady regime and the reactor temperature
increases by increasing the inlet temperature until about 1050K. For inlet temperature comprised between 1050K and 1200K, the system goes through a dynamic regime. For $T_{in}>1200K$ the temperature increment is very small, it is about 15K.

Increasing the C/O feed ratio up to 0.7, it is possible to see that the system does not evolve through oscillating conditions, and the inlet temperature increases increasing $T_{in}$, reaches a maximum and then it drops towards the isothermal line.

The same considerations apply for the systems with an hydrogen percentage equal to 7.5% and 0.9% respectively reported in figure 4.20 and 4.21.

![Figure 4.21 Bifurcation diagram for the system CH$_4$-H$_2$O$_2$/N$_2$ for an hydrogen global percentage equal to 0.9%](image)

**Effect of the nature of Diluent: Steam Water**

The behavior of the system CH$_4$/O$_2$/N$_2$ in Jet Stirred Flow Reactor (JSFR) has been studied as function of the main parameters such as the residence time, the dilution degree, the mixture composition and temperature.

In the previous studies the system has been diluted with nitrogen since the necessity
to work with an inert species. In such a way, the oxidation of methane, under non-standard conditions (high inlet temperature and the high dilution degree), has been studied in absence of species that could have altered the evolution of the oxidation process. This study has pointed out that under Mild conditions the CH₄/O₂/N₂ system can give rise to a dynamic behaviors that have been widely discussed in the previous paragraphs. Such new phenomenology should be avoided in a combustion chamber since oscillations can be responsible of mechanical damage to turbines and can lower the efficiency of combustion process.

With this aim it is interesting to value the effect of the diluent on the dynamic behavior experimentally detected.

From a practical point of view there are many species that could be used as diluent, for instance, steam water and carbon dioxide. Their importance comes from the possibility of recycling the exhausted gases from a combustion chamber in order to pre-heat and dilute the reactants in a system working in Mild conditions. The exhausted gases are mainly composed by steam water and CO₂. Hence effectively in a real plant they represent the diluent species.

Steam water and carbon dioxide can have a thermal effect and a chemical effect on the evolution of the methane oxidation process. The thermal effect is due to the different heat capacities whereas the chemical effect is due to the possible breakdown of these two species that would result in an enhancement of radical species.

Hence in this paragraph the oxidation process of system CH₄/O₂ under Mild condition has been characterized as function of the nature of the diluent. In particular the system has been diluted with nitrogen and steam water.
Experimental Ignition Map

The effect of the nature of the diluent has been experimentally tested in the Jet Stirred Flow Reactor described in the chapter III.

The working parameters are resumed in the tab 4.22. The residence time is 0.5 sec, the temperature range is comprised between 1000K and 1250K, the C/O feed ratio has been changed from value very close to zero up to 1.2. In these experimental tests nitrogen and steam water dilute the system up to 90%. In particular steam water has been added in percentage equal to 10% and 20% of the overall dilution degree.

<table>
<thead>
<tr>
<th>Reactor</th>
<th>JSFR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Residence Time</td>
<td>0.5 sec</td>
</tr>
<tr>
<td>Feed Ratio (C/O)</td>
<td>0.05-1.2</td>
</tr>
<tr>
<td>Dilution degree</td>
<td>90%</td>
</tr>
<tr>
<td>Steam water</td>
<td>10%-20%</td>
</tr>
<tr>
<td>Pressure</td>
<td>1.17 atm</td>
</tr>
<tr>
<td>Temperature</td>
<td>1000 K-1250 K</td>
</tr>
</tbody>
</table>

*Tab. 4.22 Chosen working conditions for Mild Combustion studies in systems diluted with steam water.*

The experimental study performed on methane Mild oxidation has focused on the identification of the system behavior as function of the inlet temperature ($T_{in}$), C/O ratio and dilution levels. During the set of experiments, the temporal temperature profiles, recorded by means of a facility well described in chapter III, suggested that the oxidation of methane in conditions typical of Mild processes, gives rise to a complex dynamic behavior and the attention has been focused mainly on the characterization of this new phenomenology.
The first approach to this problem was the partition of the working conditions for which the system evolves through stable combustion or oscillating regimes.

Since the residence time $\tau$, the pressure and the dilution level have been fixed, the only parameters to set up are the inlet temperature and the carbon-oxygen feed ratio C/O. In order to have a descriptive indication on possible stable or periodic states, the results were resumed in bifurcation maps of the system by using $T_{in}$ and C/O ratio as continuation parameters for the two dilution levels considered. Any point of the $T_{in}$,C/O plane represents an inlet condition, and it has been classified on the basis of the system stability.

The systems that have been analyzed are CH$_4$/O$_2$/N$_2$, CH$_4$/O$_2$/N$_2$-H$_2$O(10%) and CH$_4$/O$_2$/N$_2$-H$_2$O(20%).

![Figure 4.23](image)

**Figure 4.23** $T_{in}$-C/O bifurcation map obtained for a dilution level of 90%, $\tau$=0.5 sec for the system CH$_4$/O$_2$/N$_2$.

The experimental tests for the system CH$_4$/O$_2$/N$_2$ have been repeated in order to confirm the first results and also to properly compare the results obtained for the other two
systems. In fact the system is very sensitive to uncontrollable parameters, such as the environmental temperature, that can affect the process in terms of heat exchange, and slightly change the evolution of the oxidation.

![Figure 4.24](image)

**Figure 4.24** Bifurcation diagrams for several C/O feed ratios for the system CH$_4$/O$_2$/N$_2$.

The experimental bifurcation map obtained for the system CH$_4$/O$_2$/N$_2$ is reported in Figure 4.23. The main features of the dynamic behavior have been found out again even if the extension of the dynamic region is slightly different in comparison with the maps obtained in the other experimental tests. Anyway these slight changes in the extension of the dynamic region were expected.
The ignition map shows that the widest region corresponds to stable combustion where a single step ignition leads the system to a steady working temperature.

The steady combustion is the only phenomenology occurring in the region of richest C/O ratios down to 0.6 in the whole temperature range analyzed. At lower C/O ratios and $T_{in}$ higher than 1040 K a region where dynamic behavior occurs is also recognized. For C/O=0.6 temperature oscillations occur in a range of 50K, from $T_{in.} = 1150$K up to 1200K. The oscillating temperature region enlarges by decreasing the C/O ratio thus covering the temperature range between 1040K up to 1250 K in correspondence of the leanest C/O ratios.

Furthermore the same oscillation typologies, defined in the first experimental tests, have been recognized. In this case the temperature profiles are not reported since the attention has been focused on the effect of steam dilution on the extension of the dynamic region.

Figure 4.24 reports the temperature of the reactor ($T_{reactor}$) as function of the inlet temperatures ($T_{in}$) for several rich mixtures, respectively characterized by a C/O feed ratio equal to 0.7, 0.8,1. For all these mixtures it is possible to recognize the same trend of the $T_{reactor}$ as function of $T_{in}$.

The working temperature is close to the isothermal line (dashed line) for low values of the $T_{in}$ in the analyzed temperature range. As the inlet temperature is increased $T_{reactor}$ slowly increases, reaches a maximum and then decreases towards the isothermal line.

The results for the systems CH$_4$/O$_2$/N$_2$-H$_2$O(10%) and CH$_4$/O$_2$/N$_2$-H$_2$O(20%) have been resumed in ignition maps following the same methodical approach used for the system CH$_4$/O$_2$/N$_2$.

Figure 4.25 shows the ignition maps for the former system. Also in this case it is possible to see that for the most of the analyzed inlet conditions the system evolves trough
a steady combustion. In fact for rich mixtures, characterized by a C/O feed ratio higher than 0.6, temperature profiles show an sudden jump of reactor temperature that then goes down to the steady value. For temperature higher than 1040K and C/O feed ratio lower than 0.6 it is possible to identify oscillations.

![Diagram](image)

**Figure 4.25** $T_{inlet}$-C/O bifurcation map obtained for a dilution level of 90%, $\tau=0.5$ sec for the system CH$_4$/O$_2$/N$_2$-H$_2$O(10%)

For C/O=0.6 the dynamic behavior has been detected in a relatively small temperature range that goes from 1150 K to 1180K. Then for C/O=0.4 the temperature range enlarges and goes from 1120K to the highest exploited temperature values (1250K). Decreasing the C/O feed ratio the region enlarges and cover almost all the temperature range considered for the experiments. For very lean mixtures (C/O < 0.05), only stable combustion is detectable.

Also for the system CH$_4$/O$_2$/N$_2$-H$_2$O(10%) the reactor temperature has been plotted versus the inlet temperature for several C/O feed ratio. The bifurcation diagrams are
reported in figure 4.26. It is possible to recognize the same trend discussed for the system CH₄/O₂/N₂.

As the inlet temperature increases the $T_{\text{reactor}}$ increases, reaches a maximum, and the goes towards the isothermal line. This behavior has been named “temperature drop” and will be discussed in Chapter V. In this case it is also possible to see that, for very high values of the inlet temperature, the difference between the $T_{\text{reactor}}$ and $T_{\text{in}}$ is relatively small and almost constant. Such value is equal to about 30K.

![Bifurcation diagrams for several C/O feed ratios for the system CH₄/O₂/N₂-H₂O(10%).](image)

**Figure 4.26** Bifurcation diagrams for several C/O feed ratios for the system CH₄/O₂/N₂-H₂O(10%).
For the system CH$_4$/O$_2$/N$_2$-H$_2$O(20%) the ignition map is reported in figure 4.27. Also in this case for mixtures characterized by a C/O feed ratio higher than 0.6 in the whole analyzed temperature range methane oxidation occurs in steady conditions. For C/O lower than 0.6 and $T_{in}$ higher than 1040K experimentally temperature oscillations can be detected. Once again, the dynamic region interests a small temperature range (1150K-1180K) for values of the parameter C/O comprised between 0.4 and 0.6. For lower C/O range the dynamic region enlarges and interests almost the whole temperature range considered during the experimental tests.

![Figure 4.27](image)

**Figure 4.27**  $T_{in}$-C/O bifurcation map obtained for a dilution level of 90%, $\tau=0.5$ sec for the system CH$_4$/O$_2$/N$_2$-H$_2$O(20%).

The bifurcations diagrams are reported in figure 4.28. Reactor temperature is plotted as function of the $T_{in}$ in for several C/O feed ratios. The same trend, described before for the system with a lower steam water percentage, is here recognizable.

For $T_{in}=1225K$ and $T_{in}=1250K$, the difference between the $T_{reactor}$ and $T_{in}$ ($\Delta T$)
becomes relatively small and the $\Delta T$ reaches a constant value for any analyzed C/O considered in the paragraph.

Figure 4.28  $T_{\text{inlet}}$-C/O bifurcation map obtained for a dilution level of 90%, $\tau=0.5$ sec for the system $\text{CH}_4/O_2/N_2-H_2O(20\%)$.

**Simplified configuration for fluid-dynamic tests**

After the design of the tubular reactor, the attention has been focused on the mixing devise. As discussed in chapter III, the configuration chosen to mix reactants forecasts fuel is injected in the main duct trough nozzles disposed on the perimeter of a duct cross
The efficiency of the mixing section has been evaluated by means of experimental characterization of fluid-dynamic behavior of a simplified facility working at ambient temperature.

Obviously the geometry of this facility is very similar to the plug flow reactor designed for the study of the oxidation process in Mild Condition. The system is shown in fig. 4.29.

Figure 4.29  Simplified configuration for fluid-dynamic tests.

The facility presents an inlet part, a quartz tube and an outlet part. The first part consists in a flanged tube that is joint to the mixing section by means of bolts. The main flow is fed from the bottom of the first part of the facility while the lateral flow is injected from round, equally spaced tubes displaced on the perimeter of the first section at the end of the first section. The inlet section has an inner diameter equal to 1.4 cm. A convergent allows reducing this dimension to 1 cm to join the mixing section to the quartz tube. The convergent has a linear geometry and its slope is 26°. The mixing section is displaced at an axial distance equal to the diameter of the duct to the convergent. The mixing device has
10 tubes with a inner diameter equal to 0.05 mm. The inner dimension of tubes can be changed in order to perform the study of the mixing efficiency as function of the dimension of holes. The geometry of the mixing part slightly differs from the real reactor mixing device configuration since the latter one will have 6 holes with an inner diameter equal to 0.80mm. The simplified facility has been built before the numerical studies on the mixing efficiency, hence it has been built taking into account just the literature suggestions (Holdeman et al. 1996). Two distributors insure an equal division of the lateral flows among the 10 tubes. Each of the two distributors feeds 5 tubes.

The main flow mix with the lateral jest and enters the quartz tube. Quartz allows having a facility optically accessible. Furthermore the outlet part is provided of a quartz window in order to perform optical diagnostic analysis. Anyway this discussion is remanded to next section.

The last part of the facility is provided of four outlets in order split the main flow in four flows and have a low velocity. In this way the pressure in the system will be atmospheric. As matter of fact the flow rates used in the system are very high. Hence there is the necessity of avoiding to work in sonic condition, which would lead to an increase in pressure.

In this facility fluorescence measurements will be performed to test the efficiency of the mixing device. In particular acetone is used as a tracer in a helium flow and it is fed from the lateral injectors inside the mixing section where it blend with air.

The use of acetone has widely conditioned the choice of materials. In fact the facility has been realized in Teflon, while rigid tubes are in stainless steel and flexible tubes, such as the ones that link the distributors to injectors, are in Teflon.

Fluorescence measurements

In order to test the reactor configuration from the fluid-dynamic point of view the
model of the alumina reactor, able to work at ambient temperature has been used. An optical diagnostic system for fluorescence measurements in different sections of reactor has been set up. In particular, the second harmonic of a Nd:YAG laser ($\lambda_{\text{exc}}=266$ nm) has been used in order to excite the acetone injected as tracer along with helium in the lateral jets in order to study the their mixing degree with the main flow.

![Diagram](image)

*Figure 4.30  Experimental set-up for fluorescence measurements*

The optical diagnostic used was a bi-dimensional implementation of a simple 90° LIF collection scheme. To this aim the laser beam was shaped as a thin (200 µm) sheet by using a cylindrical telescope. The laser sheet (0.7 cm tall) crosses the reactor at the chosen section. The scattered light was filtered by means of a band-pass filter (350-450 nm). The resulting image is collected by means of an ICCD camera sensitive in this spectral range. For each test run 200 images were collected in the same experimental condition and added in order to smooth away laser pulses energy oscillation and to increase the signal-to-noise ratio of measured spectra.

Acetone is often used as tracer in combustion device in order to study the species distribution in the reaction zones. The electronic transition that characterizes spectra of carbonyl compounds is generally known as $n \rightarrow \pi^*$. It is due to one of the two non-bonding electrons of the oxygen atom, which is excited in the antibonding orbital ($\pi^*$)
of C=O group. This transition characterizes each carbonyl compound independently on the molecule to which the carbonyl group belongs. The nature of the atoms bonded with >C=O group can partially modify the spectrum of \( n \rightarrow \pi^* \). Generally this results in the appearance of additional spectral structures, observable along with the one typical of \( n \rightarrow \pi^* \).

Figure 4.31  Spectroscopic behavior of carbonyl compounds.

The luminous signal related to this electronic transition has been summarized for different ketones in Figure 4.31a, b and c (de Joannon et al, 2001). In Fig. 4.31a the absorption spectrum of a water solution of acetone has been reported as representative of absorption characteristics of aliphatic ketones. It covers the wavelength region between 210 and 310 nm with a maximum at about 270 nm. Similar behavior has been reported in literature (Hansen and Lee, 1975/2) for heavier ketones too.
The fluorescence spectrum characteristic of \( n \rightarrow \pi^* \) transition generally covers a wavelength region between 350 and 550 nm with a maximum at about 420 nm, such as shown by the fluorescence spectra relative to acetone and pentanone (Hansen and Lee, 1975/2) reproduced in Figure 4.31b. This behavior has been confirmed by the spectrum collected in the present work from a water solution of acetone, reported in Figure 4.31c.

The experiments aim to understand the dependence of the mixing degree on the parameter jet to stream mass-flow ratio \( J = \rho_j v j^2 / \rho_s v s^2 \). The system is composed by air and helium. Helium gurgles in a bath of acetone and the outlet mass flow rate is composed by helium and acetone that enter the main duct from the lateral injections and mix with the main flow.

This noble gas has been chosen as lateral flow since we have tried to reproduce the same values of \( J \) there would be the in the real system while keeping equal the velocities. This constraint comes from the same system the density of the main flow is very low since the high inlet temperatures. On the contrary the simplified facility works at environmental temperatures hence the ratio between the densities of the main and the lateral flow rate is much higher from the one of the real configuration. To reduce this difference the molecular weight of the injected flow has been chosen as small as possible since the choice of the air as main flow is due to economical reasons.

Anyway in the first set of measurements the experiments have been realized changing the helium volumetric flow rate, hence its velocity, while keeping constant the air volumetric flow rate.

Two-dimensional fluorescence images of the half section of the reactor collected at 1mm, 10mm and 20mm from the mixer exit for different \( J \) have been collected and discussed.
Experimental tests realized in the simplified configuration for the study of the fluid-dynamic

The aim of the experiments is to understand the dependence of the mixing degree on the parameters typical of the jet in cross flow configuration such as the momentum of the jet to main stream ratio $J$, the number ($n$) and the dimension of holes.

The system is composed by air and helium. Helium gurgles in a bath of acetone and the outlet mass flow rate is composed by helium and acetone that enter the main duct from the lateral injections and mix with the main flow.

This noble gas has been chosen as lateral flow since we have tried to reproduce the same values of $J$ there would be the in the real system while keeping equal the velocities. This constraint comes from the same system the density of the main flow is very low since the high inlet temperatures. On the contrary the simplified facility works at environmental temperatures hence the ratio between the densities of the main and the lateral flow rate is much higher from the one of the real configuration. To reduce this difference the molecular weight of the injected flow has been chosen as small as possible since the choice of the air as main flow is due to economical reasons.

In figure 4.30 it is represented a two-dimensional sketch of the simplified configuration that has been used in order to characterize the mixing of this geometry.

The sketch shows the first section with an inner diameter equal to 14mm, than the linear convergent with a slope of 26°, and then the third section with a inner diameter of 10mm. In particular this sketch shows 6 injectors equally spaced along the perimeter of the first section at an axial distance from the convergent equal to 7mm.

For all the configurations that have been analyzed in this chapter the origin of the system is located at the end of the convergent on the axis of the cylindrical duct. Hence the injection plane is at an axial coordinate equal to $x=-11$mm.
The geometric parameters that have been investigated are: the number of holes (n), the diameter of holes (d), the protrusion of the injectors inside the duct (p).

For any analysis the range of the value J is sufficiently wide in order to analyze the mixing in a under-penetration and over-penetration conditions. The value of J is changed varying the helium flow rate. The main flow rate is fixed to 25000 Nl/h, in such a way to have a velocity in the first section equal to 45 m/s, while the lateral flow rate, composed by helium and acetone, changes from 600NI/h to 3900NI/h.

![Figure 4.30](image) Sketch of the simplified configuration for the fluid-dynamic study.

The amount of the acetone in the helium flow may change as function of the experimental condition. Some calculations have been performed in order to estimate the concentration of acetone in the reactor once it is mixed with the main flow. Fig.4.31 shows the volumetric acetone concentration as function of the helium flow rate. It changes from $6 \times 10^{-6}$ a $1 \times 10^{-5}$ but it seems to be almost constant from a helium flow rate higher than 1000 NI/h.

The results are important for the analyses of the fluorescence measurements that have been realized on the simplified configuration for the study of the mixing degree.

For any considered geometry, it has been calculated the Standard Deviation of the fluorescence intensity profiles along a diameter of the duct. This statistic tool gives an indication on the uniformity of fluorescence signal along the reactor diameter.
The lower the StD is, the more uniform the acetone concentration is. Hereafter the standard deviation StD or mixing dis-uniformity are used with the equivalent meaning. The StD has been calculated as function of the parameter J at three axial distance from the convergent respectively equal to 1mm, 1cm e 2cm.

Figure 4.31 Acetone volumetric concentration inside the third section of the simplified set-up as function of the helium flow rate (Nl/h).

The standard deviation is calculated by means this formula:

\[ StD = \sqrt{\frac{\sum_{i=1}^{N} (x_i - \bar{x})^2}{N}} \]

where \( x_i \) is the normalized pixel intensity, \( \bar{x} \) the mean of data and \( N \) the number of pixels of the fluorescence profile.

The literature (Holdeman, 1992) suggests that for values of the StD lower than 0.1 the system has reached a very good mixing and that for StD lower than 0.2 the mixing can be considered acceptable.

In this section it has just be presented the experimental measurements relative to the system with 10 injectors located on the wall of the cylindrical duct. Hence the images
collected during the experimental tests, the radial profile of the fluorescence intensity and the standard deviation analyses has been reported in order to show the approach to the study of the mixing in the jet in cross-flow configuration. In the other considered cases it is just reported the standard deviation analysis of the fluorescence intensity. All the images and intensity profiles relative to these other cases are reported in the appendix.

**10 injectors located on the wall of the cylindrical duct**

The first analyzed geometry presents 10 injectors with an inner diameter equal to 0.5 mm. They are equally displaced on the perimeter of the cylindrical duct at 36° of distance from each other.

In this case the optimal value of the momentum of the jet to mainstream ratio $J$ according to Holdeman equations is equal to 32 ($J_{\text{Hopt.}}$). The numerical simulations have been run for a wide range of $J$, from 2 to 64, in such a way it has been possible to analyzing the mixing in a wide range of conditions. If fact the analyses have been performed for $J$ values lower and higher than the $J_{\text{Hopt.}}$.

The bi-dimensional implementation of the fluorescence measurements realized for this configuration is presented in figure 4.32. The acetone distribution and concentration inside the reactor is represented by the fluorescence intensity of pixels of images collected by means of the optical facility for the fluorescence measurements. In figure 4.32, fluorescence intensity is represented by means of a linear false color scale reported in the figure. The scale has been subdivided into sixteen different levels, hence colors, and the pixel intensity goes from zero to 1800. The white color corresponds to fluorescence intensity equal to zero; hence it indicates the complete absence of acetone. The fluorescence intensity has been normalized respect to the highest intensity value of all the images collected for the several configurations considered, in order to compare all the experimental results among them.
The images have been collected for three different cross sections located in the plane x=0 and at an axial distance equal to x=1mm, x=1cm and x=2cm. In the figure it is also reported the laser beam that hits the cylindrical duct.

The figure allows the analysis of the acetone distribution as function of the parameter J, once the axial position has been fixed, as well as the analysis of the acetone distribution as function of the axial position if the value of the parameter J has been fixed.

At an axial position x=1mm, for any J value there is a internal zone where there is not any fluorescence intensity signal. This region tends to diminish as the parameter J increases. For J>40 it almost disappears but in any analyzed case, the acetone tends to accumulate in the near-wall region.

At an axial distance fro the convergent equal to 1 cm the fluorescence intensity signal present the same trend as function of the parameter J.

For J=2 and J=6 there is an internal region with no acetone, but for J=8 a small concentration of acetone is detectable also in this region, even if the fluorescence intensity is very low.
Figure 4.32  Fluorescence Intensity images as function of the parameter $J$ in curves parametric on the axial position for the configuration with 10 holes.
positioned on the wall of the cylindrical duct.

From $J=12$ the central zone is invested increasingly more by acetone until $J=64$, when the acetone cover almost completely and uniformly the whole section except for a low internal core.

For the last considered axial position, it is possible to note that the internal core with no acetone persists from $J=2$ to $J=4$, but for $J=6$ the acetone spread out on all the cross section even if the distribution is not uniform.

The fluorescence signal becomes increasingly more uniform and from $J=50$ to $J=64$ the signal suggests that the jet in cross flow configuration ensures a good mixing of the tracer. The other way to analyze the images is to consider the fluorescence intensity as function of the axial position for a fixed $J$ value.

In general the mixing uniformity improves with the axial position. For $J=2$ and $J=4$, at $x=1\text{mm}$ the intensity signal is detected just in the near-wall region. For $x=1\text{cm}$ and $x=2\text{cm}$ the situation does not improve so much but the central region with no acetone diminishes significantly. The same considerations apply for $J=6$ but in this case for $x=2\text{cm}$ the acetone is present with a relative low concentration also in the center of the cross section. The same situation is proposed again for the sequence of images collected for $J=17$ but at $x=2\text{cm}$ the acetone spreads on the whole area with a significant acetone concentration in the center of the section.

For $J=32$ also at $x=1\text{cm}$ the distribution of acetone begins to be significant in the center region.

For $J=50$ and $J=64$ and an axial distance equal to 1mm the internal segregated area is very narrow. It diminishes at $x=1\text{cm}$ and it completely disappears at $x=2\text{cm}$ and this indicates a very good mixing.

In fig.4.33 the fluorescence intensity signal is plotted along a diameter of the duct at
the known axial distances for any J value analyzed.

Figure 4.33  Fluorescence Intensity signal profiles as function of the parameter J in curves parametric on the axial position for the configuration with 10 holes positioned on the wall of the cylindrical duct.
In these figures the fluorescence intensity has been normalized respect to its mean value for each condition. In such a way the profiles have been made independent on the acetone concentration and they can be reasonably compared among them.

The same analyses and considerations can be realized taking into account the normalized fluorescence profiles reported in figure 4.33. In this case the uniformity of acetone distribution is reached when profiles becomes flat.

For \( J=2 \) the profiles indicate that the tracer accumulates in the lateral area and that there is no acetone for a wide portion of the diameter. In this case the jets under-penetrate inside the main duct and the acetone remains segregated in the near-wall region. \( J \) represents the best condition when it is equal to 64 where the profiles are sufficiently flat for all the axial positions.

In fig.4.34 the non-uniformity of the mixing, calculated on the basis of the standard deviation, is presented as function of the parameter \( J \) on curves parametric on the axial position. The StD has been calculated considering the normalized pixel fluorescence intensity values presented in fig. 4.33.

The higher the momentum of the jet to mainstream ratio, the lower the StD is for any axial distance. As matter of fact, the StD decreases monotonically and slowly as the parameter \( J \) is increased. At \( x=1\text{mm} \) the StD goes from 1.3 to 0.25, while for \( x=1\text{cm} \) it goes from values very close to 1 to 0.11, and for \( x=2\text{cm} \) it interests \( J \) values from 0.6 to 0.06.

The best uniformity of mixing is reached at \( x=1\text{cm} \) and \( x=2\text{cm} \) for values of \( J \) respectively equal to 64 and 50. The StD becomes lower than 0.2 for \( J=50 \) at \( x=1\text{cm} \) and for \( J=23 \) at \( x=2\text{cm} \). For \( x=1\text{mm} \) the lowest StD value is reached for \( J=64 \) but it is equal to 0.28.

Therefore it is possible to state that at \( x=1\text{mm} \) the discussed configuration does not provide for a good distribution of the acetone. Furthermore it is needed a very high value
of the parameter \( J \) to have a good mixing of the tracer.

![Figure 4.34](image)

**Figure 4.34**  Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter \( J \) on curves parametric in the axial position.

6 injectors with \( d=0.9 \) mm located on the wall of the cylindrical duct

In fig.4.35 the non-uniformity of the mixing, calculated on the basis of the standard deviation, is presented as function of the parameter \( J \) on curves parametric on the axial position for the system with 6 injectors with \( d=0.9 \) mm located on the wall of the cylindrical duct The \( StD \) has been calculated considering the normalized pixel fluorescence intensity values reported in appendix for this case.

The higher the momentum of the jet to mainstream ratio, the lower the \( StD \) is for any axial distance. As matter of fact, the \( StD \) decreases monotonically as the parameter \( J \) is increased. For \( x=2\text{cm} \) it mainly diminishes from \( J=0.5 \) to \( J=6 \), than for all the axial distances it seems to reach a constant value. At \( x=1\text{mm} \) the \( StD \) goes from 0.9 to 0.21, while for \( x=1\text{cm} \) it goes from values very close to 78 to 0.16, and for \( x=2\text{cm} \) it interests \( J \) values from 0.68 to 0.14.

The \( StD \) is never lower than 0.1 but for \( x=2\text{cm} \) is lower than 0.2 for \( J>6 \). For \( x=1\text{cm} \) it is lower than 0.2 for \( J>14 \) while at \( x=1\text{mm} \) it always higher than this value.
Figure 4.35  Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position.

6 injectors with $d=0.8$ mm located on the wall of the cylindrical duct

In fig. 4.36 the non-uniformity of mixing is plotted as function of the $J$ value at the three axial distance $x=1$mm, $x=1$cm and $x=2$cm. The standard deviation is calculated on the basis of the normalized fluorescence profile reported in figure 5.3.8.

Figure 4.36  Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position.

For $x=1$cm the $StD$ becomes lower than 0.2 for $J=16$, while for $x=2$cm for $J=7$. For
this axial distance it reaches the minimum value for \( J=11 \) and than it is constant for higher value of \( J \).

For \( x=1\text{mm} \) the lowest value is 0.26 and it competes to the highest value of \( J \) here analyzed.

6 injectors with \( d=0.9 \text{ mm} \) protruded 1mm inside the cylindrical duct

In figure 4.37 the Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter \( J \) on curves parametric in the axial position are reported for the system with 6 injectors with \( d=0.9 \text{ mm} \) protruded 1mm inside the cylindrical duct

![Figure 4.37](image)

**Figure 4.37** Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter \( J \) on curves parametric in the axial position.

In the case of \( x=1\text{mm} \), the Standard deviation decreases monotonically but in at \( x=1\text{cm} \) and \( x=2\text{cm} \) it presents a minimum value respectively for \( J=6 \) and \( J=3 \). As matter of fact, the non-uniformity of the mixing increases after these values increase and the \( StD \) is lower than 0.2 just for \( J=3 \).

6 injectors with \( d=0.8 \text{ mm} \) protruded 1mm inside the cylindrical duct

In fig.4.38 it is shown the non-uniformity, hence the standard deviation of the
fluorescence signal along a diameter of the duct, in the cross section located at \(x=1\text{mm, 1cm and 2cm}\). For \(x=1\text{mm}\) the \(StD\) decreases monotonically. It goes from 0.78 to 0.27. It firstly diminishes abruptly from \(J=1\) to \(J=11\) and than it almost reaches a constant value.

For \(x=1\text{cm}\) and \(x=2\text{cm}\) the standard deviation first decreases and than slowly increases. In particular at \(x=1\text{cm}\) the minimum \(StD\) value is reached for \(J=11\), and at \(x=2\text{cm}\) for \(J=3\). For \(x=1\text{cm}\) the \(StD\) goes from 0.55 to 0.27, and for \(x=2\text{cm}\) it is 0.323 for \(J=1\) and 0.27 for \(J=34\).

\[Figure 4.38\] Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter \(J\) on curves parametric in the axial position.

From \(J=11\) the \(StD\) values at \(x=1\text{cm}\) and \(x=2\text{cm}\) are very similar at any \(J\) value and for \(J=34\) the system presents always the same non-uniformity distribution degree.

The system reaches an acceptable mixing for \(J\) comprised between 2 and 11 for \(x=2\text{cm}\), while in the cross section located at \(x=1\text{cm}\) just for \(J=11\), hence just in these conditions the \(StD\) is lower that 0.2.
Chapter V

Numerical Results

Numerical Ignition Maps with the ChemKin Software

The experimental results reported in the previous chapter underlined the existence of a complex dynamic phenomenology related to the oxidation of the methane in condition typical of Mild Combustion. The availability of feasible methane oxidation kinetic models suggested the possibility of studying the dynamical behavior experimentally identified also by means of a numerical approach. Such a study has a double aim: the former concerns the possibility of verifying numerically the existence of the dynamic phenomenology found out during the experiments; the latter is the comprehension of the methane oxidation kinetic pathways during the oscillating regimes. As described in the chapter III, the ChemKin package software and its application Aurora have been used to perform this analysis. Aurora allows simulating the behavior of a perfect stirred flow reactor in transient conditions.

For a first analysis, two different models were used for simulating the behavior of the CH₄/O₂/N₂ system in Mild condition in a stirred flow reactor: the model by J. Warnatz and V. Karbach (1997) and the model by F. Battin-Leclerc and P. Barbe (1997) from the Nancy research group. Hereafter, they will be respectively named “Warnatz” and “Nancy” model.

The “Warnatz” model is composed by 34 chemical species and 164 reactions, the other one by 64 chemical species and 439 elementary reactions. The different number of reactions is due to the higher number of reactions involved in the recombination channel of the methane kinetic mechanism. In fact the ”Nancy” model simulates the kinetic behavior of methane until the formation n-butane while the “Warnatz” model until ethane formation.
For both the kinetic models used the simulations were run in the same initial conditions considered during the experimental tests. Hence the residence time \( \tau \) is 0.5 sec, the mixture is diluted with nitrogen up to 90%.

The fig.5.1 shows the ignition map for the methane kinetic mechanism named “Warnatz”.

The mechanism forecasts a zone where oscillations have been detected between values of the C/O feed ratio comprised between 0.05 and 0.4 and temperatures ranging from 1050K to 1275K. The extension of the region, where oscillations occur, extends for C/O value equal to 0.25 in the direction of an increase of the inlet temperature.

By using the “Warnatz” model it could be possible to well identify different oscillation zones on the basis of temporal temperature profile characteristics. In particular, the oscillation region pointed out in this case can be divided in three zones.

![Figure 5.1](image)

**Figure 5.1** Experimental and numerical map of stability obtained for methane oxidation in diluted conditions.

A first zone (a), at the boundary of the “Warnatz” dynamic region, is associated to
dumped oscillations, which seem to appear during the transitions between the stable and the oscillatory regimes. In the second (b) and the third (c) zones respectively cusp-shape and triangular-shape oscillations were found.

Fig. 5.2 shows a temporal temperature profile obtained for C/O=0.3 and for an inlet temperature equal to 1073K. The system evolves through a dumped periodic oscillation.

![Figure 5.2 Dumped oscillation obtained for C/O=0.3 and T_{inlet}= 1073K.](image)

The region associated to the dumped oscillation in the C/O-T_{inlet} plane mainly extends for C/O feed ratios higher than 0.3 and they interest all the temperature range where oscillations have been numerically detected. Furthermore, this region evidently is a transition zone since it extends between the stable combustion region and the oscillating region.

For T_{inlet} equal to 1073K and C/O= 0.2 the system evolves, using a terminology applied for the description of the different temperature profiles in the paragraph, through a “cusp” oscillation.

This profile is reported in fig.5.3. It underlines an important feature of this kind of oscillations, in fact they show the same values of frequency but not the same amplitude.
Figure 5.3  
*Cusp oscillation obtained for C/O=0.2 and T_{inlet}= 1073K.*

The region where “cusp” oscillations have been numerically identified mainly extends from C/O feed ratio that range form 0.3 to 0.4 and for temperatures comprised between 1050K and 1225K, furthermore for C/O comprised between 0.1 and 0.3 and temperatures between 1048K and 1175K.

Finally the region relative to triangular oscillations extends for C/O values comprised between 0.05 and 0.25. The figure 6.4 shows the typical temporal profiles relative to triangular oscillations. It has been detected for C/O=0.2 and T=1173K.

Figure 5.4  
*Small amplitude triangular oscillations obtained for C/O=0.2 and T_{inlet}= 1173K.*

In the numerical ignition map the region that competes to the dynamic behavior extends on a narrower area in comparison with the one experimentally detected.

Hence the model is able to reproduce the oscillatory behavior but does not reproduce
all the kind of oscillations experimentally identified.

Further analyses have been realized using the “Nancy” model. The results have been resumed in the ignition map reported in fig.5.5. Also this model is able to reproduce the dynamic behavior experimentally detected. The oscillatory behavior extends from 1025K to 1275 K and for C/O feed ratios comprised between values very close to zero and 0.4.

Also in this case the extension of the region were oscillations occur is underestimated in comparison with the region experimentally detected.

Both the models are able to reproduce “dumped”, “cusp” and “triangular” oscillations. They can also predict “double” oscillations. They have been detected for stochiometric fuel-comburent C/O ratio and for very high temperatures. Anyway the region relative to such oscillations is very narrow and it was not possible to identify a significant region in the ignition map.

![Figure 5.5](image)

**Figure 5.5**  Numerical map of stability obtained for methane oxidation in diluted conditions.

A comparison between the models has not been realized since the aim of the
numerical analyses was to see whether kinetic models available in literature were able to reproduce the new phenomenology identified during the experimental tests.

Hence a detailed analysis of the difference between the two models has not been realized.

**Effect of the heat transfer coefficient**

Another parameter that can affect the insurgence and the features of the dynamic behavior is the global heat transfer coefficient. Hence a numerical analysis has been run in order to assess how much the dynamic region is sensitive to a change of this parameter. Two coefficients have been considered. They are equal respectively to $4 \times 10^{-4}$ cal/cm$^2$ sec K and $2 \times 10^{-3}$ cal/cm$^2$ sec K. The attention was mainly focused on the extension of the dynamic region as function of the heat coefficient and not on oscillations features. Figure 5.6 shows the ignition maps obtained from the two coefficients.

**Figure 5.6** Ignition maps obtained as function of the global heat transfer coefficient.

Changing such parameter, the same typologies of oscillations were been found out,
but they are not reported in the figure. The dynamic regions extends for the same values of the C/O feed ratios but not for the same range of temperatures. As matter of fact, the oscillation region relative to the coefficient $4\times10^{-3}$ cal/cm$^2$ sec extends from 1050K to 1275K, whereas the oscillating region relative to the coefficient $2\times10^{-3}$ cal/cm$^2$ sec from 1050K to 1200K.

The shape of the two areas is similar and they almost coincide for low values of temperature and for lean mixtures. For both the two global heat transfer coefficients the dynamic regions extend for a stochiometric mixture.

**Analyses of the frequency**

The computed oscillation frequencies were reported in Fig.5.8 as a function of the inlet temperature on C/O ratio parametric curves.

![Figure 5.8 Numerical frequency profile as function of inlet temperature for different C/O ratios.](image-url)
For this analysis the “Warnatz” model has been chosen. It is easily shown that for a fixed C/O ratio the frequency increases with temperature whereas it decreases with a C/O increase, thus confirming the general trend obtained by means of the experimental analysis. However, the numerical computation is not able to predict the absolute values of the frequencies. In fact, they range from 0.2 Hz to values higher than 30Hz, whereas the highest experimental frequency value is 7Hz.

Numerical Ignition map with the Dsmoke Software

In the numerical analyses, realized to characterize numerically the behavior of the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}, the model “TOT0310” of the research group of the Chemical Department of the University of Milan (E.Ranzi et al., 1994) has been used. It counts 250 species involved in more than 5000 reactions and has been extensively validated across a wide range of conditions (E.Ranzi et al., 1994; E.Ranzi et al., 2001). Hereafter the model will be referred as “Ranzi” model.

The possibility to predict the dynamic behavior by means a more complex kinetic model, that maybe could reproduce some features of oscillations not forecasted by the other two models, has engender interest.

The main pathways of methane combustion can be summarized briefly as follows. CH\textsubscript{4} oxidation undergoes H abstraction with the consequent formation of the methyl radical. CH\textsubscript{3} reacts with O\textsubscript{2} to form CH\textsubscript{3}O whose decomposition produces formaldehyde. H-abstraction and dehydrogenation of CH\textsubscript{2}O successively form HCO and CO. Finally, CO interaction with OH produces CO\textsubscript{2}. At low temperatures, CH\textsubscript{3} can add on O\textsubscript{2} forming a CH\textsubscript{3}OO radical, whose main fate is CH\textsubscript{2}O formation or CH\textsubscript{3}OH, at high pressures. At high temperatures, OH attacks on CH\textsubscript{3} can generate CH\textsubscript{i} radicals whose interactions with O\textsubscript{2} are
also responsible for CO formation. In rich conditions, the CH₃ recombination gives rise to C₂H₆ whose successive pyrolysis reactions are responsible for the formation of dehydrogenated molecules, then aromatic and polyaromatic molecules and finally soot particles.

The software used to perform these further simulations is the DSmoke code. It is discussed in chapter III.

The focus of the numerical simulations has been on the temperature region in which the oscillations took place. The numerical map of the system diluted with nitrogen up to 90% is reported in Figure 5.13. The global heat transfer coefficient was set equal to 2*10⁻³ cal/cm² sec K since more thorough calculations showed that it was more adapt for the real system used for the experiments.

![Figure 5.13](image)

*Figure 5.13  Numerical map at 90% of dilution level.*

The numerical results demonstrate that the kinetic model is able to reproduce dynamic region. For C/O=0.05-0.1, the oscillations are present in the 1030K to 1275K temperature range. By increasing the C/O, the dynamic region shrinks, covering a shorter
temperature range, and disappears altogether when the C/O is higher than 0.45. The numerical model is also able to predict different oscillation typologies. Single oscillations occur across most of the dynamic area, but, in contrast with the two other models, it was also possible to predict double and irregular oscillations and locate them in a region. Such area develops for temperature comprised 1075K-1160K and for C/O values between 0.075 and 0.18.

**Effect of hydrogen addiction**

The availability of feasible methane oxidation kinetic models has suggested the possibility of studying the effects of the hydrogen addition to the methane Mild Combustion by means of a numerical approach. As mentioned before, two reaction mechanisms have been considered for this analysis, namely the “Warnatz” and the model of research group of the "Laboratoire de Combustion et Systèmes Réactifs” of the CNRS that hereafter will be referred as “Dagaut” models (Dagaut et al., 2004). For both the kinetic models used, simulations have been run for the same initial conditions considered during the experimental tests.

Fig.5.17 shows the results obtained from the simulations using the “Warnatz” model: as shown in chapter IV such a model is able to predict the existence of a steady and a dynamic region and it is able to reproduce part of the oscillation typologies experimentally detected, for instance, cusp, damped and triangular oscillations. A thorough analysis of the numerical results has been presented in the chapter V, hence here they will not be re-proposed again since the attention has exclusively been focused on the hydrogen addiction effect on the oxidation evolution process of the system CH$_4$/O$_2$/N$_2$.

Fig.5.14 shows the T$_{in}$-C/O map obtained using the “Warnatz” model. Maps with a hydrogen molar percentage equal to 0%, 0.25%, 0.5%, 0.75% and 0.9% are reported. The
global heat transfer used for these simulations is equal to $2 \times 10^{-3}$ cal/cm$^2$ sec K.

The map relative to the system CH$_4$/O$_2$/N$_2$ extends in a temperature range that goes from 1050K to about 1200K and in a C/O feed ratio going from values very close to zero to about 0.4.

![Figure 5.14](image)

*Figure 5.14  Numerical ignition maps for the system CH$_4$/O$_2$/N$_2$ with different hydrogen contents using “Warnatz” kinetic model.*

The hydrogen addiction leads the superior extreme of the C/O feed range to lower from 0.4 to 0.3, whereas the inferior extreme does not change at all.

At the same time, as the hydrogen percentage increases, the ignition maps is shifted towards lower inlet temperatures. Furthermore there is a reduction of the extension of the dynamic region for lean mixtures, hence for mixtures with a C/O feed ratio lower than 0.25.

It is worth noting that the most relevant change in the determination of the extension of the dynamic region is obtained when hydrogen is added to the original system, that presents just methane as fuel, independently from its inlet concentration.
In fact the addiction of hydrogen also in small amount \((H_2=0.25\%)\) causes the most meaningful change in the extension of the dynamic region in the C/O feed ratio range. Further increase in hydrogen percentage causes just a shift of the dynamic region towards lower inlet temperature and a small reduction of the dynamic region for lean mixture. Anyway, although it is a relevant result, the system appears to be more sensitive to the presence of hydrogen than to its actual concentration value.

Figure 5.15 reports the numerical map predicted using the “Dagaut” model. In this case just the maps for the system \(\text{CH}_4/\text{O}_2/\text{N}_2\) and \(\text{CH}_4\text{-H}_2/\text{O}_2/\text{N}_2\), with the hydrogen molar concentration equal to 0.9\%, are presented. In fact the aim was just to see whether other kinetic mechanisms, that involve more species and reactions, were able to get the main features of the effect of the hydrogen addiction to the original system.

In this case the dynamic region for the system \(\text{CH}_4/\text{O}_2/\text{N}_2\) interests a wider region in the C/O feed ratio range that goes from values very close to zero up to about 0.4, while the
inlet temperature range extends from 1040K to 1200K. The addition of hydrogen leads to a reduction of the dynamic area both in the inlet temperature and the C/O feed ratio. In fact the ignition maps relative to the system CH₄-H₂/O₂/N₂ extends from 1025K to 1175K, and a C/O feed ratio from 0.05 to 0.3.

Furthermore it is evident that there is a reduction of the area where oscillations take place for lean mixtures.

Although both the temperature and the C/O feed ratio ranges, for which instabilities occur, are narrower in comparison with experimental data, both the models are able to reproduce the main features of the effect of the hydrogen addition to methane Mild combustion encountered during the experimental test.

As a matter of fact, the zone where dynamic behaviors occur becomes smaller and it is shifted towards lower values of the inlet temperature, in dependence of the amount of hydrogen. Moreover, models predict the reduction of the dynamic region for values lower than the C/O$_{stoich.}$=0.25.

**Rate-of-production analysis**

To identify the hydrogen addition effect on the kinetic paths of methane oxidation, a rate-of-production analysis was carried out for $T_{in}$ equal to 1015 K and for a C/O ratio value equal to 0.2. Fig.5.16 shows the effect of the hydrogen addition on the temperature temporal profiles predicted by the “Warnatz” model.
To identify the hydrogen addition effect on the kinetic paths of methane oxidation, a rate-of-production analysis was carried out for $T_{in}$ equal to 1015 K and for a C/O ratio value equal to 0.2. Fig.5.17 shows the effect of the hydrogen addition on the temperature temporal profiles predicted by the “Warnatz” model.

An addiction of hydrogen to the system CH$_4$/O$_2$/N$_2$ leads the system to pass from a slow combustion to an oscillating regime. The analysis was performed at 0.2 sec after the beginning of the simulation.

Analyses realized in absence of hydrogen show that for the chosen inlet conditions the main branching reaction might be the decomposition of the H$_2$O$_2$. H atoms react via the breaking reaction H+O$_2$+M $\rightarrow$ HO$_2$+M producing the relatively stable HO$_2$ radicals. They form H$_2$O$_2$ that decomposes into two OH radicals.

The presence of hydrogen promotes the high temperature classical branching reactions and increases the whole reactivity of the system (Dagaut P. et al., 2004). In fact H$_2$ reacts mainly with OH through the exothermic reaction H+O$_2$+OH+O. From the rate-of-production analysis it has come out that reactions that involve the radical OH show the
most significant increment. For H₂ concentration equal to 0.9% also the breaching reaction \( \text{H}_2 + \text{O} \rightarrow \text{OH} + \text{H} \) becomes significant in the production of OH radicals. They mainly dehydrogenate the methane to CH₃. In such a way the oxidation pathways of methane can be initialized and accelerated by the great amount of radicals present in the system. These kinetic paths are resumed in the flow diagram reported in figure 5.20. The thickness of the arrows is proportional to the rate of the several reactions reported in the scheme. This diagram is relative to a hydrogen inlet concentration equal to 0.9%.

Figure 5.17 Main kinetic paths involved in the ignition mechanism of the CH₄-H₂/O₂-N₂ system in presence of hydrogen for \( T_{in} = 1015 \text{ K} \) and C/O = 0.2 at the time \( t = 0.2 \text{ s} \).

**Effect of the nature of Diluent: Steam Water**

Kinetic models have shown the capacity of predicting the main features of the dynamical behavior experimentally identified. Therefore the effect of the nature of the diluent has been studied also by means of a numerical approach.

The behavior of five different systems has been studied using the “Warnatz” methane oxidation mechanism. The numerical analysis relative to the system CH₄/O₂ diluted with nitrogen up to 90% has been widely discussed in Chapter IV, but here the ignition maps
has been re-proposed. The working parameters are the same of the experimental tests, except the temperature range since the numerical possibility to exploit the behavior of the system for higher temperatures. Hence the residence time is 0.5 sec, the pressure has been set equal to 1 atm. The temperature range goes from 1000K to 1500K, while the C/O feed ratio from 0 to 1.2.

The numerical analyses have had the aim to study the behavior of the system \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \) with several steam amounts. Steam water concentration is relative to the overall dilution degree, in fact it substitutes nitrogen in order to keep fixed the dilution degree. Steam percentages are equal to 10%, 20%, in order to consider the working conditions used during the experimental tests, then 50% and 100%, to better understand the effect of steam on the methane oxidation in non-standard conditions.

Results have been resumed in ignition maps reported in figure 5.18.

In the maps the steady combustion area and the dynamic regions are identified. Furthermore the dynamic region has been split into two regions, the darker areas represent inlet conditions for which the systems evolves trough damped oscillations, while the remaining part is relative to cusp-shaped oscillations or triangular oscillations.

The figure a) is relative to the system diluted in \( \text{N}_2 \). The dynamic region extends between 1040K and 1200K and for a C/O feed ratio comprised between 0.4 and 0.01. For C/O=0.4 oscillations occurs in a very narrow temperature range. It goes from 1100K to 1140K. Decreasing the C/O feed ratio towards the stoichiometric value (C/O=0.25) the dynamic region enlarges. A further decrease of the parameter C/O causes a narrowing of the region, in fact both the left and side borders of the region go towards lower inlet temperatures. Then for very lean mixtures, the dynamic region closes and stable combustion occurs. The damped oscillations are located on the top and on the left side of the map.
Figure b) shows the evolution of the regimes that can occur during the methane oxidation in Mild condition for the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}-H\textsubscript{2}O with a steam percentage, respect to the overall dilution degree, equal to 10%. The steam addition seems to enlarge the extension of the dynamic region in the temperature field but to reduce it in the C/O feed ratio field. In fact oscillations occur in a temperature range that goes from 1020K to 1240K and a C/O feed ratio that goes from 0.4 to 0.1. Also in this case the region is relatively narrow for C/O values close to 0.4 but than it enlarges towards the stoichiometric value. In fact for C/O=0.25 the region reaches its maximum extension. Decreasing the parameter C/O towards values that indicates lean mixtures, the region slightly reduces its extension but for C/O comprised between 0.2 and 0.1 there is a central core where the system reaches the stability and oscillation disappears. Hence in this C/O feed ratio range oscillations occur for an inlet temperatures comprised between 1020K and 1080K, and than between 1160K and about 1220K. Furthermore, for C/O=1 oscillations are numerically predicted in the range 1020K-1140K and they are damped. Other damped oscillations have been found out for rich mixtures characterized by a C/O feed ratio comprised between 0.3 and 0.4 in all the temperature range where oscillations occurs for these C/O feed ratios and for all the inlet conditions that are near the left side border of the dynamic region, just in correspondence to the passage between the stable combustion and the dynamic region.
Figure 5.18  Numerical ignition maps realized for the system CH4/O2 diluted with steam and nitrogen up to 90% as function of the steam concentration.

Figure c) shows the ignition maps obtained for the system CH4/O2/N2-H2O (20%). The dynamic region extends in a wide temperature range that goes from 1040K to about
1300K and in a C/O feed ratio range that goes from 0.4 to about 0.1. Also in this case the maximum extension of the dynamic region, respect to the parameter $T_{in}$, is reached for a stoichiometric mixture.

If the C/O feed ratio is increased, the region narrows and disappears for C/O=0.4; on the contrary if C/O is decreased, the dynamic region diminishes its extension and there is a central core in the region where stable combustion occurs. For C/O=0.1 the oscillations have been found out in the temperature range comprised between 1040K and 1160K. Damped oscillations have been identified for rich mixtures, characterized by a C/O feed ratio comprised between 0.4 and 0.3, and for values close to 0.1. Furthermore damped oscillations establish for the inlet conditions that are positioned in the left side of the map in correspondence of the passage from the stable and dynamic regions.

Similar considerations can be applied to the system CH$_4$/O$_2$/N$_2$-H$_2$O (50%). The ignition map relative to this system is reported in figure d). Oscillating region extends from $T_{in}$=1060K to $T_{in}$=1380K. For lower inlet temperatures (1060K-1160K), the dynamic region extends between C/O feed ratios equal to 0.1 up to 0.4. In this temperature-C/O feed ratio range the most of the inlet conditions give rise to damped oscillations except for a narrow region that develops in the surrounding of the C/O stoichiometric ratio up to the maximum values of temperatures where oscillation have been identified.

The last system analyzed is fully diluted in steam water. The ignition map is reported in figure e). In this case oscillations have been identified in two different separated areas. The former develops for a temperatures range that goes from 1060K to 1240K and a C/O feed ratio that ranges from 0.4 down to 0.15, the latter goes from $T_{in}$ in the range 1360K up to 1440K, and for C/O feed ratios very close to the stoichiometric values. It is worth noting that in the first area just damped oscillations have been identified, while in the second area triangular oscillations occur.
Figure 5.19  Numerical methane conversion and yields in various species as function of steam concentrations.
The system CH₄/O₂/N₂-H₂O has been analyzed also in terms of methane conversion and yields of species such as CO, CO₂, and C₂H₂ as function of the different steam water percentages considered in this analysis. The analysis has been realized for a temperature range that goes from 1000K to 1700K and for a rich mixture (C/O=0.4), in order to avoid the oscillations regions in the various systems.

The results are shown in figure 5.19. The trends of the curves relative to the methane conversions and/or to species yields as function of the inlet temperatures are very similar among them; hence in this paragraph the behavior of the system diluted in N₂ is thoroughly described as representative of all the other systems. A systematic comparison among the systems is remanded to Chapter V.

For the system CH₄/O₂/N₂ methane conversion for Tᵢn=1025K is very close to 0.2. As the inlet temperature increases, the methane concentration abruptly increases, reaches almost a plateau, and then very slowly increases. Methane is converted mainly in CO and CO₂ as the figure2a shows.

The CO yield increases, reaches a maximum value, slowly decreases until it reaches a minimum value, but for temperature higher that about 1500K starts increasing again. The CO₂ increases as the temperature is increase from 1025K, but after a sharp enhancement it increases slowly in correspondence of the plateau of methane conversion, then reaches a maximum and start decreasing after the CO curve has passed through it minimum value.

At the same time, if the attention is focused on the C₂ compounds, it is possible to see that the methane conversion in C₂H₄ and C₂H₆ has a maximum at 1075K but then, as the inlet temperature increases, it goes slowly to zero. On the contrary, the yields in acetylene cannot be neglected since it increases with the inlet temperature.

The same considerations apply to the other systems. In particular it is worth noting that, as much as the concentration of steam water is augmented, the methane yield into
CO\textsubscript{2} increases and the one into CO decreases. In addition the CO\textsubscript{2} curves for the system diluted with steam at 50\% and 100\%, monotonically increase. Furthermore the acetylene curves pass trough a maximum and then slowly start decreasing. It is also clear that the minimum values of methane yield into CO corresponds to the maximum values relative to C\textsubscript{2}H\textsubscript{2} production.

**Identification of the Main Parameter of the Mixing Configuration**

In order to assess the goodness of the mixing device described in previous sections, several numerical analyses were performed employing the CFD package software FLUENT 6 (www.fluent.com). The geometry of the duct has been drawn taking into account the reactor design.

There is a first duct 10 cm long with a diameter of 1,4 cm, followed by the convergent section with different geometries and then by a cylindrical duct with a diameter of 1 cm. It is long 5 cm since the attention was focused just on the mixing. The first part of the sketch in the diagram shown in this paragraph has been cut off since the concentration of the methane is zero and it does not give any further information for this analysis. Edges, surface and volume are meshed employing respectively the Successive Ratio grading scheme, the Tripave face-meshing scheme and the Tetrahedral volume meshing scheme. Meshes are much denser near lateral holes and get coarser upstream and downstream of the holes plane. The FLUENT Segregated solver has been chosen since it is traditionally used for incompressible and mildly compressible flows. The Energy Equation, the turbulent \( \kappa-\omega \) (kinetic energy-specific dissipation rate) model and the Species models have been enabled.

The turbulent \( \kappa-\omega \) model has been chosen in this case because it is widely used for
round and radial jets in cross flow geometries; the Species model allows for simulating the mixing and transport of chemical species by solving conservation equations hence describing convection, diffusion, and reaction sources for each component species.

Several numerical simulations have been run in order to assess the efficiency of the mixing device analyzing the mixture along the axial and radial coordinate.

In particular the dependence of the mixing degree was studied as function of \( J \), the number of holes, the geometry of the convergent and finally, the position of injectors in the mixing section.

In these chosen configurations the main flow rate enters the first duct with a velocity of 45 m/s at 1400 K and with a composition of steam vapor at 92% and O\(_2\) at 8%. This temperature has been chosen since it represents the middle value in the range of temperatures that will be exploited experimentally in the future during experiments on Mild Combustion condition. The lateral flow is composed by CH\(_4\)-N\(_2\)-He in equi-molar fraction. It has been necessary to use also nitrogen and helium in order to make \( J \) invariable on the C/O feed ratio varies. By means of this trick, the lateral flow is always the 10% of total flow, hence the velocity from the injector is constant, and the mix CH\(_4\)-N\(_2\)-He in equimolar fraction has a molecular weight equal to 16. Therefore \( J \) in not affected by C/O feed ratios changes since the flow rates are the same and the molecular weight of the lateral flow does not change. The value of the injected flow temperature is reasonable since the lateral flow rate should be at environmental temperature but the whole reactor will be located in a heater that will work at very high temperatures. Hence the inlet temperature of the lateral volumetric flows will slight increase. The chosen compositions for the main flow rate and the lateral flow rate are relative to a system with the stoichiometric C/O ratio and a dilution level \( \alpha \) of 90%. The diameters of holes and the inlet velocity of the lateral jet are set in order to have the desired values of \( J \).
The reason why the methane has been chosen as fuel is that the first trend of experiments in Mild condition will be performed is that it is the simplest hydrocarbon. In fact, in order to characterize a new process, such as Mild Combustion, it is reasonable to start from the simplest possible conditions. As matter of fact, the kinetic of methane is well known for traditional process. Furthermore our aim is the characterization of the mixing for this fuel in Mild condition in presence of water.

Fig. 5.20 shows the molar fraction distribution of CH$_4$ along the plane $z=0$ and the cross sections at the injection plane, at an axial distance equal to $X/R=1$ from the injection plane where the convergent is located and at a distance of 1 and 2 centimeters from the last plane. A plane has been located at a distance of $X/R=1$ in order to verify the mixing in this position since Holdeman equations should insure a good mixing by this plane. Methane molar fraction has been subdivided in twenty levels as the scale of color on the bottom of fig.4 suggests. When the systems reaches the complete mixing the final value of methane molar fraction is 3.34%.

**Dependence of mixing degree on n**

Cases a), b) and c) show the dependence of the mixing degree on the number of holes $n$. the values of $n$ are respectively is 10, 8 and 6. $J$ is fixed and it is equal to 32. This value is the optimum value for a configuration with 10 holes in according to Holdeman equation.

It is possible to see that decreasing the parameter $n$ the axial mixing becomes increasingly better. In fact the full mixing is reached for a shorter axial distance from the injection plane as the number of holes increases. This is mainly due to the increase of the jets penetration. As matter of fact if $J$ is fixed, it means that the velocity of the lateral jet is the same but the diameter of jets is bigger as $n$ decreases. Hence its structure is more consistent and it can penetrate for a longer radial distance. On the other hand, a higher
number of holes provides for a more merged and uniform structure as it can be seen from the methane molar concentration in the chosen cross sections of the duct.

*Dependence of mixing degree on J*

Case d), e) and f) the influence of \( J \) on the mixing for a system with 6 equally spaced holes. The value of \( J \) is respectively 28, 18 and 11. The last value represents the optimal condition for the chosen geometry according equation from literature.

Decreasing \( J \) the axial mixing becomes increasingly worse. In fact, an unmixed central core persists for a longer axial distance.

The case with \( J=28 \) provides for the fastest mixing even if it is possible to see in the near-wall region a small persistent layer in which the concentration of methane is lower. It is a case of over-penetration. These simulations suggest, in according with Holdeman results, that it is more convenient to work with a slight over-penetration.

Furthermore it has to be underlined that case a) and case f) represent optimal conditions according to Holdeman equations. The methane distribution in the cross sections and in the longitudinal section of the reactor suggests that it is better a configuration with a lower number of holes.

*Dependence of mixing degree on tube position*

Case f), g) and h) show that the position of tubes inside the duct is an important parameter. In these cases the inlet fuel jet velocity is the same but the radial position of the six tubes is respectively \( R=0.7 \) mm, \( R=0.6 \) mm and \( R=0.5 \) mm from the duct axis. The first case represents a situation of under-penetration, while the last one a case of under-penetration. In fact there is an unmixed core with respectively a lower and a higher methane concentration in comparison with the final value. Case g) seems to provide for a
very efficient mixing.

*Dependence of mixing degree on the convergent geometry*

Fig. 3 a), i) and l) show the dependence of the mixing on the geometry of the convergent.
Figure 5.20  $\text{CH}_4$ molar fraction distribution along the plane $z=0$ and on different cross sections at fixed $x$ values.
In case a) and i) the convergent is linear but it is characterized by a different slope. It is respectively 26° and 15°; in case l) it is a round convergent. In any case the mixing distance, before the incoming of the reactor, has been fixed and it is 0.7 cm.; \( J \) is 32 and the number of holes is 10.

In case a) there is a persistent unmixed central core that remains for a long axial distance. A convergent with an angle of 15° makes worse the mixing. In fact, as shown in case i), the unmixed core persists for a longer axial length.

Mixing seems to work slightly better with a round convergent as case l) shows. In this case geometry gives a radial component to the main flow at the entrance of the reactor and it results in an improvement of mixing. It is comparable with case a).

**Brief Discussion**

These results suggest that for a fixed \( J \) it is better to work with a lower number of holes respect to the number of holes suggested by Holdeman equations. Furthermore it comes out that the radial position of injection tubes is an important parameter in order to achieve an efficient mixing of reactants for experiment in the tubular flow reactor. The use of a mixing section with a greater diameter provides for a higher \( J \) since in this way the velocity of the main flow is decreased. It has benefic effect on the entity of the penetration of jets. But at the same time a larger diameter means that jets flow might enter for a longer radial distance towards the center of the duct. This inconvenient is resolvable by changing tubes position inside the duct. As matter of fact, the nozzle protrusion inside the duct is an important parameter in order to reach a good and fast mixing and, at the same time, it makes the mixing device be very adaptable to different working conditions.

Furthermore the geometry of convergent is the other parameter that mainly affects the mixing. It comes out that a convergent quite pronounced is to be preferred because it
gives flow a radial velocity component to the main at the incoming of the reactor that improves the mixing. At the same time a vertical convergent is to be avoided since it could induce a stagnant zone on the wall just before the inlet of the reactor where undesired reactions could occur.

Hence at the light of these results the optimum configuration of the mixing device is the one characterized by 6 holes and a convergent with a slope of 26°. The optimal $J$ for this configuration according to Holdeman equation is 11 and the diameter for our working conditions should be 0.84 mm. In order to enhance the value of $J$ it has been thought to work with a nominal dimension of the diameter equal to 0.80 mm. The position of injectors inside the duct will be adjusted respect to the working conditions in order to enhance the efficiency of the mixing device since it is obvious that it is the parameter that mainly can affect the mixing of reactants.

**Velocity profiles**

The system has been numerically studied also to see if the velocity profile is close to a flat condition. The geometry of the duct is the same of the one used to analyze the goodness of the mixing device. All the configurations of the mixing section were suitable to perform this study. In particular in the analyzed case the mixing device has 6 holes and $J$ is 32. The velocity of the main flow is about 45 m/s at 1400 K and the composition is steam vapor at 92% and O$_2$ at 8%. Methane enters into the main duct diluted with N$_2$ and He in equimolar fraction trough the six holes with a velocity of 170 m/s at 500K. The system is long 15 cm, the main duct is 10 cm and jets are located on the circumference of the section at an axial distance equal to 9.3 cm. The distance between the injection section and the beginning of the convergent is 0.7 cm. The convergent has a linear geometry and a slope equal to 26° characterizes it. The results are shown in fig. 5.21.
In the figure the first 5 centimeters of the reactor have been cut off since the attention has been focused on the velocity field, but the analysis of the first part of the main duct does not provide for further meaningful information.

Figure 5.21  Study of the velocity field in the CH\textsubscript{4}/O\textsubscript{2} diluted with H\textsubscript{2}O, He and N\textsubscript{2}.

Figure 10 a) shows the velocity field along on the plane z and on the cross-section at an axial distance of 6 cm from the inlet section of the main flow.

The velocity has been subdivided in fifty ranges of values which correspond to fifty colors as shown on the scale reported on the right side of the figure a). Furthermore figure 5.21 b) shows the velocity values corresponding to axial position of points that lie on the
center line of the duct. The figure shows the velocity trend from the beginning to the end of the reactor. It is possible to see that the inlet velocity is 45 m/s, and then it slightly increases up to 50 m/s until the injection section. In the proximity of the cross section, where jets are located, it decreases slightly but then it sharply increases up to about 100 m/s. This value remains constant until the outlet section.

Figure 5.21 c) plots the velocity as function of the radial position on the diameter located at the intersection between the plane x=6 and the plane z=0.

It is possible to note that the profile is quite flat and the maximum value of velocity is about 103 m/s. For more than the 40% of the entire diameter the velocity has the same value. Also in this case the viscous sub-layer is almost the 20% of the entire diameter.

**Characteristic Times of the System**

In order to fully characterize the tubular reactor for the study of the Mild combustion processes, it is very helpful to assess the characteristic times of the chosen system in terms of the auto-ignition time and the mixing time. They have a great relevance in the comprehension of the feasibility of experiments and on the designing of the reactor.

*Auto-ignition time* $\tau_{\text{ign}}$

In order to consider efficient a mixing device it has to ensure the mixing of reactants before the occurrence of the oxidation reaction. In particular in the jet in cross-flow configuration the fuel is introduced inside the main duct, where it mixes with the main flow, through the injectors. Hence there is the region close to the nozzles where the mixture composition is very rich in fuel, then the jets penetrates inside the duct and the composition changes and later, after a certain axial distance from the injection plane, the system is well mixed and reaches the wanted composition. Thus it is clear that during the mixing there
form different mixtures with different compositions. Therefore the requirement the mixing device has to satisfy is that the mixing time has to be lower than the auto-ignition time of any mixtures that form in the mixing process.

Hence, a preliminary analysis of the auto-ignition time of inlet reactants has to be performed for a system working in Mild Combustion conditions.

The mixture which has been analyzed is composed by methane and oxygen diluted in nitrogen or vapor water. This auto-ignition time $\tau_{\text{ign}}$ has been evaluated for different inlet temperatures and for different C/O (carbon/oxygen) feed ratios.

First of all, the system has been analyzed in presence of nitrogen since it is inert, and than in presence of vapor water since it will be the diluent in our experiments. Vapor water is expected to give different results on the characterization of $\tau_{\text{ign}}$ since its higher heat capacity and since its efficiency as third body in tree-body reactions is very high. Hence it should influence the reactions responsible of the ignition of methane influencing the auto-ignition time.

The reason why the methane has been chosen as fuel is that the first set of experiments in Mild conditions will be performed with this fuel as mentioned in the previous paragraphs.

The characterization of the auto-ignition time $\tau_{\text{ign}}$ has been performed numerically by means of the PLUG application of the CHEMKIN 3.7 package (CHEMKIN), that allows for the simulation of a plug flow reactor. The results were then compared with the ones obtained by means of the SENKIN application that allows simulating the behavior of a zero-dimensional reactor. The kinetic model used for the simulation is the model of Warnatz (1997) for the oxidation of methane.

It is important to highlight that the ChemKin software is able to describe the system in term of chemistry but it is not a computational fluid-dynamic code hence it does not deal
with complex mixing problems. Reactants that enter the reactor are already mixed.

Before performing this analysis we need a definition of the auto-ignition time since in literature there is not a rigorous definition. We refer to the auto-ignition time as the time reactants need to increase the inlet temperature of 10K.

Simulations have been run for temperatures ranging from 1000K to 1800K and C/O comprised between 0.01 and 1 for a dilution level equal to 90%. The plug flow reactor has been simulated in adiabatic condition.

The auto-ignition time is calculated dividing the axial distance in the plug flow at which there is an increase of the inlet temperature of 10K by the velocity that is assumed to be equal to 100 m/s. This value can be considered constant since the volumetric flow rate does not change significantly for a temperature increase of 10K.

Figure 5.22 plots the auto-ignition time as function of the C/O feed ratio in parametric curves respect to the inlet temperatures for a system diluted in nitrogen.

The curves relative to 1000K, 1100K and 1200K are not reported since the ignition of the mixture occurs for axial distance longer then 1 m, which is the dimension of the reactor.

![Auto-ignition times for the systems CH₄/O₂/N₂ as function of C/O feed ratio for different T_{inl}](image)

*Figure 5.22*  Auto-ignition times for the systems CH₄/O₂/N₂ as function of C/O feed ratio for different T_{inl}.*
It is possible to recognize a general trend: any curve presents a minimum for very lean conditions. For instance, for $T_{\text{inlet}}=1300$K there is a minimum value for C/O=0.025. It is a interesting result since it is note that for paraffins an increase of reactivity of the system is expected for rich feed ratios very close to the stoichiometric value (Warnatz et al., 2001).

This trend is smoothed as much as we increase the inlet temperatures but it is still present for $T=1800$K. In fact increasing the inlet temperature $\tau_{\text{ign}}$ for different fuel/oxygen ratio become closer.

This trend was recognized also using other mechanism such as GRIImech 3.0 (http://www.me.berkeley.edu/gri_mech/) for the oxidation of methane. For $T=1800$K the minimum value of $\tau_{\text{ign}}$ is $1.7 \times 10^{-4}$ sec for C/O=0.025. It represents a very extreme situation not just because of the very short auto-ignition values but also for the very high temperature that is reached for this inlet condition. Anyway the analysis of the condition in which our experiments can be run is remanded to the next paragraphs.

Without taking into account the most stringent conditions, it is possible to say that if the inlet temperature is increased up to 1500K the value of the auto-ignition time $\tau_{\text{ign}}$ is of the order of magnitude of $10^{-3}$ sec.

Therefore it will be the order of magnitude of the auto-ignition time for the analyzed system.

At this point it is interesting to perform the same numerical analyses for a system diluted with vapor water. The results are shown in fig. 5.23. The auto-ignition time curves show the same trend individuated also for the system diluted with N$_2$. Also in this case any curve presents a minimum for very lean working condition. Anyway there is not big difference between the auto ignition times for the two systems.
Figure 5.23  Auto-ignition times for the system CH$_4$/O$_2$/H$_2$O as function of C/O feed ratio for different $T_{\text{inlet}}$.

This aspect is better highlighted in figure 5.24 where it is shown a comparison between the auto-ignition times for the system diluted with nitrogen and vapor water for $T=1300K$, 1500K and 1800K.

In this figure there is a comparison between the auto-ignition time for the system diluted with nitrogen and vapor water for $T=1300K$, 1500K and 1800K. In this case the auto-ignition time is plotted as function of the inlet temperatures. The curves are parametric in the C/O feed ratio. The continuous lines are relative to the system CH$_4$/O$_2$/N$_2$, the dashed lines to the system CH$_4$/O$_2$/H$_2$O. Also here it is possible to see that the minimum of the auto-ignition time $\tau_{\text{ign}}$ is not at the stochiometric values (C/O=0.25) but it is for lower C/O ratios. In fact the curves relative to a C/O feed ratio equal to C/O=0.1 is lower than the one relative to the stochiometric condition (C/O=0.25).
Figure 5.24  Comparison between auto-ignition times for the systems CH₄/O₂/N₂ and CH₄/O₂/H₂O.

It shows that there is a very small difference between the auto-ignition times. Anyway the presence of vapor water causes a slight damp of the reactivity of the system causing a small delay in the auto-ignition time. Furthermore it is possible to note the same trend of τ_{ign} obtained for the system diluted in nitrogen as function of the C/O feed ratio. The system shows an increase of the reactivity for lean conditions.

Therefore also in this case it can be assumed that the characteristic τ_{ign} is 10⁻³ sec.

*Mixing time* τ_{mix}

The mixing time is the other characteristic time that has to be evaluated. We will assume that the reactants mix completely in the mixing section. This assumption is quite reasonable since the mixing device can be adjusted in order to insure this condition. The distance between the entrance of the reactor and the injection plane is 0.7 cm. The velocity can be considered equal to 75 m/s since it is the average between the velocity of the main flow before the injection plane (45 m/s) and the velocity in the reactor (100 m/s). The increase of velocity is due to the presence of the convergent, which reduces the cross section of the duct from 1.5 cm² to 0.785 cm², and to the increase of the volumetric flow
rate since the addiction of the injected flows. Hence with this assumption the mixing time \( \tau_{\text{mix}} \) is of the order of magnitude of \( 10^{-4} \) sec.

Therefore concluding we can say that for the most of the conditions \( \tau_{\text{mix}} < \tau_{\text{ign}} \).

**Strain rate \( a_s \)**

The mixing is realized using a jet in cross-flow mixing. Lateral jets enter the mixing zone with a high velocity and they are invested by the main flow. In this configuration high gradients of velocity can be realized. If the auto-ignition had been shorter than the mixing time, anyway it could have been taken into account the fact that high velocity gradients could cause the blow out of the flame in a diffusion system. This is not our case because, as shown in the previous paragraph, \( \tau_{\text{mix}} \) is an order of magnitude smaller than \( \tau_{\text{ign}} \). But it is an interesting aspect of this configuration since it provides for a further insurance on the possibly of avoiding the insurgence of reactions in the mixing section where they are not desired.

Therefore a further numerical analysis has been performed by means of the SPIN application of the CHEMKIN 3.7 package, that allows for the simulation of one-dimensional stagnation flow reactor.

The configuration of this reactor is shown in fig. 5.25.
This configuration is characterized by two opposed plates, the former has a porous set through that mixed gases come out and hit the second non-porous plate located at a distance \( x=L \). The gas parameters are the inlet temperature \( (T_{\text{inl}}) \), the composition and the velocity. More commonly in this configuration the parameter strain rate \( a_g \) is used. It is simply calculable dividing the enter gas velocity by the distance \( L \) (Smith et al., 1971).

The numerical study has been realized with the aim to calculate the critical strain rate as function of the mixture composition and the inlet temperature.

The inlet mixture is composed by water steam, nitrogen, helium, methane and oxygen in such a composition that the sum of the water steam, nitrogen and helium represents the 90% of the mixture while the methane and oxygen the 10%. The nitrogen and helium are fed in equi-molar composition and their sum is equal to the oxygen amount. The fuel and the oxygen molar proportion is given by the parameter Carbon/Oxygen feed ratio \( (C/O) \). These compositions are the same of the ones that will be used in the real reactor.

The chosen temperatures are 1300K, 1500K and 1800K, while the parameter \( C/O \) has been exploited from values very close to zero to 1. The distance between the plates has

\[
\begin{align*}
\mathbf{u} &= -u_L \\
\mathbf{r} &= \theta
\end{align*}
\]

Figure 5.25  Sketch of the infinite-radius disk and inlet boundary conditions.
been fixed to 2 cm.

For these simulations the GRI 3.0 ([http://www.me.berkeley.edu/gri_mech/](http://www.me.berkeley.edu/gri_mech/)) methane oxidation kinetic mechanism has been used. The kinetic mechanism has been properly changed, in fact the species helium and its efficiency in the third-body reactions have been declared.

The critical strain rate has been defined as the value for which the heat released from the mixture is equal to 1% respect to the heat that, for any mixture composition and inlet temperature would be released considering the system in adiabatic condition.

![Critical Strain Rate vs C/O Feed Ratio](image)

**Figure 5.26**  Critical strain rate as function of the C/O feed ratio on curves parametric in the inlet temperature.

Fig. 5.26 shows the critical strain rate as function of the C/O feed ratio on curves parametric in the inlet temperature. It is possible to note that the curves present the same trend as function of the system composition. In fact the strain rate, necessary to quench the flame, increases if the C/O feed ration is decreased.

The maximum value of the critical strain rate for the mixture fed at 1300K is 550 and it is correspondent to a system with C/O=0.01. For an inlet temperature equal to 1500K it is 5200 for a C/O feed ratio equal to 0.01 and it is 19500 for $T_{in}=1800K$ and again.
C/O=0.01. Hence the highest value corresponds to very lean mixture, since the stochiometric value is equal to 0.25.

These values should be compared with the ones that establish in the system that will be used to perform study in the Mild Combustion condition. Hence, it is necessary to calculate the strain rate characteristic of the jet in cross-flow configuration.

In literature there are several works on diffusion flames (Riechelmann D. et al, 2002). A counter-flow diffusion flame can be established in the forward stagnation region of a porous cylinder immersed in a uniform air stream, by ejecting a fuel gas uniformly from the cylinder surface (Tsuiji, 1982). The equation used in these works for the calculation of the velocity gradient is $2V/R$, where $V$ is the velocity of the main flow and $R$ the radius of the porous cylinder. If it is assumed that the jet can be schematized with a rigid cylinder, at least in the first part of the injection, it is possible to use this equation is valid.

Considering that in the real system the velocity of the main flow is about 45 m/sec and that the jet has a diameter of 0.8 mm, the gradient of velocity is of the order of $1\times10^5$ sec$^{-1}$.

The estimate of this value has been done also by means of the commercial fluid-dynamic code Fluent 6.2.1.

In 3D Cartesian coordinates, the strain rate, $\mathbf{S}$, is defined as:
The simulations have been run enabling the energy equation, the
turbulent $\kappa - \omega$ (kinetic energy-specific dissipation rate) model and the Species models.
The turbulent $\kappa - \omega$ model is widely used for round and radial jets and the species model allows for simulating the mixing and transport of chemical species by solving conservation equations, hence describing convection, diffusion, and reaction sources for each component species. In these simulations, the reaction model has not been enabled since the attention has been focused just on the strain rate values.

Figure 5.27 shows the critical strain rate in a section of the tubular flow reactor located in the plane $z=0$ for several inlet temperatures. The jet in cross-flow configuration considered in this analysis presents 6 nozzles with a inner diameter equal to 0.8mm. The jet velocity is 100 m/sec while the inlet main stream velocity is 45 m/s. The jet is composed by methane, nitrogen and helium in equal-molar fraction, while the main flow by oxygen and water steam. The compositions are set in such a way that, after the system has reached the species mixing, the mixture is diluted at 90% with water, nitrogen and helium while the remaining part is composed by methane and oxygen that represent the 10% of the mixture. The main stream enters the reactor with an inlet temperature equal to 1300K, 1500K and 1800K, whereas the lateral stream enters the main duct at 500K.
**Strain rate, 1/s**

![Diagram showing strain rate on a section of the tubular flow reactor for T_{in} = 1300K, 1500K and 1800K.]

**Figure 5.27** Strain rate on a section of the tubular flow reactor for T_{in} = 1300K, 1500K and 1800K.

The geometry of the duct has been drawn taking into account the reactor design. There is a first duct 10 cm long with a diameter of 1.4 cm, then the convergent section with an angle of 26.6° since, as reported in a previous work, it is an efficient geometry. The second duct is just 5 cm long since the attention was focused just on the mixing. Edges, surface and volume are meshed employing respectively the Successive Ratio grading scheme, the Tripave face-meshing scheme and the Tetrahedral volume meshing scheme.

It is evident that the strain rates values are similar in the three cases. In particular the highest values are reached in the proximity of the jets entrance and in the near-wall region of the convergent.

The strain rates values are reported in a logarithmic scale sub-divided in 100 levels. The scale goes from 1 to about 3*10^{19}.

Fig. 5.28 plots the strain rate values as function of the axial coordinate on the axis of
the reactor. In any analyzed case, the critical strain rate is very similar, hence here, it is just reported a single profile as representative of all the three cases. The strain rate increases for an axial distance equal to 10 cm, hence at the beginning of the convergent. It reaches a value of about $1 \times 10^4$ and than it drops towards a value of about $10^{-3}$.

Figure 5.28  Strain rate profile as function of the axial coordinate on the axis of the reactor.

The axial position has been chosen since it is a critical position, in fact here there are the lowest strain rate values in the reactor. Hence in this region it can be possible the insurgence of the oxidation reaction.

This is evident in figure 5.29 where the strain rate has been plotted, on a logarithmic scale, along a diameter of the duct in the plane $z=0$, and an axial position equal to 9.3, 9.6, 9.8 and 10 cm. Hence, in this analysis it has been considered the axial position from the injection plane to the end of the main cylindrical duct.

At $x=9.3$ cm, in the injection plane, the highest strain rate values are in the region near the nozzles, here the strain rate reaches $2.3 \times 10^5$ sec$^{-1}$, but in the central section it presents the lowest value, about 1500 sec$^{-1}$, in comparison with the other axial position chosen for this analysis. It is worth noting that as the axial distance is increased the strain rate values become more and more slow in the near-wall region and they increase in the
central part of the duct thus the profiles tends to be flatter and flatter.

At \( x=10\text{cm} \) the slowest values is about 9000 and anyway it relative to a point in the center of the duct, whereas the highest value, in the near-wall region, is \( 4\times10^{-4} \).

![Figure 5.29](image)

**Figure 5.29** Strain rate profile as function of the axial coordinate on the axis of the reactor.

Both the analytic and numerical calculations of the strain rate lead to assess that the characteristic value of the strain rate, for the tubular reactor, is of about \( 10^5 \), hence it is rational to assume that this is the characteristic value for the tubular reactor. Therefore, this value is higher, in the area very close to the nozzles, of one order of magnitude than the maximum strain rate calculated by means of the ChemKin 3.7 software.

Even if this is just an estimate of these gradients of velocity, it indicates that an eventual insurgence of the oxidation reaction would be damped down by the high strain rates present in the mixing zone.

At the same time, for \( T_{\text{inl.}}=1300\text{K} \) and \( 1500\text{K} \), the strain rate values, obtained by the numerical integrations, are higher than the ones calculated by means of the software ChemKin, hence, in these cases, the insurgence of any oxidation reaction could be hindered by the too high flame stretching.


Study of the working conditions

The conditions in which the process of Mild Combustion could be characterized have been already indicated. The fuel is methane to avoid the complexity of higher hydrocarbons and the diluent will be vapor water.

The study can be performed as function of several parameters such as the inlet temperature, the composition of the reactants and the dilution degree. In particular the temperature range of interest is comprised between 1000K and 1800K, the Carbon/Oxygen feed ratio range goes from very lean to rich values (C/O=0.01-1), and the dilution level has been fixed equal to 90%.

It is anyway convenient to do a preliminary analysis in order to individuate the working conditions that are feasible for the plug flow reactor.

As matter of fact there are several limits that delimit the working conditions. First of all the auto-ignition time, as shown in the previous section, has to be higher than the mixing time. All the couple of parameters $T_{inlet}$-C/O feed ratio for which this condition is not respected have to be discarded.

Another constrain which can restrict the field of existence of the experimental conditions is the temperatures that are reached during the oxidation process. Although the increase of temperature is low in Mild Combustion processes in comparison with traditional processes, the temperature that cannot be exceeded is 2000K, since the materials that have been used to build the reactor can resist until this value. The choice of materials will be presented in another paragraph.

The last constrain comes from the axial dimension of the reactor. It has been fixed to 1 m. Hence an important parameter to assess is the length of the reaction zone during the oxidation reaction. It does not represent a very strict limit since the axial dimension of the reactor can be changed taking into account the practical constraint of a laboratory scale.
Therefore the maximum working temperature and the length of the reaction zone have to be assessed.

In order to perform this study the Plug configuration of the CHEMKIN 3.7 package has been used. Several numerical simulations have been run considering a plug flow reactor in adiabatic condition. This assumption makes the system working in the most stringent condition since the maximum temperature will be the adiabatic one. The kinetic mechanism used is the methane oxidation mechanism by Warnatz (1997).

**Adiabatic temperature**

The adiabatic temperatures for the system CH₄/O₂/N₂ and the system CH₄/O₂/H₂O are shown in Figures 5.30 and 5.31. They show the maximum temperatures reached during the oxidation reaction as function of the C/O feed ratio on parametric curves in T_{inlet}. For both the systems the molar fraction α of the diluent is 0.9.

![Adiabatic temperatures for the system CH₄/O₂/N₂ as function of the C/O feed ratio.](image)

**Figure 5.30** Adiabatic temperatures for the system CH₄/O₂/N₂ as function of the C/O feed ratio.
Although the simulations have been run for a wide range of $T_{\text{inlet}}$ (from 1000K to 1800K) the figures show the results obtained for $T=1300$K, $T=1500$K and $T=1800$K.

Obviously there is an increase of the adiabatic temperature for a fixed fuel/oxygen ratio as this value is close to the stochiometric condition (C/O=0.25).

In particular the adiabatic temperature is, for the same inlet conditions, always higher for the system CH$_4$/O$_2$/N$_2$. The $\Delta T$ are for the system diluted with water 536, 498 and 413K while for the other system they are 694, 638 and 597K. This is mainly due to the higher specific heat at constant pressure of the steam water. In fact the $C_p$ of water is respectively equal to 9.31, 9.6 and 10.1 cal/mole K, while $C_p$ of nitrogen is equal to 8.1, 8.3 and 8.6 cal/mole K for the three analyzed temperatures. Furthermore the differences between the $\Delta T$ for the same increment of the inlet temperature are for the former system 38K and 85K, for the latter system 56 and 41K. This difference is due to the observation that the specific heat at constant pressure of vapor water increases perceptually more than in the case of nitrogen.

![Adiabatic temperatures for the system CH$_4$/O$_2$/H$_2$O as function of the C/O feed ratio.](image)

*Figure 5.31* Adiabatic temperatures for the system CH$_4$/O$_2$/H$_2$O as function of the C/O feed ratio.
Anyway it could be caused also for the decomposition of water at high temperature that is note to be an endothermic reaction.

**Reacting zone**

The reaction zone \( \delta_{\text{reac}} \) is defined as the zone comprised between the axial position of the reactor in which the temperature is higher of 10K than \( T_{\text{inlet}} \) and the position in which the temperature is equal to the 90% of the adiabatic temperature. Figure 15 shows the reaction length on the plane \( T_{\text{inlet}}/\text{C/O} \). Obviously the axial distance comprised between the inlet of the reactor and the point in which the oxidation reaction occurs is proportional to the auto-ignition time. In order to obtain \( \tau_{\text{ign}} \) is sufficient to divide this axial distance by the velocity \( (v=100 \text{ m/s}) \).

The red part of the diagram indicates those inlet conditions for which the oxidation reaction is detected for an axial distance greater than one meter which represent a physical limit since the reactor is 1 meter long.

Figure 5.32 shows the \( \tau_{\text{ign}} \) and \( \delta_{\text{reac}} \) for the system \( \text{CH}_4/\text{O}_2/\text{N}_2 \). It is possible to note that the thickness of reaction and the auto-ignition time increase for any C/O feed ratios as the inlet temperature decreases. This is due to the decrease of the reactivity of the system as much as \( T_{\text{inlet}} \) is decreased.

For \( T_{\text{inlet}} \) equal to 1200K it is possible to see that the \( \tau_{\text{ign}} \) is longer for C/O=0.01 than for C/O=0.1 and also the thickness of the \( \delta_{\text{reac}} \) is higher. In fact as shown in a previous paragraph, \( \tau_{\text{ign}} \) has a minimum value for C/O equal about to 0.025, for lower C/O values it sharply goes up to higher values but for higher C/O ratios it slowly increases. This trend is more evident at low temperatures where the auto-ignition times are meaningfully different
from each other.

![Graph showing δ_reac for the system CH\(_4\)/O\(_2\)/N\(_2\).](image)

**Figure 5.32** \(\delta_{\text{reac}}\) for the system CH\(_4\)/O\(_2\)/N\(_2\).

The same trend is recognizable also for the system CH\(_4\)/O\(_2\)/H\(_2\)O as shown in figure 5.33. The difference between the two auto-ignition times is more evident at T=1200K. This agrees with the results obtained in the analysis of the auto-ignition time since as shown in figure 12, \(\tau_{\text{ign}}\) increases more sharply for the system CH\(_4\)/O\(_2\)/H\(_2\)O in comparison with the system CH\(_4\)/O\(_2\)/N\(_2\) for lean conditions on the left of the minimum value.
Numerical Simulation for the Mild Combustion Process in Methane Tubular Reactor in Stream of Nitrogen and Steam

Methane kinetic mechanisms have been widely employed for the characterization of the methane oxidation process in a perfect stirred flow reactor. They can be as well used to perform a preliminary analysis of the evolution of the combustion process in terms of temperatures and species concentration as function of the axial coordinate of the tubular flow reactor. The ChemKin package software is provided of an application, i.e. PLUG, that can simulate the behavior of plug flow reactor. It is worth underlining that reactants enter the reactor in pre-mixed conditions, hence there are no problem related to the mixing of reactants, and the velocity profile is assumed to be flat. Therefore no radial temperature
and species concentration are allowed. Furthermore no axial dispersion is forecasted in this model. Hence the oxidation process is described as function of the axial coordinate. The numerical integrations have been performed considering the experimental conditions that will be analyzed in the future, i.e temperatures comprised between 1000K and 1800K, and mixtures with a C/O feed ratio from values very close to zero to 1. The velocity of the inlet gas is 100 m/s and the reactor is 100 cm long. The oxidation of methane, in a system diluted up to 90% with steam water or nitrogen, occurs in adiabatic condition. Nitrogen has been considered in the simulations in order to compare the temperatures and species distributions relative to a system diluted with an inert species, to results obtained with steam water, in order to underline the chemical effect of the last diluent.

The model used for these simulations is the “Warnatz” methane oxidation mechanism.

The fig. 5.34 and 5.35 show results obtained for inlet temperatures equal to 1300K and 1400K for several C/O feed ratio (0.01-0.05-0.1-0.2-0.25-0.3-0.5-0.8-1). In particular the reactor temperature, the methane conversion, the CO₂, CO and C₂H₂ yields were plotted as function of the axial coordinate of the reactor on curves parametric in the C/O feed ratios.

For T=1300K the model forecasts that just lean mixtures (C/O=0.01, 0.05, 0,1) ignite. In particular the mixture with a C/O feed ratio equal to 0.01 ignites for an inlet distance of 50 cm and the temperature increase is relatively low, while the mixture with a C/O = 0.05 ignites for an inlet distance of 65 cm and reaches a working temperature equal to 1510K. The mixture with a C/O feed ratio equal to 0.1 ignites for an axial distance equal to 95 cm but does not reach a steady state before the end of the reactor. The oxidation reactions for the other analyzed mixture does not occurs in 100cm. The first results identify a clear trend: the higher is the C/O feed ratio, the longer is the ignition time delay but the
higher is the working temperature.

This trend is confirmed for an inlet temperature equal to 1400K. In this case the ignition delay time shorten for the analyzed mixtures and the oxidation reaction occurs for mixtures with a C/O feed ratio up to the stoichiometric value (C/O=0.25). The conversion of methane is unitary in any case. The CO and C$_2$H$_2$ concentration increase during the transitory of the system but go quickly down to zero when the system reaches a stationary value. In correspondence of the CO and C$_2$H$_2$ concentration decrease the CO$_2$ abruptly increases and methane fully converts in CO$_2$. Figures 4.5 and 4.6 show the behavior of the system for inlet temperatures equal to 1500K and 1600K. In this first case ignition occurs for mixtures with a C/O feed ratio up to 0.5. It is possible to note that for this mixture the temperature increase is lower than the one corresponding to the stoichiometric mixture, the methane conversion does not reach the unitary value, and the main products are CO and acetylene. For T$_{\text{inlet}}$=1600K all the mixtures ignite. In particular the lowest ignition delay time competes to lean mixtures, while the stationary temperature increases with the C/O feed ratio, until the stoichiometric value, whereas for rich mixtures it decreases.
Figure 5.34  Numerical simulations of the Mild combustion process in a tubular reactor for the system CH$_4$/O$_2$ diluted in N$_2$ up to 90% for inlet temperatures equal to 1300K and 1400K and different C/O feed ratios.
Figure 5.35  Numerical simulations of the Mild combustion process in a tubular reactor for the system CH$_4$/O$_2$ diluted in N$_2$ up to 90% for inlet temperatures equal to 1500K and 1600K and different C/O feed ratios.
Figure 5.36  Numerical simulations of the Mild combustion process in a tubular reactor for the system CH₄/O₂ diluted in N₂ up to 90% for inlet temperatures equal to 1700K and 1800K and different C/O feed ratios.
Furthermore the richer the mixture is, the lower is the methane conversion while the higher is the carbon monoxide and acetylene yields.

The same considerations apply for system pre-heated up to 1700K and 1800K.

The dilution with steam water present the same characteristic discussed for the system diluted in nitrogen

But the effect of water is evident if the methane conversion and yields are compared for the two systems in the same operative conditions. Steam presence induces higher methane conversion degree, higher CO$_2$ concentration and lower C$_2$H$_2$ and CO production.

The description of the water effects on the combustion of methane in Mild conditions confirms results that have been obtained on the CSTR configuration, hence in this paragraph they have not been properly discussed. For further information we remand to the numerical results obtained in the other model reactor.
Figure 5.37  Numerical simulations of the Mild combustion process in a tubular reactor for the system CH$_4$/O$_2$ diluted in H$_2$O up to 90% for inlet temperatures equal to 1300K and 1400K and different C/O feed ratios.
Figure 5.38  Numerical simulations of the Mild combustion process in a tubular reactor for the system CH₄/O₂ diluted in H₂O up to 90% for inlet temperatures equal to 1500K and 1600K and different C/O feed ratios.
**Figure 5.39**  Numerical simulations of the Mild combustion process in a tubular reactor for the system CH$_4$/O$_2$ diluted in H$_2$O up to 90% for inlet temperatures equal to 1700K and 1800K and different C/O feed ratios.
Numerical Simulations on the simplified configuration for the study of the fluid-dynamic of the mixing section

In the next chapter the efficiency of the mixing zone will be valued by means of optical techniques applied on a simplified configuration that works at environmental temperature.

Its geometry and dimensions reproduce in a rational way the main features to the tubular reactor that will be used for the study of Mild Combustion processes. Such a configuration will be described well in the following chapter.

In such a way, the study of the fluid-dynamic field of the tubular reactor at environmental temperature will be performed focusing the attention on the mixing of the jet in cross-flow configuration chosen for the realization of the real reactor.

The study of the fluid-dynamic field in the reactor can be tentatively performed by means of CFD commercial codes such as Fluent. Hence in this paragraph it will be shown the numerical results obtained by means of Fluent 6.1. The working conditions used for the numerical simulations reproduce the real operative ones that will be used on the simplified configuration. They will be presented later in the same paragraph.

The geometry used in the simulations reproduce the reactor one. Hence there is a first duct with an inner radius (Rt) equal to 0.7cm and a length of 10cm. The last dimension is nor really restrictive but it is used since, in order to have a well developed motion of the fluid inside the duct, it is needed an axial length longer more than approximately 7-10 times the inner radius of the duct. At radius distance from the outlet of the cylindrical duct there are the injectors. The round, equally spaced injectors are displaced on the perimeter of the cylindrical duct.

At the end of the first section there is a convergent which leads the radius from 0.7cm to 0.5 cm. The axial length of the second section is 0.4cm and hence it is
characterized by a slope of 26°.

After the convergent there is the second cylindrical duct that represents the third section. It has a inner diameter equal to 1 cm and a length of 10cm, since this numerical analysis is focused on the study of the mixing of reactants.

The fig.5.39 shows a sketch of the system and it clearly indicates the position of origin axes.

The numerical analyses differ from the ones presented in the previous paragraph for two main reasons. The former is the position of the system of reference since its origin is located at the beginning of the third section and not at the injection section. The latter difference is the composition of the mix, and the main and secondary flows temperatures.

Figure 5.39   Sketch of system and position of the origin axes.

In the simplified configuration the main flow is composed by air while the injected flow by helium and acetone. More thoroughly helium gurgles in an acetone bath and than together are injected inside the main duct trough the injectors where they mix with air. The acetone has been used as tracer for fluorescence measurements that will be realized for the study of the mixing degree.

The choice of air responds to an economical requirements since the availability of compressed air in the lab. As matter of fact, the main flow represents the 90% of the total flow and, since the test have been run at environmental temperature, the flow rate is not negligible.
The helium has been selected since the need of having the same values of the parameter $J$ that characterize the tubular reactor keeping equal the velocity of the main and lateral flows in the two different configurations. Hence in the simulation the air velocity is equal to 45m/s, while the velocity of lateral jets will vary in a range of values that will be really close to the ones reachable in the real system.

The simulations will be focused on several geometries of the mixing section that will be characterized by the number $(n)$, the diameter $(d)$ and the protrusion $(p)$ of the injectors in the main duct.

In particular the number of injectors will be set equal to 6 and 10, while the injectors will be located at a radial distance from the axis of the first section equal to 7mm ($p=0$) and 6mm ($p=1$).

For any geometry several values of the momentum of the flows $J$ will be studied considering lower values as well as higher values in comparison with the Holdeman optimal momentum of the jet to main flow ratio $J_{Hopt}$.

Therefore, the main flow velocity will be 45m/sec and the temperature will be 300K. Any desired value of $J$ is obtained changing the flow rate of the lateral jet while its composition is calculated considering that at environmental temperature the helium flows is saturated by acetone. It leads to a change of the concentration of the tracer in according with the different working condition analyzed. It will make necessary a normalization of the acetone molar fraction in order to compare the geometries analyzed in this chapter.

10 injectors located on the wall of the cylindrical duct

The first analysed geometry presents 10 injectors with an inner diameter equal to 0.5mm. They are equally displaced on the perimeter of the cylindrical duct at 36° of distance from each other.

In this case the optimal value of the momentum of the jet to main stream ratio $J$
according to Holdeman equations is equal to 32 \( (J_{\text{Hopt}}) \). The numerical simulations have been run for a wide range of \( J \), from 8 to 80, in such a way it was possible to analyzing the mixing in a wide range of conditions. If fact the analyses have been realized for \( J \) values lower and higher than the \( J_{\text{Hopt}} \).

The working conditions are reported in tab. 5.1, where the velocity of lateral jets \( (V_{\text{inj}}) \), and the helium \( (Y_{\text{He}}) \) and acetone \( (Y_{\text{C3H6O}}) \) mass fraction are reported.

<table>
<thead>
<tr>
<th>( J )</th>
<th>( V_{\text{inj}} )(m/s)</th>
<th>( Y_{\text{C3H6O}} )</th>
<th>( Y_{\text{He}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>167.49</td>
<td>0.826</td>
<td>0.174</td>
</tr>
<tr>
<td>10</td>
<td>203.05</td>
<td>0.821</td>
<td>0.179</td>
</tr>
<tr>
<td>16</td>
<td>238.71</td>
<td>0.815</td>
<td>0.185</td>
</tr>
<tr>
<td>20</td>
<td>273.35</td>
<td>0.813</td>
<td>0.187</td>
</tr>
<tr>
<td>26</td>
<td>310.51</td>
<td>0.807</td>
<td>0.193</td>
</tr>
<tr>
<td>32</td>
<td>354.85</td>
<td>0.791</td>
<td>0.209</td>
</tr>
<tr>
<td>38</td>
<td>386.75</td>
<td>0.795</td>
<td>0.205</td>
</tr>
<tr>
<td>45</td>
<td>433.36</td>
<td>0.778</td>
<td>0.222</td>
</tr>
<tr>
<td>53</td>
<td>469.69</td>
<td>0.778</td>
<td>0.222</td>
</tr>
<tr>
<td>62</td>
<td>505.03</td>
<td>0.778</td>
<td>0.222</td>
</tr>
<tr>
<td>70</td>
<td>570.02</td>
<td>0.746</td>
<td>0.254</td>
</tr>
<tr>
<td>80</td>
<td>588.26</td>
<td>0.767</td>
<td>0.233</td>
</tr>
</tbody>
</table>

*Tab. 5.1  Velocity and mass fraction of the lateral flows for the configuration with 10 nozzles with a inner diameter equal to 0.5 mm.*

The results of the numerical simulation are presented in fig. 5.40. The acetone distribution inside the system is reported in molar fraction on a colored scale subdivided in 30 levels. The molar fraction goes from 0 to \( 5 \times 10^{-2} \). The acetone distribution is shown on a longitudinal section of the reactors and on several cross section located at \( x=1 \)mm, \( x=1 \)cm and \( x=2 \) cm from the end of the convergent.

The acetone concentration is reported as function of the parameter \( J \). Observing the sequence of images it is possible to note that jets penetrate increasingly more inside the
main duct as $J$ increases.

It is possible to perform two different analyses on the acetone distribution: the former concerns the variation of the uniformity of the mixing as function of $J$ on several cross sections; the latter regards the variation of the uniformity of the mixing as function of $J$ along the axial direction. In the discussion of the results the analysis of the acetone distribution is carried on taking as reference value an acetone mole fraction equal to $1 \times 10^{-2}$. In particular, a molar fraction lower than this threshold indicates that the acetone concentration is very low.

Observing the cross section located at $x=1\text{mm}$ and $J=8$ it is possible to note that the concentration of acetone at the center is very close to zero, or better lower than 0.01, it increases in the radial direction and it has its maximum in the proximity of the wall. As soon as the value of $J$ increases, the central core decreases and it finally disappears for $J=53$. Anyway a central core with a lower concentration of acetone persists. The disuniformity at $x=1\text{mm}$ is significantly reduced for $J=80$ where the central core with a lower concentration is very small.

A similar trend can be found out performing the same analysis on the cross at $x=1\text{cm}$. From $J=8$ to $J=32$ there is a small central core with no acetone. From $J=38$ to $J=53$ the concentration of acetone is, in any point of the cross section, higher than 0.01 but the distribution indicates that there is not an homogeneous mixing. For $J$ values higher than 53 the mixing configuration seems to guarantee a good distribution of acetone inside the duct.

For the cross section located at $x=2\text{ cm}$ it is evident that in any case there not exists a core with no acetone even if a good mixing is guaranteed for values of the momentum of jet to stream ratio higher than 26.

The second analysis concerns the study of the variation of the mixing as function of $J$ along the axial direction.
For $J=8$ it is possible to see that for $x=1\text{mm}$ the central core has a concentration very close to zero, the same consideration appalls for $x=1\text{cm}$ but not for the section located at 2cm from the convergent. In this case a good mixing is not still reached but the acetone molar fraction is not still lower than 0.01. The same considerations apply for $J$ comprised in the range 8-20. The only difference is that the central core with no acetone diminishes as $J$ increases.

For $J=26$ and $J=32$ at the first analyzed cross-section ($x=1\text{mm}$) It is still visible a core with a concentration lower that 0.01. At $x=1\text{cm}$ the core with no acetone persists but it disappears for $x=2\text{cm}$ and the system reaches a good mixing degree.

For $J=38$, at the axial distance equal to 1mm, it is still recognizable a core with a very low acetone concentration but already in the cross section placed at $x=1\text{cm}$ it disappears. Finally, a good mixing is reached in the last cross section section ($x=2\text{cm}$).

The same discussion is valid for $J$ values until 53, with the consideration that increasing $J$ the dimension of the internal core decreases.
Figure 5.40 Acetone Molar Fraction distribution along the plane $x=0$ and on different cross sections at fixed $x$ values.
Figure 5.41  Acetone molar fraction profiles along the the diameter of the duct in the plane $z=0$ as function of $J$ at different axial locations.
For \( J = 62 \), \( J = 70 \) and \( J = 80 \) in the section at \( x = 1 \text{mm} \) it is not identifiable a core with an acetone molar fraction lower than 0.01 but a not uniform acetone distribution that is reached on the last section analyzed.

Therefore the simulations suggest that for \( x = 1 \text{mm} \) it is not possible to reach a good mixing degree but there is always a core where the concentration of acetone is lower in comparison with the other radial positions.

In fig. 5.41 it is shown the molar concentration of acetone along a diameter of the radial section located at \( z = 1 \text{mm}, z = 1 \text{cm} \) and \( z = 2 \text{cm} \) from the convergent.

These profiles suggest similar considerations about the mixing of the species inside the configuration. In particular any image shows the acetone molar fraction for the three chosen position. It comes out that for any \( J \) in the range analyzed it is possible to reach a good distribution of acetone for an axial distance from the convergent equal to 1mm.

For \( z = 1 \text{cm} \) a value of the momentum jet to stream ratio \( J \) equal to 53 ensures a flat profile as well as a value of \( J \) equal to 26 is sufficient for a good distribution of the acetone for an axial distance from the convergent equal to 2cm.

![Figure 5.42](image)  
**Figure 5.42** Standard Deviation of the acetone molar fraction along a diameter of the duct as function of the parameter \( J \) on curves parametric in the axial position \( x \).
By following the indication reported in literature by Holdeman (1992), the efficiency of the mixing device has been evaluated by means of the *Standard Deviation (StD)* of the concentration of acetone along a diameter of duct. In fig. 4.5.3 it is shown the mixing disuniformity as function of the parameter \( J \), calculated by means of the *Standard Deviation (StD)*, for \( x=1\text{mm} \), \( x=1\text{cm} \) e \( x=2\text{cm} \). The \( \text{StD} \) gives an indication of the uniformity of mixing along the reactor diameter. In general the lower the StD is, the more uniform the acetone concentration is.

The \( \text{StD} \) is calculated by this formula:

\[
\text{StD} = \sqrt{\frac{\sum_{i=1}^{N} (q_i - \bar{q})^2}{N}} \tag{4.5.1}
\]

where \( q_i \) are the normalized values of acetone molar fraction with the mean value of each profile and any axial distance, while \( \bar{q} \) is the mean value of the \( q_i \), \( N \) the number of point in the concentration profile.

In fig 5.42 it is possible to see that the \( \text{StD} \) goes from values equal to 0.08 to 0.35. Holdeman (1992) in his analyses estimated that when the *Standard Deviation* is lower than 0.1 the system has reached a good mixing degree.

Hence it is possible to assess that whether the \( \text{StD} \) is lower than 0.1 the mixing disuniformity is negligible as well whether the \( \text{StD} \) is lower than 0.2 the mixing is not perfect but anyway it is satisfactory.

From fig.4.5.3 it is evident that a perfect mixing (\( \text{StD}<0.1 \)) is reachable for the cross section sited at \( x=1\text{cm} \) and \( x=2\text{cm} \) for values of the parameter \( J \) respectively higher than \( J=53 \) and \( J=26 \) while for the cross section located at \( x=1\text{mm} \) it is not possible to have a good mixing for any of the values of \( J \) analyzed in the paragraph.
6 injectors located on the wall of the cylindrical duct

The second analyzed geometry presents 6 injectors with an inner diameter equal to 0.8 mm. They are equally displaced on the perimeter of the cylindrical duct at 60° of distance from each other. The Holdeman relations indicate that in this case the optimal value of the momentum of the jet to main stream ratio $J$ is equal to $11(J_{\text{opt}})$. The numerical simulations have been run for a wide range of $J$, from 3.5 to 30, in such a way it was possible to analyzing the mixing in a wide range of conditions. As previously described, the values of $J$ are varied changing the velocity of the lateral jets. The working conditions are reported in tab. 5.2, where the velocity of lateral jets ($V_{\text{inj}}$), and the helium ($Y_{\text{He}}$) and acetone ($Y_{\text{C3H6O}}$) mass fraction are reported.

<table>
<thead>
<tr>
<th>$J$</th>
<th>$V_{\text{inj}}$ (m/s)</th>
<th>$Y_{\text{C3H6O}}$</th>
<th>$Y_{\text{He}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.5</td>
<td>106.83</td>
<td>0.839</td>
<td>0.161</td>
</tr>
<tr>
<td>5</td>
<td>128.21</td>
<td>0.839</td>
<td>0.161</td>
</tr>
<tr>
<td>6.5</td>
<td>155.72</td>
<td>0.813</td>
<td>0.187</td>
</tr>
<tr>
<td>9</td>
<td>179.69</td>
<td>0.807</td>
<td>0.193</td>
</tr>
<tr>
<td>11</td>
<td>184.24</td>
<td>0.866</td>
<td>0.134</td>
</tr>
<tr>
<td>13</td>
<td>231.02</td>
<td>0.79</td>
<td>0.209</td>
</tr>
<tr>
<td>16</td>
<td>256.44</td>
<td>0.784</td>
<td>0.216</td>
</tr>
<tr>
<td>19</td>
<td>287.24</td>
<td>0.767</td>
<td>0.233</td>
</tr>
<tr>
<td>22</td>
<td>316.49</td>
<td>0.754</td>
<td>0.246</td>
</tr>
<tr>
<td>26</td>
<td>346.48</td>
<td>0.746</td>
<td>0.254</td>
</tr>
<tr>
<td>30</td>
<td>383.08</td>
<td>0.725</td>
<td>0.275</td>
</tr>
</tbody>
</table>

Tab. 5.2  Velocity and mass fraction of the lateral flows for the configuration with 6 nozzles with a inner diameter equal to 0.8mm

The results of the numerical simulation are presented in tab.5.2. The acetone distribution inside the system is reported in molar fraction on a colored scale subdivided in 30 different levels. The molar fraction goes from 0 to $5 \times 10^{-2}$. The acetone distribution is
shown on a longitudinal section of the reactors and on several cross section located at x=1mm, x=1cm and x=2 cm from the end of the convergent. The numerical results have been resumed in fig. 5.43.

Observing the cross section located at x=1mm from the convergent it is possible to note that for J=3.5 the concentration of acetone at the center is very close to zero, or better lower than 0.01, it increases in the radial direction and it has its maximum in the proximity of the wall. As soon as the value of J increases, the central core with a acetone molar fraction lower than 0.01 decreases and it finally disappears for the J_{\text{Hopt}}. For J=22 the central core is almost not discernible from the surrounding area.

Likewise, the cross section located at 1cm from the convergent clearly shows that for J=3.5 and J=6.5 the extension of the central core with no acetone reduces significantly.

For J=9 and J=11 the zone with the acetone concentration lower than 0.01 disappears, but the acetone distribution does not indicates a uniformity pattern. For J higher than 13 the mixing seems to be good.

At the cross section located x=2cm there is anymore the zone where the acetone concentration is lower than 0.01, for any of the J analyzed, but until J=5 there is just a central core with a lower concentration respect to the surroundings. Moreover from J=6.5 a good mixing of the species is reached.

The second analysis concerns the study of the variation of the mixing as function of J along the axial direction.

For J=3.5 and the cross section located at x=1mm the central core shows an acetone concentration very close to zero, this situation remains in the cross section located at 1 cm from the convergent but it is not verifiable in the last cross section sited at x=2cm, where the distribution of acetone is not still uniform but the acetone molar fraction is higher than the threshold value.
Figure 5.43  Acetone Molar Fraction distribution distribution along the plane $x=0$ and on different cross sections at fixed $x$ values.
6 injectors

Figure 5.44 Acetone molar fraction profiles as function of $J$ along diameters of the duct located in the plane $z=0$ at different axial locations.
The same considerations apply for $J=5$, with the difference that comparing the cross sections with the ones just discussed, the central core is narrower and shorter.

For $J=6.5$ in the cross section located at 1mm from the convergent, it is still evident a core with $X_{\text{CH}_3\text{O}}<0.01$. At the section located at $x=1\text{cm}$, the core with $X_{\text{CH}_3\text{O}}<0.01$ remains even if it is narrow, while in the section located at $x=2\text{cm}$ both the core with acetone low concentration and any disuniformity disappear hence the system seems to reach a good mixing degree.

For $J=9$ in the first cross section the central core with a low acetone concentration persists, whereas already in the section at 1cm from the convergent such a core disappears, but a good mixing is reached just in the last cross section located at $x=2\text{cm}$.

For $J=11$ in the first cross section it is not visible a core with $X_{\text{CH}_3\text{O}}<0.01$ but just a disuniformity in the distribution of acetone that fully disappears in the section located at 2cm from the convergent.

From $J=13$ to $J=19$ the mixing of the species is reached in the sections located at 1cm and 2cm while in the first section a central core persists but the acetone molar fraction is higher than 0.01.

From $J=22$ to $J=30$ the system reached a perfect mixing in any cross section considered in this analysis.

The consideration from the analyses relative to the uniformity of distribution of acetone as function of the parameter $J$ along the axial and radial directions, can be evicted also analyzing the acetone molar fraction profiles along the diameter of the duct in the plane $z=0$ as function of $J$ at different axial locations. The figure 5.44 reports the profiles for any $J$ and any axial distance chosen for these analyses.

Also in this case it is possible to see that the acetone molar fraction profile becomes increasingly flatter both increasing the values of the parameter $J$, once the axial position
has been fixed, or increasing the axial distance from the convergent for any value of $J$.

For values of the momentum of the jet to stream flow $J$ equal to 22, 13 and 6.5, a flat profile is reachable for an axial distance equal respectively to 1 mm, 1 cm and 2 cm.

In fig. 5.45 it is possible to note that a molar fraction of acetone higher than 0.01 at the cross section located at $x=1$ mm is reached for a value of $J$ equal to $J_{\text{opt}}$. In the cross section located at $x=1$ cm the same condition is verified for $J>6.5$. The acetone molar fraction is never lower than 0.01 in the cross section located at $x=2$ cm.

![Diagram](image)

**Figure 5.45.** Standard Deviation of the acetone molar fraction along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position $x$.

Figure 4.5.6 shows Standard Deviation of the acetone molar fraction along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position $x$.

It is possible to note as a uniform distribution of acetone (StD<0.1) is reachable for $x=1$ mm, $x=1$ cm e $x=2$ cm for values of $J$ respectively equal to 22, 13 and 6.5.

*6 injectors located inside the cylindrical duct with a protrusion of 1 mm*

The third analyzed geometry presents 6 injectors with an inner diameter equal to 0.8
mm. They are equally displaced on the perimeter of the cylindrical duct at 60° of distance from each other. The 6 nozzles protrude of 1 mm inside the main cylindrical duct. Hence this geometry is equal to the one examined in the previous paragraph except for the nozzles position.

Therefore Holdeman the optimal momentum of the jet to main stream ratio $J$, according to the literature, is equal to $11(J_{\text{opt}})$. The numerical simulations have been run for $J$ from 3.5 to 30.

The results of the numerical simulations are presented in fig. 5.46. The acetone distribution inside the system is reported in molar fraction on a colored scale subdivided in 30 different levels. The molar fraction goes from 0 to $5\times10^{-2}$. The acetone distribution is shown on a longitudinal section of the reactors and on several cross section located at $x=1\text{mm}$, $x=1\text{cm}$ and $x=2\text{cm}$ from the end of the convergent.

Also in this case it is possible to perform two kinds of analysis: the former concerns the variation of the mixing uniformity as function of the parameter $J$, in the radial direction, the latter along the axial direction.

Considering the cross section located at $x=1\text{mm}$, it is possible to see, for $J=3.5$, that the acetone molar fraction $(X_{\text{CH}_3\text{O}})$ is lower than 0.01 in the center of the section, but it increases in the radial direction and reaches its maximum in the near-wall region.

As the value of $J$ is increased, the zone where the concentration of acetone is lower than 0.01 diminishes and it almost disappears for $J=9$. For $J=11$ the acetone molar concentration $X_{\text{CH}_3\text{O}}$ in the near-wall zone is equal to the one in the center of the section. But the higher concentration is reached in the zone comprised between the center and the near-wall zone. This is a case of over-penetration of the jets. For values higher than 11, jets over-penetrates inside the duct and they for a central core with a very high acetone concentration but in the near-wall region the acetone molar fraction is lower. In the cases
$J=26$ and $J=30$, the acetone molar fraction is significantly higher in the center of the duct in comparison with the surroundings region.

In the cross section located at $x=1\text{cm}$ the acetone molar fraction is never lower than 0.01. For $J=3.5$ and $J=5$ in the center of the cross section shows a region with a lower acetone concentration. For $J>6.5$ the acetone distribution is more uniform in the section considered, although there in the near-wall region the acetone tends to vanish as $J$ increases. For $J=26$ and $J=30$ the concentration of acetone in the center of the section is significantly higher in comparison with the rest of the section.

Considering the cross section located at $x=2\text{cm}$, it is possible to see that just for $J=3.5$ the acetone concentration is lower in the middle of the section in comparison with the rest of the section. For $J>5$ the mixing is to be considered even if the acetone tends to accumulate in the center of the second cylindrical duct, until $J=26$ and $J=30$, where a small central core presents a concentration significantly higher than in the rest of the section.

The second analysis concerns the study of the variation of the mixing as function of $J$ along the axial direction.

Taking into account again $J=3.5$, it is possible to note that at an axial distance equal to 1mm from the convergent, there is a central core with a low acetone concentration and an intermediate section where the concentration is higher in comparison with the near-wall region. This condition does not persist for an axial distance equal to $x=1\text{cm}$ and $x=2\text{cm}$, although there is not a good distribution of the tracer because a small central core with a lower acetone concentration in comparison with the rest of the section persists.

For $J=5$ and an axial distance equal to 1mm it is still visible central core with acetone concentration $X_{\text{CH}_3\text{H}_6\text{O}}$ lower than 0.01 and there is an intermediate region where the $X_{\text{CH}_3\text{H}_6\text{O}}$ is higher in respect to the near-wall region. For an axial distance equal to 1 cm from the convergent, the core with a lower acetone concentration persists but $X_{\text{CH}_3\text{H}_6\text{O}}$ is higher than
0.01. For \( x = 2 \text{cm} \) the acetone distribution is to be considered homogeneous.

![Diagram of acetone molar fraction distribution along the plane \( x = 0 \) and on different cross sections at fixed \( x \) values.](image)

**Figure 5.46** Acetone Molar Fraction distribution distribution along the plane \( x = 0 \) and on different cross sections at fixed \( x \) values.
6 injectors located inside the cylindrical duct with a protrusion of 1 mm

Figure 5.47 Acetone molar fraction profiles as function of J along diameters of the duct located in the plane z=0 at different axial locations.
For \( J=6.5 \) at \( x=1\text{mm} \) it is still visible central core with acetone concentration \( X_{\text{CH}_3\text{O}} \) lower than 0.01 and there is an intermediate region where the \( X_{\text{CH}_3\text{O}} \) is higher in respect to the near-wall region. For \( x=1 \) and \( x=2\text{cm} \) the mixing can be considered good.

For \( J=9 \) at \( x=1\text{mm} \) a core with \( X_{\text{CH}_3\text{O}}<0.01 \) does not exist, even if the acetone accumulates in the intermediate region comprised between the center and the near-wall region. For the other two analyzed axial distances the species injected mix well with the main flow.

For \( J=11 \) there is for an axial distance from the convergent equal to \( 1\text{mm} \) a singular situation: the acetone concentration \( X_{\text{CH}_3\text{O}} \) is equal in the center and in proximity of the wall but it is higher in the intermediate region. For the other two axial positions here analyzed, the system reaches a good mixing degree.

For \( J=13 \) and \( J=22 \) in the section located at \( x=1\text{mm} \) the acetone does not spread in the near-wall region, while in the rest of the section the acetone distribution seems to be homogeneous. For \( x=1\text{cm} \) e \( 2\text{cm} \) the mixing appears uniform except in the region in the proximity of the wall, where the acetone concentration is lower. For \( J=26 \) and \( J=30 \) the presence of a core so highly rich in acetone at \( x=1\text{mm} \) entails that the same situation is re-proposed also for an axial distance equal to 1cm and 2 cm.

In fig.5.46 it is possible to see that the \( J \) higher, the higher the penetration of the jets is. In the cases \( J=26 \) and \( J=30 \) the over-penetration of the jet causes the formation of a central core with an high acetone concentration. This core persists for a long axial distance from the convergent.

Fig. 5.47 shows the numerical profiles of acetone molar fraction along a diameter of the duct located in the plane \( z=0 \), at an axial distance equal to \( 1\text{mm} \), \( 1\text{cm} \) and \( 2\text{cm} \), as function of the parameter \( J \). The study of these profiles suggest the same considerations that have been realized in the other analyses. In particular here it is evident that in the case
J=11 and x=1mm, the acetone concentration in the near-region wall and in the center is equal. Furthermore, it can be seen that from J=3.5 the acetone tends to accumulates in the intermediate region comprised between the center and the near-wall region. For J=26 and J=30 the profiles at x=1cm and x=2cm show that the acetone molar fraction values are higher in the central region of the duct in comparison with the rest of the section.

In fig.4.48 the Standard Deviation of the acetone molar fraction along a diameter of the duct as function of the parameter J on curves parametric in the axial position x.

The uniform mixing is not reachable at x=1mm, in fact the StD is never lower than 0.1. This is mainly due to the accumulation of the acetone in the zone comprised between the near-wall area and the center of the cylindrical duct for low values of J. As J increases the acetone concentration in the intermediate area tends to conform to the central zone and accumulates in the same area while the surrounding area becomes increasingly more segregated. At x=1cm the StD is lower than 0.01 for J values higher than J=5 and it shows a minimum for J=9. At x=2cm for any analyzed J values the StD is lower than 0.01 and the minimum is reached again for J=9.

![Figure 5.48](image)

**Figure 5.48** Standard Deviation of the acetone molar fraction along a diameter of the duct as function of the parameter J on curves parametric in the axial position x.
The figure 5.49 the acetone molar fraction profiles, normalized to their correspondent mean value, along a diameter of the duct in the plane \( z=0 \) for an axial distance from the convergent equal to 2 cm.

In this figure it is possible to see that for \( J=3.5 \) the acetone tends to accumulate in the near-wall region (\( q_{\text{C}_3\text{H}_6\text{O}}=1.05 \)) and the acetone normalized molar fraction is low (\( q_{\text{C}_3\text{H}_6\text{O}}=0.85 \)) in the center of the duct in comparison with the lateral concentration.

![Figure 5.49](image)

**Figure 5.49** Acetone molar fraction profiles, normalized to their correspondent mean value, along a diameter of the duct located in the plane \( z=0 \) at an axial distance from the convergent equal to 2 cm.

As \( J \) increases the acetone normalized molar fraction increases in the center of the duct but decreases in the near-wall region. For \( J=9 \) the acetone profile is almost flat and very close to the mean normalized value (\( q_{\text{C}_3\text{H}_6\text{O}} \equiv 1 \)) for any point of the diameter. For \( J=11, J=13 \) and \( J=30 \) the acetone normalized molar fraction values are higher than the unity (until \( q_{\text{C}_3\text{H}_6\text{O}}=1.07 \)) while in the lateral area they decreases until 0.92.

Therefore the value of the parameter \( J \) equal to 9 ensures the best mixing and the lowest values of the Standard Deviation.
Charter VI
Discussion

**Continuos Stirred Reactor**

In order to extensively describe the phenomenology detected in diluted oxidation of methane it is useful to analyze reactor temperatures in different conditions. To this aim experimental bifurcation diagrams obtained by fixing one of the continuation parameters considered above were represented in Figure 6.1, where reactor temperatures \( T_{R1} \) measured for C/O ratios of 0.8, 0.4 and 0.1 were reported as function of \( T_{inlet} \). Solid lines in the diagrams represent conditions where the system reaches a stable working temperature or the stable static branch, whereas dotted lines represent the maximum \( T_{max} \) and minimum \( T_{min} \) temperatures measured during oscillations, i.e. the periodic branch. Moreover in these diagrams the dashed line is used in order to extrapolate a possible unstable steady state in the region of hysteresis, not detectable by means of an experimental test.

The temperature profile measured for C/O=0.8 shows the typical “S” shape found in presence of a steady state multiplicity. The lower branch of temperature profile in the hysteresis region lies on isothermal line up to \( T_{inlet} = 875 \) K. For \( T_{inlet} = 925 \) K a temperature increase of about 10 K were recorded. In the same region the upper branch of the hysteresis is characterized by temperatures varying from 1000 K to 1100 K.

The difference between the reactor and the inlet temperature (\( \Delta T \)) is nearly constant up to \( T_{inlet} = 1150 \) K. On the contrary, starting form \( T_{inlet}= 1175 \) K the reactor temperature profile drops towards the isothermal line and for temperatures higher than 1225 K \( T_R \) is very close to the inlet temperature.
Such as also clear in the map reported in Figure 6.1, for C/O = 0.4, i.e. at leaner conditions, the hysteresis region slightly shifts towards higher temperatures and tightens up to disappear for C/O ratios lower than the stochiometric value.

Figure 6.1  Reactor temperature profiles as function of inlet temperature for dilution of 90%, \( \tau = 0.5 \) sec.

Also in this case the maximum temperature increase measured in the lower branch of hysteresis is of the order of 20 K. As it could be expected, the temperature of the upper branch is higher than the one collected in richer conditions. It increases from 1175 K to
1450 K for $T_{inlet}$ passing from 875 K to 1125 K, keeping nearly constant its trend up to the occurrence of stable periodic branch at 1150 K. For this $T_{inlet}$ the amplitude oscillation is about of 160 K. Both the maximum and the minimum temperatures measured during the oscillations decrease by increasing $T_{inlet}$. In the same way the oscillation amplitude weakens up to become of about 5 K at $T_{inlet} = 1225$ K. In contrast, the oscillation frequency increases with temperature passing from 0.25 Hz at $T_{inlet} = 1150$ K to 1.3 Hz at $T_{inlet} = 1225$ K. Such as it occurs at C/O = 0.8, starting from this inlet temperature, $T_R$ dramatically decreases towards the isothermal line. At $T_{inlet} = 1250$ K a stable static branch is again reached.

As already clear from the map of Figure 6.2, the bifurcation diagram of Figure 6.1 for C/O=0.1 does not show the hysteresis region. Also in this case the periodic stable branches show the amplitude oscillation decreasing with a temperature increase.

For rich conditions it was possible to identify in the ignition maps a curve composed by points at which the maximum temperature is reached in the reactor for a fixed C/O.

The dashed lines, which crosses the steady combustion region, reported in figure 6.2 identifies such loci. In the case of rich conditions, this value also corresponds to the maximum temperature increase ($\Delta T$) obtained during oxidation. On the right side of the dashed line, $\Delta T$ decreases with $T_{inlet}$ until a condition is reached at which it becomes independent of $T_{inlet}$ and reaches the nearly constant value of 50K, as is described more clearly in Figure 3. As shown in Figure 2a, $T_{inlet}$ corresponding to the maximum temperature is almost independent of C/O and is about 1175K.

When C/O is lower than 0.55, the system displays more complex behavior. For a $T_{inlet}$ that depends on C/O, steady combustion is replaced by a dynamic phenomenology, characterized by temperature oscillations never identified before in methane oxidation in the temperature range explored here. As can be seen from Fig. 6.2a, for C/O=0.55,
temperature oscillations occur in a range of 50K, from $T_{\text{inlet}}=1150$K up to 1200K. The oscillating temperature region is increased by decreasing C/O thus covering the temperature range between 1025K up to 1275K for the leanest C/O.

Figure 6.2 (T_{\text{inlet}}-C/O) experimental maps at 90% (a) and 85% (b) of dilution level for methane Mild oxidation.

The dependence of reactor temperature ($T_R$) on $T_{\text{inlet}}$ is re-proposed in the diagram in Figure 6.3 where reactor temperatures measured for C/O of 0.5 and 0.1 are reported as a function of $T_{\text{inlet}}$. In the figure the $C_2H_6$ and $C_2H_4-C_2H_2$ concentrations measured in the same experimental conditions of temperature profiles are also reported.

The temperature profile measured for C/O=0.5 shows the typical “S” shape found in the presence of a steady state multiplicity. The lower branch of the temperature profile in the hysteresis region lies on the isothermal line up to $T_{\text{inlet}}=925$K. For $T_{\text{inlet}}=975$K, a temperature increase of about 20K was recorded. In the same region, the upper branch of the hysteresis is characterized by a $T_R$ varying from 1129K to 1285K. $\Delta T$ is nearly constant up to $T_{\text{inlet}}=1150$ K. In this temperature range, $C_2H_6$ and $C_2H_4-C_2H_2$ concentrations...
increase with $T_{\text{inlet}}$. At $T_{\text{inlet}}=1150\text{K}$, $T_R$ reaches its maximum value, then drops towards the isothermal line and, for temperatures higher than $1225\text{K}$, it comes very close to $T_{\text{inlet}}$. In correspondence with the maximum temperature, the $C_2H_4-C_2H_2$ concentration becomes equal to $C_2H_6$. Interestingly, this occurs before the onset of oscillation. After that, $C_2H_6$ reaches a maximum and then becomes nearly constant whereas $C_2H_4-C_2H_2$ increases continuously up to $1275\text{K}$.

Different considerations apply to $C/O=0.1$, however. In this case both $C_2H_6$ and $C_2H_4-C_2H_2$ grow with temperature up to $T_{\text{inlet}}=1000\text{K}$ where they reach a maximum. At $T_{\text{inlet}}=1125\text{K}$, the temperature oscillations start and both $C_2H_6$ and $C_2H_4-C_2H_2$ decrease.

![Figure 6.3](image)

**Figure 6.3** Temperature temporal profiles at $C/O=0.1$ and $C/O=0.5$ and $T_{\text{inlet}}=1150\text{K}$ and $C_2$ samplings.

Other important information in the analysis of the methane oxidation in Mild conditions is provided by the sampling of the species $C_2$ as function of the parameter **residence –time**.

The figure 6.4 shows the temperature temporal profiles as function of the residence time discussed in the previous paragraph.
The trend of maximum temperature occurring during the oscillation is not directly related to the variation in heat transfer. For JSFR used in the present work both the mixing and the thermal flux are related to the fluid-dynamic conditions inside the reactor itself. In this case, for a fixed inlet temperature, a decrease in residence time corresponds to an increase of the inlet flow that in turn, leads to a higher overall heat transfer coefficient [9]. Therefore, the variation in heat transfer should affect the process by decreasing the working temperature with the residence time. On the contrary, the opposite trend has been pointed out during the experimental analysis.

![Graph](image)

**Figure 6.4** Temperature temporal profiles at C/O=0.2 (a) and C/O=0.4 (b) and $T_{\text{inlet}}=1150K$ for different residence times

The same phenomenology was evidenced by Gray et al. (1996) by studying the ethane oxidation in a continuous well stirred reactor. Although the residence times and the temperature range were very different from the conditions considered in the present work, the authors showed that in the cool flames region the temperature increase measured
during the oscillation decreased from 40K to 14K varying τ from 15 sec to 60 sec. This temperature decrease corresponded to an increase of oxygen conversion that passed from 87% at τ = 15 sec to 95% at τ = 40 sec. In this work the authors used a mechanically stirred reactor where the heat transfer coefficient does not depend on mass flow. As a consequence, also in this case it is not responsible for the temperature dependence on residence time.

Therefore, the relation between τ and the maximum temperature achieved during oscillation could be due to the increase of mass flow rate corresponding to a decrease in residence time.

In previous works it was supposed that the dynamical behavior evidenced during methane oxidation is due to the interaction between the kinetic of the methane oxidation and the thermal exchange between the reactor and the environment.

Although the chain branching of the CH₄ reaction mechanism is basically due to the H₂/O₂ system, methane evolves according two main pathways that are the oxidation and the recombination channels respectively. The rate of production analysis showed [2, 3] that recombination channel acts subtracting CH₃ radicals from the oxidation channel, storing them as C(2) compounds. When the chain branching starts, the recombination channel releases the CH₃ radicals through the formation of acetaldehyde and its dehydrogenation until the formation of CH₃CO radicals. These, in turn, are thermally decomposed, producing CH₃ radicals and CO that feed the oxidation channel enhancing the reactivity of the system and causing the temperature increase. Therefore, the recombination channel modulates the oscillation occurrence. The proper radical concentrations and temperature inside the reactor, that make the chain branching reactions related to the temperature oscillations start, do not depend on inlet flows. However, when the branching starts the lower the residence time is, the higher the mass flow rate is and therefore, the higher the
thermal power obtained. This leads to an increase of the maximum temperature reached during the oscillation. This also corresponds to a slight growth in C_{(2)} concentration, such as shown by the normalized ethane and ethene/acetylene concentration reported in Fig.6.5 as function of residence time.

![Normalized concentration profiles of C_{(2)} compounds as function of τ.](image)

Such an increase could be due to the temperature effect on competition between the two different kinetic paths. In fact, the higher temperature obtained at lower residence time could improve the recombination channel.

The same effect was obtained by increase the inlet temperature for a fixed residence time. This can be easily inferred on the basis of temperature profiles reported in Fig.6.6. They represent temperature reaction increases (ΔT) as function of C/O for T_{inlet} equal to 1025K, 1125K, 1225K. The dashed lines individuate the region where oscillations occur, showing the minimum and the maximum temperature measured during the oscillations themselves. For the highest inlet temperature the ΔT is independent from C/O ratio and the difference between the working and inlet temperature is of about 50K for rich mixtures (C/O > 0.25). Such limited temperature increase suggests that in these conditions the recombination channel is very active. Moreover, in this case it could be hypothesized that the C_{(2)} compounds are not oxidized to acetaldehyde leading to the formation of CH_{3} radicals, but they mainly form and accumulate as C_{2}H_{2}. In fact for temperature values...
higher than 1200K the acetylene becomes a relatively stable compound as explained in chapter II. Hence the reactivity of the system is dramatically lowered and the system does not reach high working temperatures.

\[ T_{\text{inlet}, K} \]

\[ \Delta T \]

Figure 6.6  Temperature increase (\( \Delta T \)) for dilution of 90\%, \( \tau=0.5 \) sec.

**Hydrogen Addiction Effect**

Some important characteristics of the effect of hydrogen addiction to the system \( \text{CH}_4/\text{O}_2/\text{N}_2 \) have not been put in results in chapter V, but they can be simply highlighted considered same comparisons between the experimental results.

Fig.6.7 shows the \( T_{\text{in}}-\text{C/O} \) map just presented in the previous paragraph and its “evolution” as function of the inlet hydrogen percentage.
Figure 6.24  Experimental ignition map indicating the dynamic behaviors region as a function of the inlet hydrogen percentage.

In this figure the ignition maps relatively to the system CH₄/O₂/N₂, with a global molar concentration of hydrogen respectively equal to 0%, 0.25% and 0.9% have been reported. The other ignition maps, obtained for the other hydrogen considered in this thesis, have not been reported since they do not add any further information about the system CH₄-H₂/O₂/N₂.

The first main effect of the hydrogen addiction is a reduction of the extension of the dynamic region in the C/O feed ratio range. In fact when hydrogen is fed into the system CH₄/O₂/N₂, the C/O feed ratio range, in which dynamic phenomenologies are detectable, narrows, in particular the maximum C/O feed ratio value reduces from 0.5 to 0.4, whereas the minimum one does not change.

Furthermore a slight reduction of the extension of the inlet temperature range can be detected even if, the most evident effect of hydrogen addiction is the shift of the dynamic
region of almost 25K towards lower inlet temperatures.

Moreover, for mixtures with a C/O feed ratio smaller than the stoichiometric value (C/O=0.25), the shift of the inlet temperature range is accompanied by a reduction of the extension of the region where the dynamic behavior takes place.

The experimental data show that the system is more sensitive to the presence of hydrogen than to the actual value of its concentration, hence in the just the mixtures at 0.25% and 0.9% have been reported because they exhaustively show the effect of the addiction of hydrogen to the CH₄/O₂/N₂ system.

Some other aspects of the hydrogen addiction can be emphasized considering the bifurcation diagrams.

In particular fig.6.8 reports the working temperature as function of the inlet temperature in parametric curves of the hydrogen molar percentages for a fixed carbon/oxygen feed ratio (C/O=0.7).

![Bifurcation Diagram](image)

**Figure 6.8**  **“Temperature drop” experimentally detected.**

For all the curves it is possible to recognize the same trend: there is a gradual increase of the reactor temperature, it reaches a maximum and then it drops towards the
inlet temperature line. Furthermore in all the analyzed cases, the difference between the working temperature and the inlet temperature reaches a constant value for very high inlet temperatures.

For low $T_{in}$, the final temperature increases as much as the molar fraction of hydrogen while for higher temperatures the final temperature decreasing by enhancing the hydrogen molar fraction. This is explainable considering that hydrogen promotes the conversion of methane at low temperatures but at the same time mixtures with hydrogen have a lower calorific power respect to the system CH$_4$/O$_2$/N$_2$.

Furthermore, as it has explained in the chapter V, the “temperature drop” has been explained by means of a thermodynamic analysis: the maximum $T$ identifies the condition from which acetylene becomes a stable product. Higher values of the inlet temperature involve a more significant production of recombination species. The dehydrogenation of these species to acetylene occurs via endothermic reactions. Moreover, acetylene is not oxidized hence the conversion of methane to CO$_2$ as well as the temperature gradient, is significantly lowered.

Moreover, as explained in chapter II, it is known that hydrogen addiction promotes the production of C$_2$ species, and in particular acetylene. It means that in rich conditions more acetylene is formed and, since it is a stable product for high temperature, the C and H atoms are stored as C$_2$H$_2$ and the oxidation channel, is not consequently fed, hence the reactivity of the system and the reactor temperature become relatively low.

The other behavior that is evidently affected by the presence of hydrogen is the “temperature drop” line. The “temperature drop” is detectable for all the rich mixtures experimentally analyzed and for the several mixtures considered, hence the “temperature drop” lines have been reported also in the $T_{in}$-C/O maps. Figure 6.9 shows the ignition maps and the “temperature drop” line obtained addicting hydrogen to the system.
CH₄/O₂/N₂ in several amounts.

Figure 6.9 Experimental ignition maps and “temperature drop” lines for the systems $CH_4H_2/O_2/N_2$ with different hydrogen concentrations.

Dotted lines identify the loci at which the maximum temperature increase ($\Delta T$) is reached in the reactor due to the oxidation process, for a fixed C/O value. The double-dotted line is relative to the system CH₄/O₂/N₂. The inlet temperature at which the system experiments its highest temperature is almost 1230K for high C/O feed ratios while it goes towards lower temperatures as the C/O feed ratio is decreased. The maximum temperature line ends in correspondence of the dynamic region. The dotted line is relative to both the other two systems considered. Similar considerations apply in these cases but lines coincide.

It is evident that the addiction of hydrogen to reactants leads such loci to shift of 25K towards lower temperatures but this effect seems to be independent of the hydrogen inlet amount.
The macroscopic effect of the shifting of the whole dynamic behavior region to lower values of the inlet temperature reflects the influence of the hydrogen addition on the time-resolved temperature profiles of the system. From this point of view, the hydrogen addition causes a monotonic increase of the oscillation frequency and a decrease of the oscillation amplitude.

Therefore, hydrogen addiction to the reactants represents a further parameter to modulate the amplitude and the frequency of the oscillations experimentally found as shown in fig.6.10. The system CH$_4$/O$_2$/N$_2$ evolves through a bell-shape oscillations regime for an inlet temperature equal to 1150K and a C/O=0.4. An increase of hydrogen concentration from zero to 0.25% and 0.9% results in a increase of frequency and a decrease of amplitude. Analyses of oscillations features as function of several parameters, such as residence time and the dilution degree, have shown that the evolution of the oxidation process is very sensitive to the interaction of the kinetic and exotermicity of the system, hence the system is very sensible to any variable that influences this interaction. In this case hydrogen influences the kinetic evolution of the oxidation as well as the exothermicity of the system.
Figure 6.10  Modulation of the oscillations amplitude and frequency due to hydrogen addition.

In particular for relatively low temperature hydrogen promotes the oxidation of methane and the effects of an enhanced frequency and of a lower amplitude are typical of a situation in which the oxidation channel is accelerated.

Effect of the nature of Diluent: Steam Water

The effect of the steam water as diluent can be better understand comparing the ignition maps, presented in the chapter IV, obtained for the systems CH$_4$/O$_2$ diluted up to 90% by nitrogen or by nitrogen and steam. The steam percentage, defined as the
percentage relative to the overall dilution degree, is equal to 10% and 20%.

The comparison between the ignition maps is reported in figure 6.11.

![Figure 6.11](attachment:image.png)

**Figure 6.11**  *Comparison between the ignition maps obtained for the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2} - H\textsubscript{2}O diluted up to 90% for several steam water percentage.*

It is evident that the extension of the dynamic regions slightly changes as the percentage of steam water increases from zero to 20%. In any case the ignition maps extend for temperature range comprised between 1040K and 1250K and a C/O feed ratio comprised between values very close to zero and 0.6. The maps perfectly overlap for very lean mixtures, in fact for C/O=0.05 the border that separates the dynamic region from the steady combustion region coincides. A slightly change in the extension of the map is present for the left side of the areas.

The most relevant effect is the reduction of the dynamic region for inlet temperatures higher than 1200K and for C/O ratios higher than 0.4.

In particular passing from the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2} to the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}-H\textsubscript{2}O
(10%), the system reaches a stable combustion in the region comprised between 1200K and 1180K and C/O between 0.6 and 0.5. Furthermore oscillations are not detected anymore in the area comprised between 1180K and 1250K for C/O higher than 0.4 whether the system is diluted with steam up to 20% of the overall dilution degree.

**Figure 6.12** Bifurcation diagrams of the system \(\text{CH}_4/\text{O}_2/\text{N}_2/\text{H}_2\text{O}\) diluted up to 90% for several steam water percentage and for different C/O feed ratios

The bifurcation diagrams, reported in Chapter IV, have been used to compare the three systems. Figure 6.12 reports the reactor temperatures as function of the inlet temperature for three different C/O feed ratios and different steam water amounts.

In any case the reactor temperature indicates that for low inlet temperatures, in the
analyzed range, the water amount induces a higher reactivity of the system. In fact the temperatures relative to the system diluted with steam water up to 20%, are higher than the ones reached in the system diluted in nitrogen.

This effect is less pronounced for the system with a steam percentage equal to 10%, in fact working temperatures are higher than the ones of the system fully diluted with nitrogen just for small temperature ranges.

At the same time for both the systems diluted in part with steam water, the reactor temperature goes towards the isothermal line (dashed line) for lower inlet temperatures respect to the system \( \text{CH}_4/\text{O}_2/\text{N}_2 \). Furthermore for inlet temperatures higher than the ones that correspond to the systems maximum temperature values, the higher the amount of water is, the lower the reactor temperature is for any system.

![Figure 6.13 Ignition maps and maximum temperature line for the system \( \text{CH}_4/\text{O}_2/\text{N}_2 \). \( \text{H}_2\text{O} \) diluted up to 90% for several steam water percentage.](image)

The bifurcation diagrams show that after the maximum temperatures, the reactor
temperature goes down towards the isothermal line and the difference between the reactor and the isothermal temperature becomes relatively small and it slightly varies with a further increase of the inlet temperatures. It is possible to identify, for any C/O feed ratios and any considered system, the maximum temperature reached during the oxidation process. If these pointed are reported in the ignition maps, for any system it is possible to draw the line of the maximum temperatures.

Figure 6.14  Ignition maps and maximum temperature line for the system $CH_4/O_2/N_2-H_2O$ diluted up to 90% for several steam water percentage.

The maps and lines in questions are reported in figure 6.13. On the right side of these lines the reactivity of the system meaningfully diminishes. The figure show that, as the steam concentration increases, the maximum temperature line is shifted towards lower inlet
temperatures.

Figure 6.14 shows some temporal temperature profiles obtained for C/O=0.1 and $T_{in}=1100$K (a) and for C/O=0.4 and $T_{in}=1300$K (b) for the three system discussed in this paragraph.

Figure 6.14a shows a case of triangular oscillations while figure 6.14b triangular oscillations with high amplitude.

The presence of steam does not change the oscillation typology and slightly affects the frequency and the amplitude of oscillations.

**Comparison between Numerical and Experimental Results**

In the chapter IV several models have been employed to see if the dynamic behavior, detected experimentally, was predictable by means of numerical analyses. In particular the models of “Warnatz”, “Nancy”, “Dagaut” and “Ranzi” were employed in these simulations.
oxidation in diluted conditions.

As matter of fact, they were able to predict the oscillation phenomenology found out during experimental tests. The results were resumed in ignition maps reported and discussed in chapter IV. It is hence possible to compare the experimental and numerical results on the basis of experimental and numerical ignition maps. They have been obtained for a system CH₄/O₂ diluted with nitrogen up to 90% and for a residence time of 0.5 sec.

In the stable combustion region, the dashed-dotted curve, representing the numerically computed loci of maximum temperature increase for a fixed C/O, quite ably reproduces the same curve obtained by means of the experimental analysis (dashed line).

Fig.6.15 shows the comparison between the experimental map and the numerical maps obtained with the “Nancy model” and the “Warnatz” model. For these simulations the global heat transfer coefficient was equal to 4.4*10⁻³ cal/cm² sec K.

The range of parameters where stable combustion occurs is well predicted by the two models. Furthermore, both of them predict the existence of a zone where oscillations are present and they reproduced all the kinds of oscillations but irregular and bell-shape ones. The models are also able to predict double oscillations even though in these conditions the zone is hardly identifiable on the map because it is very narrow.

The numerical dynamic regions only partially covers the one identified by means of the experimental analysis. As a matter of fact, both the models fail the prediction in high temperature range and at high C/O ratios.

Better results have been achieved using the “Ranzi” model. A comparison of the experimental and the numerical maps is reported in Figure 6.16. The global heat transfer coefficient was set equal to 2*10⁻³ cal/cm² sec K since more thorough calculations showed that it was more adapt for the real system used for the experiments.

The numerical results demonstrate that the kinetic model is able to reproduce the
system behavior for a significant portion of the dynamic region. For C/O=0.05-0.1, the oscillations are present in the 1030K to 1275K temperature range. By increasing the C/O, the dynamic region shrinks, covering a shorter temperature range, and disappears altogether when the C/O is higher than 0.45. Up to this C/O value, the left-hand boundary of the region follows that of the experimental dynamic area quite well. In contrast, the right edge limits the oscillation region to a temperature range that is smaller than the one corresponding to the experimental area.

The numerical model is also able to predict different oscillation typologies. Single oscillations occur across most of the dynamic area, but, in contrast with the two other models, it was also possible to predict double and irregular oscillations and locate them in a region. Such area develops for temperature comprised 1075K-1160K and for C/O values between 0.075 and 0.18.

In the stable combustion region, the dashed-dotted curve, representing the numerically computed loci of maximum temperature increase for a fixed C/O, quite ably reproduces the same curve obtained by means of the experimental analysis (dashed line).

![Figure 6.16](image)

*Figure 6.16  Comparison between experimental and numerical map at 90% of dilution level.*
In order to compare the numerical results obtained with the other models among them, new numerical integrations have been realized, since the analyses realized with “Warnatz” and “Nancy” models were obtained for a different global heat transfer coefficient. The heat transfer used in these new simulations was $2 \times 10^{-3}$ cal/cm$^2$ sec K.

The comparison between the “Warnatz”, “Ranzi” and the experimental ignition maps is reported in figure 6.17.

As shown in chapter IV, an increase of the global heat transfer coefficient sensibly reduces the extension of the dynamic region in the temperature range. Hence the “Warnatz” ignition map, obtained with the new coefficient, is less wide and the agreement with the experimental data worsens.

The comparison among the maps does not lead to any new results, but it can be seen that the “Warnatz” model identify a minor number of inlet conditions for which the system evolves through a dynamic regime. Furthermore it fails to predict the dynamic behavior for very high temperatures, relatively to the range analyzed, and lean mixtures.

![Figure 6.17](image.png)

Figure 6.17  Comparison between experimental and “Warnatz” and “Ranzi” maps at 90% of dilution level.
Moreover the “temperature drop” line shown on the figure does not coincide with the experimental line. This indicates that the “Warnatz” model does not work properly for rich mixtures very at high temperatures.

Maybe it is due to the minor amount of species that are involved in the “Warnatz” model in comparison with the “Ranzi” one. In fact it counts for 34 species, until the formation of compounds with two carbon atoms, and 164 reactions while the “Ranzi” mechanism has 250 species implicated in more than 5000 reactions.

Anyway it suggests the idea that, even if the numerical results obtained by means of the “Warnatz” do not predict properly the experimental behavior of the system, the oscillations are reproducible, with their main characteristics, considering just the oxidation and the recombination channel with just C₂ species.

**Flow diagrams**

The good results obtained using the methane oxidation mechanisms have suggested the possibility of performing new numerical simulations to understand the kinetic pathways responsible of the insurgence of the dynamic behaviors. To this aim a rate of production analysis was carried using the “Warnatz” model, because it counts for a minor number of reactions and species, and hence it is a relatively mechanism to analyze. In such a way the numerical study can be easier to perform and however can lead to important basic information concerning the dynamic behavior experimentally recognized.

The rate of production analysis has been realized for an initial condition that corresponds to a cusp-shape oscillation with a frequency of 0.22 Hz and amplitude of about 200K. In particular, the T_{inlet} was fixed at 1050K and C/O at 0.2. The temperature temporal profile computed in these conditions was reported in Figure 6.18. According to the definition of cusp-shape oscillation, the first, very weak, temperature increase represents the first step ignition. After a long induction time, that lasts about 4s, it is
followed by the second ignition step that leads to the maximum oscillation temperature.

Figure 6.18  Cusp-shaped oscillation obtained for C/O=0.2 and $T_{inlet} = 1050 K$.

The rate of production analysis was performed at different time during the oscillation period, with particular regard to times closer to the second step ignition. The numeric results are summarized in species flow diagrams that allow understanding which is the main oxidation path through which the methane and oxygen react at any time.

In the flow diagrams, the blocks represent the species, which follow the path indicated by the arrows. The position of a species on the diagram depends on the type and the number of atoms that it contains. The hydrogen content in molecules decreases moving from the top toward the bottom of the diagram. The species with more than one carbon atom lay on the right side of the scheme whereas the molecules containing oxygen are reported on the left side of each column representing the evolution of species with the same carbon atoms. The arrow thickness is proportional to the reaction rate.

The flow diagram obtained for 4.5 sec was reported in Figure 6.19. The thick line entering the methane block represents the feed that is equal in both the flow diagrams here considered. Although its thickness was arbitrary chosen, the thickness of all the arrows emerging from the methane block are scaled in such a way that difference between the entering and emerging arrows thickness represents the methane conversion. This
consideration applies for each block reported in the flow diagram. Moreover, in flow diagram equilibrium reaction involving CH$_3$O$_2$ and CH$_4$ is indicated with a different grey level since it is one order of magnitude thicker than the other arrows.

The flow diagram reported in Figure 6.19 shows that the few radicals available at this time in the reactor dehydrogenate methane thus producing CH$_3$ that, in turn, mainly reacts with O$_2$.

![Species flow diagram obtained for 4.5s](image)

Therefore, the main oxidation path is CH$_3$→CH$_2$O→CHO→CO. All the radicals OH, H and O produced along this reaction path, come back to the initial step of the chain and dehydrogenate the methane. Since the oxidation of CO to CO$_2$ is very slow and the methane conversion is very low, the temperature increases of few degrees. At this time
only the oxidation reaction is active. At higher time, up to 8.7s, HO₂ radicals, which can also lead to the formation of H₂O₂, mainly oxidize CH₃. The decomposition of hydroperoxy radical, that represents the reaction branching, is very slow in these conditions, such as occurs for the branching reactions of high temperature regimes. As a consequence, the system reactivity is very low. Up to this time the recombination mechanism covers a marginal role.

At the 8.7 sec the system is closer to the second step ignition and its temperature reaches 1070K. The main reaction path is still the oxidation of the radical CH₃ to CH₃O and its dehydrogenation up to CO. The conversion of CO to CO₂ increases and the recombination reaction begins to cover a more important role. The main path of the recombination channel, involving C₂ species, is C₂H₅→C₂H₄→C₂H₂→CH₂CHO→CH₃CHO→CH₃CO. The CH₃CO radical, in turn, decomposes thus producing CH₃ and CO.
The second step ignition is due to the slow but continuous temperature increase and to the increase of the amount of small radicals involved in the branching reaction related to the H₂/O₂ system.

The flow diagram reported in Fig.6.20 photographs the system during the temperature jump, at t = 8.87s. Arrow colors have been changed from black to grey in order to indicate that, in this condition, the reaction rates are very high in comparison with the one represented in the flow diagram of Figure 6.19. Because of the availability of OH and O radicals, the CH₃ mainly react with them producing methanol and formaldehyde, respectively. The recombination channel covers a more important role and the oxidation of CO to CO₂ is very fast. In these conditions the methane conversion attains the unity. At
8.88s the temperature reaches the maximum value of 1240K and then decreases down to inlet temperature.

In order to understand which reactions play an important role in the establishment of oscillatory behavior a further analysis has been done by means of reaction flow analysis. It was performed by properly changing the “Warnatz” methane oxidation mechanism, deleting some reactions or changing their kinetic constants.

The rate of production analysis showed that the recombination reactions gain relevance during the phases of the second step ignition. Therefore, the attention was focused on the weight of this reaction channel on the oscillation phenomenology. Starting from the initial conditions considered in the previous simulations, the first analysis was performed by deleting from the kinetic mechanism the whole recombination channel. The results were summarized in Figure 6.21 where the temperature profiles obtained with the original and modified model were reported. In figure 6.21b it can be easily seen that the closure of the recombination reaction path leads to an increase of oscillation frequency that passes from 0.2Hz up to 1.6Hz.

The opposite effect was obtained by increasing the velocity of CH₃ recombination.
In particular, the activation energy of this reaction was decreased from 81240 J/mole to 70000 J/mole. In this case the oscillation phenomenology disappears leading to a stable temperature profile as shown in figure 6.21c. These results suggest that a faster recombination channel removes CH$_3$ radicals from the oxidation channel. Therefore, these
radicals pass through reactions that are slower in comparison with the reactions of the other “competitive” channel and at the same time they are not able to provide the same amount of radicals. The system pays this lack with a lower reactivity. Furthermore, the CH$_3$CO decomposition, which produces CH$_3$ and CO making them available for oxidation, is very slow. This results in a CH$_3$ radicals trapping in the recombination channel.

The same effect can be obtained by suppressing the CH$_3$CO decomposition from the initial model, such as shown by the temperature profile reported in Figure 6.21d. Again, the recombination channel removes CH$_3$ radicals that are not made available again due to the absence of CH$_3$CO decomposition.

This mechanism seems to give also a plausible explanation for the observed increase of frequency by increasing the inlet temperature, at a fixed C/O ratio. As a matter of fact, the less the inlet temperature is, the later the second step ignition will be favored. This means that the amount of CH$_3$ stored by the recombination channel will be greater. Therefore, when the conditions favor the second step ignition, the reactivity of the system will be higher. It means the oscillation regime will have low frequency values but high temperature gradients. On the other hand the higher the temperature is, the faster the oxidation channel will win the competition with the recombination channel. This means the system will have a shorter time to store the radical CH$_3$ so when the ignition occurs the system will evolve through oscillatory regimes with a higher frequency but a lower temperature gradient.

By this way the recombination channel is able to module the frequency of the oscillation regimes and so the temperature gradient.

In order to verify the consideration reported above in a wider range of parameters, the same analysis was carried out both in higher temperatures and richer feed ratios. The results confirmed the crucial role of the recombination pathway in dynamic evolution of
the system. As matter of fact it coherently responds to the same model modifications.

In figure 6.22 it is reported a scheme of the main pathways active in the oxidation scheme of methane. Several radicals, such as OH, H and O; firstly dehydrogenate methane to CH₃. Methyl radical can pass through the oxidation pathways until the formation of CO or CO₂ or can recombine and form ethane. This compound can be further on dehydrogenated, by means of radicals or thermal decompositions, to form several species until the vinyl radical (C₂H₃). It can oxidize with the formation of oxygenated species or can dehydrogenise, yielding C₂H₂.

![Reaction scheme of methane.](image)

**Figure 6.22  Reaction scheme of methane.**

The rates of reactions responsible for C₂H₃ consumption have been evaluated as function of T_{inlet}. The results at C/O=0.5 were reported in Figure 6.23a where the dashed curve represents the rate of C₂H₃ oxidation whereas the solid line indicates the rate of C₂H₃ dehydrogenation to C₂H₂. The rate of C₂H₃ oxidation increases up to T_{inlet}=1175K. As shown by dashed-dotted line in Figure 6.23b, this temperature corresponds to the highest ΔT computed at C/O=0.5. In the same temperature region, the rate of C₂H₃
dehydrogenation increases continuously with $T_{\text{inlet}}$ although it always remains lower than $\text{C}_2\text{H}_3$ oxidation rate. From $T_{\text{inlet}}=1175\text{K}$ onwards, the rate of $\text{C}_2\text{H}_3$ oxidation decreases and is overwhelmed at about $T_{\text{inlet}}=1275\text{K}$ by $\text{C}_2\text{H}_3$ dehydrogenation which continues to rise.

![Figure 6.23](image)

**Figure 6.23**  $\text{C}_2\text{H}_3$ reaction rate for oxidation and dehydrogenation channel at $\text{C/O}=0.5$ and $\text{C/O}=0.1$

The same analysis was performed for $\text{C/O}=0.1$, i.e. under lean conditions. From $T_{\text{inlet}}=1000\text{K}$ up to $T_{\text{inlet}}=1050\text{K}$, $\text{C}_2\text{H}_3$ oxidation is the only active channel of $\text{C}_2\text{H}_3$ consumption. It reaches an initial maximum at $T_{\text{inlet}}=1025\text{K}$ then decreases up to $T_{\text{inlet}}=1050\text{K}$. Higher $T_{\text{inlet}}$ corresponds to a temperature oscillation region, where the reaction rates represent the mean value computed for a single oscillation period. With the onset of oscillation, both oxidation and dehydrogenation reactions increase. The former reaches a maximum at $1150\text{K}$, then decreases but still remain higher than the $\text{C}_2\text{H}_3$ dehydrogenation rate. At $T_{\text{inlet}}=1050\text{K}$, the $\text{C}_2\text{H}_3$ dehydrogenation rate suddenly reaches a nearly constant value and remains that way until $1300\text{K}$ before falling steeply to very low values.
Hydrogen Addiction: Rate of Species Production Analysis

To identify the hydrogen addition effect on the kinetic paths of methane oxidation, a rate-of-production analysis was carried out for $T_{in}$ equal to 1015 K and for a C/O ratio value equal to 0.2. Fig. 6.24 shows the effect of the hydrogen addition on the temperature temporal profiles predicted by the “Warnatz” model.

*Figure 6.24  Hydrogen addition effect on the ignition kinetic mechanism of the system for $T_{in}=1015 \text{ K}$ and C/O=0.2.*

To identify the hydrogen addition effect on the kinetic paths of methane oxidation, a rate-of-production analysis was carried out for $T_{in}$ equal to 1015 K and for a C/O ratio value equal to 0.2. Fig. 6.24 shows the effect of the hydrogen addition on the temperature temporal profiles predicted by the “Warnatz” model.

An addiction of hydrogen to the system CH$_4$/O$_2$/N$_2$ leads the system to pass from a slow combustion to an oscillating regime. The analysis was performed at 0.2 sec after the beginning of the simulation.

Analyses realized in absence of hydrogen show that for the chosen inlet conditions the main branching reaction might be the decomposition of the H$_2$O$_2$. H atoms react via the breaking reaction H+O$_2$+M$_2$HO$_2$+M producing the relatively stable HO$_2$ radicals. They
form $\text{H}_2\text{O}_2$ that decomposes into two OH radicals.

The presence of hydrogen promotes the high temperature classical branching reactions and increases the whole reactivity of the system. In fact $\text{H}_2$ reacts mainly with OH through the exothermic reaction $\text{H}+\text{O}_2\rightarrow\text{OH}+\text{O}$. From the rate-of-production analysis it has come out that reactions that involve the radical OH show the most significant increment. For $\text{H}_2$ concentration equal to 0.9% also the breaching reaction $\text{H}_2+\text{O}\rightarrow\text{OH}+\text{H}$ becomes significant in the production of OH radicals. They mainly dehydrogenate the methane to $\text{CH}_3$. In such a way the oxidation pathways of methane can be initialized and accelerated by the great amount of radicals present in the system. These kinetic paths are resumed in the flow diagram reported in figure 6.25. The thickness of the arrows is proportional to the rate of the several reactions reported in the scheme. This diagram is relative to a hydrogen inlet concentration equal to 0.9%.

\[ \begin{array}{c}
\text{HO}_2 \\
\text{H}_2 \\
\text{O}_2 + M \\
\text{H} \\
\text{O} \\
\text{OH} \\
\text{CH}_4 \\
\end{array} \]

Figure 6.25  Main kinetic paths involved in the ignition mechanism of the $\text{CH}_4\text{H}_2/\text{O}_2/\text{N}_2$ system in presence of hydrogen for $T_m=1015$ K and $\text{C/O}=0.2$ at the time $t=0.2$ s.

The effect of hydrogen addiction is very similar to the effect that has been obtained
by removing the recombination channel from the “Warnatz” model as reported in chapter V.

The numerical analysis consisted in properly changing the “Warnatz” methane oxidation mechanism, deleting some reactions or changing their kinetic constants. It was performed for a system composed by methane and oxygen diluted up to 90% by nitrogen. The temperature was 1050K and the C/O feed ratio was 0.2.

The results have been summarized in Figure 6.26 where the temperature profiles obtained with the original and modified model were reported. Using the original “Warnatz” model for the inlet conditions analyzed the system evolves through a cusp-shaped oscillating regime.

In figure 6.26b it can be easily seen that the closure of the recombination reaction path leads to an increase of oscillation frequency that passes from 0.2Hz up to 1.6Hz.

This is mainly due to the fact that CH₃ radical cannot pass through the recombination channel, hence they just can go through the recombination channel thus they feed such pathway in a more consistent way and also the radicals, produced in the oxidation channel from CH₃ to CO, are consumed just in this pathway. It results in a higher reactivity of the system.

The opposite effect was obtained by increasing the velocity of CH₃ recombination. In particular, the activation energy of this reaction was decreased from 81240 J/mole to 70000 J/mole. In this case the oscillation phenomenology disappears leading to a stable temperature profile as shown in figure 6.26c. These results suggest that a faster recombination channel removes CH₃ radicals from the oxidation channel. Therefore, these radicals pass through reactions that are slower in comparison with the reactions of the other “competitive” channel. At the same time, they are not able to provide the same amount of radicals and the dehydrogenation reactions, typical of the recombination channel, consume
the radicals present in the system. The system pays this lack with a lower reactivity. Furthermore, the CH$_3$CO decomposition, which produces CH$_3$ and CO making them available for oxidation, is very slow. This results in a CH$_3$ radicals trapping in the recombination channel.

The same effect can be obtained by suppressing the CH$_3$CO decomposition from the initial model, such as shown by the temperature profile reported in Figure 6.26d. Again, the recombination channel removes CH$_3$ radicals that are not made available again due to the absence of CH$_3$CO decomposition.

Therefore, if the attention is focused on the figure 6.26a and 6.26b, it appears that the hydrogen addiction promotes the oxidation channel and leads the system to oscillate.
Furthermore, an analysis realized on the reaction rates of the reactions that promote the chain mechanism, and hence sustain the combustion process, appeared clear that during the temperature jump the branching reactions are the reactions of the system $\text{H}_2/\text{O}_2$ typical of high temperatures. The results are shown in figure 6.27. This analysis has been realized for the same inlet conditions considered in the sensitivity analysis.

In particular for low temperatures the main branching reaction is the decomposition
of the hydrogen peroxide (reaction 1). It causes the first temperature step.

\[ \text{H}_2\text{O}_2 + \text{M} \rightarrow \text{OH} + \text{OH} + \text{M} \]

1)

Then there is an induction time before the temperature jump occurs. In this period the most important reactions is reaction (reaction 2).

\[ \text{H} + \text{O}_2 + \text{M} \rightarrow 2\text{HO}_2 + \text{O} + \text{M} \]

2)

\[ \text{HO}_2 \text{ radicals react and form the hydrogen peroxide that decomposes and provides for OH radicals.} \]

When there is an enough high amount of radicals the system reach the condition to realize the second temperature jump. The temperatures become sufficiently high to promote the chain radical mechanism of the system H/2/O2 typical of high temperatures (reaction 3 and 4)

\[ \text{H} + \text{O}_2 \rightarrow \text{OH} + \text{O} \]

3)

\[ \text{H}_2 + \text{O} \rightarrow \text{OH} + \text{H} \]

4)

Since a hydrogen addiction promotes the formation of radicals H, O and OH, enhancing the reaction rates of the reactions 3) and 4), as shown in figure 6.25, it is clear
that the oxidation channel becomes more important.

In figure 6.28 it is reported the diagram relative to the methane yield in CO, CO₂, C₂H₂ obtained by means of the “Dagaut” mechanism for a C/O feed ratio equal to 0.6 and an inlet temperature equal to T₀ = 1175 K.

For these inlet conditions, the model predict that higher reactor temperatures with increasing the hydrogen percentage.

As matter of fact, the system with an inlet hydrogen concentration equal to 2.5% leads the methane conversion to be almost twice the methane conversion of the system CH₄/O₂/N₂. The conversion does not increase with a linear law as function of the hydrogen concentration, in fact for the cases H₂ = 0.5%, 0.75% and 0.9% the conversion is respectively 36%, 42% and 39%.

This trend is mainly due to the fact that hydrogen can react with the methyl radical to produce methane. Hence the conversion of methane is lowered by the hydrogen addiction but methyl radicals that pass through the oxidation channel, can be easily oxidized to CO and CO₂ since the amount of radical is enhanced by the presence of hydrogen.

This is also understandable considering the increase of methane yield in CO, CO₂ and C₂H₂. Also in this case they increase with a non-proportional law as function of the hydrogen concentration.

In particular the CO₂ yield increase from 9% to 17%. This justifies the higher reactor temperatures numerically obtained for the systems with hydrogen. As matter of fact, the reaction of carbon monoxide to carbon dioxide is the most exothermic reaction of the methane kinetic mechanism, thus it implicates higher working temperatures.

An important aspect of the hydrogen addiction to the system CH₄/O₂/N₂ is the higher yield of methane in C₂H₂. It has been underlined that the higher the working temperature is, the higher the acetylene stability is. In particular for temperature higher than about
1200K the acetylene starts becoming a stable species.

Furthermore the hydrogen presence, as explained in chapter II, increases the formation of acetylene and slows down the formation of species such as ethane, benzene and carbon coke. Hence the stability of C$_2$H$_2$ is improved by hydrogen addiction. Furthermore the relative low partial pressure of methane and the relatively high temperatures favor the formation of acetylene instead of benzene and ethene.

Hydrogen interacts both in the oxidation and recombination channels leading to a higher reactivity for low inlet temperatures, but it damps the reactivity of the system for high working temperatures and rich mixtures favoring, in the mean time, the formation of acetylene.

![Diagram](image.png)

**Figure 6.28** Methane yield diagram in CO, CO$_2$, C$_2$H$_2$ obtained for the “Dagaut” mechanism for C/O=0.6 and $T_{in}$ = 1175K
Discussion

This could explain the “temperature drop” behavior that has been explained in the experimental bifurcation diagram. In fact, the possibility to produce acetylene represents the capacity of the system to store carbon and hydrogen atoms and subtract them to the oxidation channel. Hence, if hydrogen enhances the availability of radical species and induce the system to work with higher temperatures, and higher yields, from the other side, it favors the thermodynamic stability of the acetylene, thus, for certain working conditions, depending on the inlet temperatures and mixture composition, it slows down the oxidation reactions.

Steam Water: Chemical Effect

In the Chapter IV it has been reported a numerical study realized to characterize the system CH₄/O₂ diluted with steam water and nitrogen up to 90% for several steam concentrations, in terms of species produced during the methane oxidation process. Hence the fuel conversion and its yields into carbon oxide, carbon dioxide and C₂ products have been calculated. The study has revealed that, increasing the steam concentration; the methane conversion towards CO₂ increases, while the CO production decreases. In order to better understand the effect of water addition to the system CH₄/O₂ further numerical simulations have been realized.

The analysis has the aim to discriminate the thermal and chemical contribution of steam water to the evolution of the methane oxidation process in Mild conditions. In literature is in fact known that water can act in two different ways: a thermal and a chemical effect. The former is mainly due to its higher capacity in comparison with nitrogen, hence it can lower the working temperature causing a reduction of reaction rates
involved in the oxidation process. The latter effect is due to its higher efficiency as third-body in third molecular reactions, in comparison with nitrogen. Hence water can induce an enhancement of the rate of third molecular reactions, such as terminating ones. Furthermore water is not an inert species, thus it can breakdown causing an increase of radical species.

In order to clarify and separate the contribution of the two effects just illustrated, during the numerical simulations it has been defined a species X that has the same heat capacity and the same efficiency of water but it is an inert species. As matter of fact this species is not involved in the elementary reactions of the methane oxidation kinetic mechanism. To this aim the “Warnatz” model has been modified.

Results are shown in the following figures. In particular in figure 6.29 the methane conversion for the systems CH$_4$/O$_2$ diluted with N$_2$ and steam are reported. In particular steam has been added in such a way that nitrogen and steam dilute the system up to 90%. Steam percentage has been set equal to 0, 10% and 20% of the overall dilution degree. Then methane conversion is compared with the ones of the systems in which steam water has been substituted with the inert species X.

The analyses has been realized in a temperature range that goes from 1000K to 1700K for a rich mixture, in which the C/O feed ratio is equal to 0.4.
Figure 6.29  Methane conversion as function of the inlet temperature for systems diluted with nitrogen and water or species X for several steam or X percentages.

For very low temperatures, comprised between 1025K and 1050K, the system diluted in nitrogen has the lowest conversion degree. As the temperature is increased up to 1100K the same system shows higher conversion degrees.

For temperature up to 1500K, the systems CH₄/O₂/N₂-X (10%) and CH₄/O₂/N₂-H₂O (10%) seem to have the same methane conversion degree, in reality the conversion degree is slightly different but the in the figure it is not clearly visible the discrepancy between the two methane conversion degrees. In particular the former system has a slightly higher CH₄ conversion degree. The same considerations apply to the systems CH₄/O₂/N₂-X and CH₄/O₂/N₂-H₂O. In particular if the systems diluted with water or X up to 20% of the global dilution degree it is possible to see that the curves almost overlap but in point of fact the systems diluted partially with water has a lower conversion. The difference between the conversion degrees is almost negligible in both the cases. For temperature higher than 1550K the highest conversion degree competes to the system with a water percentage equal to 20%. The system CH₄/O₂/N₂-H₂O (10%) has hence the second highest dilution
degree while for the other systems curves overlap.

The effect of water on the methane conversion is not very evident since the methane conversion and temperatures reached by the systems are very close to each other. More meaningful information can be obtained considering the methane yield into CO\(_2\) and CO.

Figure 6.30  
\[\text{CO}_2\] yield as function of the inlet temperature for systems diluted with nitrogen and water or species X for several steam or X percentages.

Figure 6.30 shows the conversion of methane into carbon dioxide as function of the inlet temperature for the several systems considered in the numerical analysis.

It is here evident that the highest value of the discussed parameter competes to the system CH\(_4\)/O\(_2\)/N\(_2\)-H\(_2\)O (20%). In fact it has the highest value for temperatures higher than 1100K, and it reaches a value equal to about 0.58 for an inlet temperature equal to 1700K.

The system CH\(_4\)/O\(_2\)/N\(_2\)-H\(_2\)O (10%) has the second highest CO\(_2\) yield. The curves relative to the other considered systems overlap.

It is worth noting that the curve relative to the system CH\(_4\)/O\(_2\)/N\(_2\)-H\(_2\)O (10%) reaches a plateau, while in the other cases the CO\(_2\) yield curves pass through a maximum value and then slowly decrease.
Figure 6.31 shows the conversion of methane in CO as function of inlet temperature for systems diluted with nitrogen and water or X, for several steam or X percentages.

In this case the system diluted in nitrogen presents the highest values of the parameter CO yield. The conversion significantly lowers for the systems diluted in nitrogen and water. The systems CH₄/O₂/N₂-X (10%) and CH₄/O₂/N₂-X (20%) show a methane yield into CO slightly different from the system diluted just with nitrogen. In theses cases curves overlap for very high inlet temperatures. Furthermore the higher the concentration of X is, the lower the CO yield is.

In this case it is possible to identify the chemical contribute of water addiction. The species X and steam water, takes part to the kinetic reaction mechanism of methane in different ways, in particular they participate in the same way in third molecular reactions as third-body but the species X can not dissociate or react in other way, while water can give rise to breakdown reactions. Hence the gap between the curves relative to the species X and the steam water, for a fixed concentration, clearly indicates the chemical effect of water. The main effect on the kinetic evolution of the methane oxidation is that steam acts in such a way to increase the conversion of methane to CO₂ while decreasing the conversion to CO.
Figure 6.31  CO yield as function of the inlet temperature for systems diluted with nitrogen and water or species X for several steam or X percentages.

Figure 6.32 shows the methane conversion in acetylene as function of the inlet temperature for the systems CH$_4$/O$_2$/N$_2$, CH$_4$/O$_2$/N$_2$-H$_2$O (10%-20%) and CH$_4$/O$_2$/N$_2$-X (10%-20%). The figure shows that in any system acetylene increases as the inlet temperature is increased, reaches a maximum and quickly diminishes. The system diluted in nitrogen and water, with a steam relative percentage equal to 20%, present the highest values of methane conversion in C$_2$H$_2$ until a value of the temperature equal to 1500K, then it reaches a maximum and decreases. The curve relative to the system CH$_4$/O$_2$/N$_2$-H$_2$O (10%) shows that same trend, but it has a maximum for an inlet temperature equal to 1600K.

In correspondence of these maximum values, the C$_2$H$_2$ yield of the other systems overcomes the ones relative to the systems diluted in nitrogen and water. In the other cases curves almost coincide. For temperatures lower than 1400K the system diluted in nitrogen shows a slightly higher production of acetylene in comparison with the systems diluted in nitrogen and X. In this case the higher is the X species concentration, the lower is the methane conversion in acetylene.
Figure 6.32  $C_2H_2$ yield as function of the inlet temperature for systems diluted with nitrogen and water or species X for several steam or X percentages.

For temperatures lower than 1400K the acetylene production curves invert their relative position and the system diluted in nitrogen shows the lowest acetylene yield while the highest one competes to the system $CH_4/O_2/N_2$-X (20%). The discrepancy among values for the systems $CH_4/O_2/N_2$-X (10%-20%) and $CH_4/O_2/N_2$ is very small.

Other simulations have been run to understand the effect of steam on methane oxidation in Mild condition. In particular higher steam percentages; up to 50% and 100%, have been used. These high steam concentrations have been used in order to make more evident the effect of vapor water on the system analyzed. Figure 6.33 shows the reactor temperature as function of the inlet temperatures for the system diluted in nitrogen and water with a steam concentration equal to 0%, 10%, 20%, 50% and 100%. The reactor temperature is not significantly affected by the presence of water in the several percentage reported above. In fact all the curves almost overlie. The difference among the temperatures is just of few degrees.

Figure 6.34 shows the methane conversion as function of the inlet temperature for
the systems taken in consideration.

Figure 6.33  Reactor Temperature as function of the inlet temperature for systems diluted with nitrogen and water for several steam percentages.

Figure 6.34  Methane conversion as function of the inlet temperature for systems diluted with nitrogen and water for several steam percentages.

In this case in the temperature range comprised between 1050K and 1460K the system diluted in nitrogen presents the highest conversion. It is identifiable a clear trend of
the methane conversion, in fact as the steam concentration increases the methane conversion decreases. For an inlet temperature equal to 1460K, curves intersect and for higher temperatures they invert their relative position. In this case an opposite trend, respect to the one just discussed above, is recognizable, in fact the higher the steam concentration is, the higher methane conversions are.

Figure 6.35 shows the methane conversion in carbon dioxide as function of the inlet temperature for the systems diluted in nitrogen and water.

![Figure 6.35](image.png)

*Figure 6.35*  
CO$_2$ yield as function of the inlet temperature for systems diluted with nitrogen and water for several steam percentages.

Except for very low temperatures, relative to the range analyzed in these numerical simulations, the highest CO$_2$ yield competes to the system fully diluted with steam water. Decreasing the steam concentration in the systems CH$_4$/O$_2$/N$_2$-H$_2$O the methane conversion in carbon dioxide lowers.

In particular the conversion degree is 0.8 for a steam percentage equal to 100%, then it becomes 0.7, 0.55, 0.45 and 0.3. Furthermore the CO$_2$ yield curves increases monotonically for the two systems that have the highest steam amount. In the other cases
the CO$_2$ yield reaches a maximum and than slowly decreases. The maximum value is gained by the systems for lower inlet temperatures as the steam concentration decreases.

An opposite trend is identifiable for the methane conversion in carbon monoxide. Figure 6.36 shows such a yield as function of the inlet temperature for the systems diluted up to 90% with nitrogen and water for several diluent compositions. In this cases the higher the steam concentration is, the lower the CO yield is.

The several curves show a similar trend: the CO yields firstly quickly increase, pass through a maximum value, than decrease reaching a relative minimum value, finally increase again.

![Figure 6.36 CO$_2$ yield as function of the inlet temperature for systems diluted with nitrogen and water for several steam percentages.](image)

Both the maximum and the minimum values occur for lower inlet temperatures as the steam amount is enhanced.

Figure 6.37 reports the acetylene yield as function of the inlet temperature for systems diluted with nitrogen and water for several steam percentages. Curves show that
the methane conversion in acetylene increases as function of the inlet temperatures, reach a maximum and decrease.

![Figure 6.37](image)

*Figure 6.37  C\textsubscript{2}H\textsubscript{2} yield as function of the inlet temperature for systems diluted with nitrogen and water for several steam percentages.*

The maximum occur for lower inlet temperatures and has a lower value as the steam concentration is increased. In fact for the system completely diluted in steam it occurs for an inlet temperature equal to 1440K, while for the system diluted in nitrogen it seems to occur for 1700K.

The results obtained using the “Warnatz” model have been compared to the ones found out using another methane kinetic oxidation mechanism, the “Dagaut” model, that has been used in other sections to study the effect of hydrogen on the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}.

Figure 6.38 shows the reactor temperature as function of the inlet one for the systems CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}, CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}-H\textsubscript{2}O (10%), CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}-H\textsubscript{2}O (20%) for the two used models. In the legend of the figure the “W” indicates data from the “Warnatz” model while “D” from the “Dagaut” one.

It can be seen that the reactor temperatures relative to the same kinetic model overlie,
while data from the two models show that the second oxidation mechanism predicts lower temperatures for low inlet temperatures. In particular the “Dagaut” model for temperatures up to 1125K indicates that the system is not able to ignite. Once the methane oxidation reactions start, the reactor temperatures for the two models match. In fact for inlet temperatures higher than 1175K lines overlap.

![Graph](image)

**Figure 6.38** Reactor Temperature as function of the inlet temperature for systems diluted with nitrogen and water predicted by the “Warnatz” and the “Dagaut” models.

Figure 6.39 shows the conversion of methane as function of the inlet temperatures predicted by the two models. The “Warnatz” model forecasts higher conversion degrees for inlet temperature lower than 1200K since the mixtures ignite for lower inlet temperature respect to the other model. But for inlet temperatures higher than 1300K the “Dagaut” model predicts higher values of methane conversion. Anyway it is confirmed the trend discussed earlier in the same paragraph. The system diluted in nitrogen has a higher conversion for low temperatures, but as the inlet temperature increases the curves intersect and they change their relative position indicating that, in the system diluted in nitrogen and
water with a percentage equal to 20%, fuel is more efficiently consumed.

The “Dagaut” results confirm also the trend of the methane conversion into CO$_2$ and CO observed in a first analysis realized by means of the “Warnatz” model. Figures 6.40 and 6.41 show the CO$_2$ and CO yields predicted by the two models as function of the inlet temperatures.

![Diagram](image)

*Figure 6.39* Methane conversion as function of the inlet temperature for systems diluted with nitrogen and water predicted by the “Warnatz” and the “Dagaut” models.

The highest carbon dioxide yields compete to the system diluted in water up to 20%. In particular for such a system, the “Warnatz” model forecasts higher inlet methane conversion for temperature up to about 1140K respect to the results obtained by the other model. For the system CH$_4$/O$_2$/N$_2$-H$_2$O (10%) the “Warnatz” model, once again, indicates higher conversion degree, but for temperatures higher than 1420K the CO$_2$ yield curves overlie. On the contrary, for the system diluted just in nitrogen the “Warnatz” model predicts CO$_2$ yields higher than the ones numerically found out by means of the other kinetic model, in all the analyzed temperature range.
The CO yields curves obtained by the “Dagaut” model validate the trend already identified earlier in the analyses realized by means of the “Warnatz” model and earlier discussed. The curves present a maximum, than a relative minimum and than slowly increase again. Furthermore the higher the steam concentration is, the lower the CO production is.

However, comparing the several systems once the diluent composition has been fixed, the “Dagaut” model predicts higher methane conversion to this species for high temperatures, while for low temperatures they become lower in comparison to the one obtained by the other models. In particular curves relative to the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}, come across for an inlet temperature equal to 1300K. After this value the CO yields obtained by the “Dagaut” model overcome the ones got by the “Warnatz” model.

![Graph showing Reactor Temperature as a function of the inlet temperature for systems diluted with nitrogen and water predicted by the “Warnatz” and the “Dagaut” models.](image)

Figure 6.40 Reactor Temperature as function of the inlet temperature for systems diluted with nitrogen and water predicted by the “Warnatz” and the “Dagaut” models.
Similar considerations apply for the other systems, even if the intersection between curves happens for lower inlet temperatures as the steam percentage increases.

Figure 6.42 shows the acetylene production predicted by means of the two models as function of the inlet temperature for the several considered systems.

In this case comparing the data from the two kinetic models some differences are identifiable. In fact in general both the models predicts that the systems with steam have a slightly higher values of the C$_2$H$_2$ yields. Acetylene yield increases, reaches a maximum and decreases.

The “Warnatz” model indicates that the maximum values significantly change with the diluent composition, in particular a higher steam concentration implies a lower maximum, additionally it leads the systems to reach its maximum in acetylene production for lower inlet temperatures. This last feature is confirmed by data obtained with the “Dagaut” model but the maximum values are comparable among them.
Indeed the new numerical simulations clearly confirm the trend in methane consumption and species production obtained with the “Warnatz” model, even if some differences occur.

The steam water dilution causes hence a reduction in methane conversion for low temperature the low temperatures (T<1450K according to the “Dagaut” model, T<1500K according to the “Warnatz” model), while for high temperatures the trend is inverted, a higher conversion of methane to CO$_2$ at detriment of a lower conversion in CO, finally a shift of the maximum acetylene production towards lower inlet temperatures.

*Rate of production analysis*

In order to comprehend what reactions are more affected by the presence of great amounts of steam water a rate of production analysis has been realized using the “Warnatz” model for the systems CH$_4$/O$_2$/N$_2$-H$_2$O with several steam dilution percentages (from 0% to 100%). The analysis has been carried out for a C/O feed ratio equal to 0.4 and
an inlet temperature equal to 1200K. This value has been chosen since the discrepancy between the methane conversion and CO and CO$_2$ yields for the various systems is here consistent.

The rate of production analysis has been realized identifying the most influential reactions of the methane oxidation mechanism and the attention has been focused on some key species such as methane, methyl radical, CO and radicals H, O, OH and HO$_2$. Results have been reassumed in histograms.

Figure 6.43 shows the most important elementary reactions that methane involve methane net consumption. It is consumed by the following reactions:

\[
\text{CH}_4 + H = \text{H}_2 + \text{CH}_3 \\
\text{CH}_4 + O = \text{OH} + \text{CH}_3
\]
\[ \text{CH}_4 + \text{OH} = \text{CH}_3 + \text{H}_2 \]

and mainly produced by the following reactions:

\[ \text{CH}_3 + \text{H} = \text{CH}_4 \]

\[ \text{CH}_3 + \text{HO}_2 = \text{CH}_4 + \text{OH} \]

In the system diluted just in nitrogen methane is mainly dehydrogenated to methyl radicals by reaction 1), than reaction 3) followed by reaction 2). While the most important reaction in the methane production is reactions 4).

It can be observed that increasing water concentration the reaction 1) and 2) become increasingly slower, while the rate of reaction 3) is significantly enhanced. At the same time reaction 4) becomes slower, while reaction 5) faster. For the system completely diluted in steam water, the fastest dehydrogenation reaction is reaction 3) followed by reaction 1) and 2). Hence it seems that all the reactions that involve radicals H and O become slower, while reactions that involve OH and HO\textsubscript{2} radicals become faster as steam concentration is augmented.

Figure 6.44 shows the most important reactions for the methyl radical as function of the diluent composition. Methyl radicals are mainly produced by the reactions 1), 2) and 3) reported above. It is consumed mainly by these reactions:

4) \[ \text{CH}_3 + \text{H} = \text{CH}_4 \]

\[ \text{CH}_3 + \text{CH}_3 = \text{C}_2\text{H}_6 \]

\[ \text{CH}_3 + \text{HO}_2 = \text{CH}_3\text{O} + \text{OH}. \]

The same considerations realized for the methane reactions relative to reactions 1), 2), 3), 4) and 5) can be repeated for the methyl radicals. Furthermore the rate of reaction 6), that leads to the formation of ethane, is lowered by the presence of steam.

It means that the methyl radicals, as steam concentration is enhanced, prefer going towards the oxidation channel more than towards the recombination channel.
Figure 6.44  Reaction rates of methyl radicals as function of the composition of the diluent in the system \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \).

Figure 6.45  Reaction rates of CO as function of the composition of the diluent in the system \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \).
Figure 6.45 reports the reaction rates of CO as function of the composition of the diluent in the system CH4/O2/N2-H2O. Reactions that produce CO are the following:

\[
\text{CHO} + \text{M} = \text{CO} + \text{H} + \text{M}
\]

\[
\text{CH}_3\text{CO} = \text{CH}_3 + \text{CO}
\]

While reaction that consume this species are:

\[
\text{CO} + \text{OH} = \text{CO}_2 + \text{H}
\]

\[
\text{CO} + \text{HO}_2 = \text{CO}_2 + \text{OH}
\]

It is clear that steam dilution enhances the velocity of the reaction 8), 10) and 11) while reduce the rate of reaction 9). Reaction 8) becomes faster since water has a very high third body efficiency in third-molecular reactions in comparison with nitrogen.

![Graph showing reaction rates of H2O as function of the composition of the diluent in the system CH4/O2/N2-H2O.]

Figure 6.46  Reaction rates of H2O as function of the composition of the diluent in the system CH4/O2/N2-H2O.

In fact in the “Warnatz” kinetic model the nitrogen efficiency for this reaction is 4, while for steam water it is 6.5. Reaction 10) and 11) becomes faster in presence of steam
water in a manner proportional to water concentration, showing again that reaction that involve OH and HO\textsubscript{2} radical becomes faster.

The next step in this analysis has been the identification of reactions that involve the steam water itself. Figure 6.46 shows the reaction rates of H\textsubscript{2}O as function of the composition of the diluent in the system CH\textsubscript{4}/O\textsubscript{2}/N\textsubscript{2}-H\textsubscript{2}O.

In the system entirely diluted in nitrogen the main reaction that produce water is the reaction 3) together with the following reactions:

\begin{align*}
H_2 + OH &= H_2O + H \\
C_2H_4 + OH &= C_2H_3 + H_2O \\
C_2H_6 + OH &= C_2H_5 + H_2O \\
CH_2O + OH &= CHO + H_2O
\end{align*}

And it consumed by reaction

\begin{align*}
OH + OH &= H_2O + O \\
CH_2(S) + H_2O &= CH_3 + OH
\end{align*}

Steam water meaningfully affects the rate of reaction 12) as well as 16). Hence it affects the equilibrium of reaction 12), and produce OH radicals by reaction 16). Moreover reactions 15) and 3), as well as 13) and 14), become faster and faster. All these reactions involve OH radicals.

Figure 6.47 reports the main elementary reaction rate of the production and consumption of molecular hydrogen.

It is produced by reaction 1) and the other reactions ranked below:

\begin{align*}
CH_2O + H &= CHO + H_2 \\
C_2H_4 + H &= C_2H_3 + H_2 \\
C_2H_6 + H &= C_2H_5 + H_2
\end{align*}

It is then produced by reaction 12) and 21):
21) \( \text{H}_2 + \text{O} = \text{OH} + \text{H} \)

The figure 6.47 suggests that all the reactions that involve molecular hydrogen become less important as the steam percentage increases.
At the light of these results it emerges that water acts increasing the rate of third-molecular reactions, since its highest efficiency as third-body species, in comparison with nitrogen, and of reaction 16) \((\text{OH} + \text{OH} = \text{H}_2\text{O} + \text{O})\) thus enhancing the production of OH radicals. Rates of reactions that involve these radicals are enhanced and at the same time the reactions that involve O, and H radicals slow down.

Indeed the steam significantly affects the evolution of the whole oxidation process. Since it is mainly based on radical branching reactions, in order to further characterize the effect of steam, it can be interesting to observe the vicissitude of H, O and OH radicals.

Figure 6.48 shows the reactions relative to the radical H. Reactions that produce H radicals are reported below:

8) \(\text{CHO} + \text{M} = \text{CO} + \text{H} + \text{M}\)
10) CO + OH = CO₂ + H
12) H₂ + OH = H₂O + H
   H₂ + O = OH + H
22) CH₃O + M = CH₂O + H + M
23) C₂H₅ = C₂H₄ + H

while it is consumed by these reactions:

CH₄ + H = H₂ + CH₃
4) CH₃ + H = CH₄
18) CH₂O + H = CHO + H₂
19) C₂H₄ + H = C₂H₃ + H₂
20) C₂H₆ + H = C₂H₅ + H₂
24) O₂ + H = OH + O
25) O₂ + H + M = HO₂ + M
26) HO₂ + H = OH + OH

Also in this case it is clear that the rate of reactions that involve H radicals decrease in a proportional way respect to the steam concentrations (18, 4, 1, 19, 20). On the contrary reactions that involve HO₂ radicals (26) or a third- body M (22, 25) have a higher importance in the methane oxidation process in these operative conditions.

In particular it is very important to see how water acts on the branching reactions. The reactions that lead to a huge amount of radicals, as explained in chapter II, are the reactions 21), 24) and 12). When reaction 24) starts it is followed by the reactions 12) and 21). They enhance the pool of radicals thus the reactivity of the system. Reaction 24) can compete with the breaking reaction (25); this reaction leads to the formation of HO₂ radicals that are less reactive that radicals OH. If reaction 25) is favored respect the chain branching reactions (24, 12, 21) the reactivity of the system is lowered.
The competition between the two reactions depends mainly on the working temperature, the pressure and diluents of systems.

Now in figure 6.48 it is evident that reaction 25) becomes faster and faster as the steam concentration is increased. It is mainly due again to the higher water third body efficiency in third-molecular reactions. It is worth noting that in absence of steam the evolution of oxidation process would be based on the typical high temperature H₂-O₂ system branching reactions.

![Figure 6.49](image)

**Figure 6.49** Reaction rates of H as function of the composition of the diluent in the system CH₄/O₂/N₂-H₂O.

The same results can be achieved considering the rate of production and consumption of the radical HO₂. Figure 6.49 shows the most important reactions for this radical as function of the diluent compositions. It is mainly consumed by reaction 26), 11) and reaction 7). In particular reaction 26) leads to the formation of two OH radicals. It is produced mainly by reaction 25).
Figure 6.50 shows the reactions and their rate of production or consumptions relative to radicals O. Also in this case it emerges that the branching reactions are repressed while the reaction between O radicals and water is increased.

Figure 6.51 shows the reaction rates of OH as function of the composition of the diluent in the system CH₄/O₂/N₂-H₂O.

In this case it is evident how the reactions between species containing carbon atoms and the radical OH become faster as the steam percentage increases.

OH radicals are mainly produced by reaction 26), 24) and 21) and consumed by reactions.12), 10) and 3). Also in this case it is meaningful that the oxidation process, passing from a system diluted in nitrogen to a system diluted in water; goes by from operative conditions in which the combustion would be sustained by the branching reactions to a combustion based on the breaking reaction and the reaction of breakdown of water.
Figure 6.51  Reaction rates of OH as function of the composition of the diluent in the system CH₄/O₂/N₂-H₂O.

The same analysis has been repeated for the same system but with an inner temperature equal to 1650K. Such new simulations have been run in order to study how steam affects the oxidation of methane as function of the temperature. In this case just the systems entirely diluted with nitrogen and with steam have been considered.
The reactions relative to methane are reported in figure 6.52. It can be seen how the reaction 1) becomes slower as soon as the diluent is changed from nitrogen to steam. On the contrary reaction 3) becomes faster following a behavior already discussed in this section. The reactions of methane with radicals O almost disappear for the system diluted in steam.

![Figure 6.52 Reaction rates of OH as function of the composition of the diluent in the system CH₄/O₂/N₂-H₂O.](image)

A similar analysis has been realized also for the species CO. Reaction rates are reported in figure 6.53. It mainly oxidizes to CO₂ reacting with OH radicals. It is produced by means of several reactions shown in the figure. In particular should be noted that the presence of water significantly enhances the reaction rate of reaction 8) \((\text{CHO} + \text{M} = \text{CO} + \text{H} + \text{M})\).
Reactions that mainly produce and consume the radical O are the following:
24) $O_2 + H = OH + O$

$H_2 + O = OH + H$

16) $OH + OH = H_2O + O$

It can be noted that surprisingly reaction 24) is faster for the system diluted in steam while reaction 22) still remains slower. $O$ radicals are consumed again by reaction 16) in the system diluted with water. It indicates that steam still affects the evolution of the oxidation process.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure6.55.png}
\caption{Reaction rates of $OH$ as function of the composition of the diluent in the system $CH_4/O_2/N_2-H_2O$.}
\end{figure}

In figure 6.55 the reaction rates for the radical $OH$ are reassumed for the two considered systems. In this case the same considerations made for the radical $O$ can be applied. But in particular it is worth noting that the rate of the reaction 12)($H_2 + OH = H_2O + H$) is still damped by the presence of steam.

The last system analysis considered is the one relative to the radicals $H$. the reaction
rates for this radicals are reported in figure 6.56.

There are a lot of reactions that do not appear in the figure 6.48, but for an inlet temperature equal to 1650K the oxidation of methane passes through other pathways. Anyway the most important aspect to underline is than reaction 25) \( \text{O}_2 + \text{H} + \text{M} = \text{HO}_2 + \text{M} \) does not appear in the figure.

![Figure 6.56](image)

**Figure 6.56**  Reaction rates of H as function of the composition of the diluent in the system \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \).

It appears clear that steam still affects the evolution of the oxidation process. In particular for the two systems considered the oxidation process is sustained by the typical branching reactions of the system \( \text{H}_2-\text{O}_2 \) and the breaking reaction is not active in this operative conditions. In fact in this case reaction 24), and 22) are relatively fast while reaction 25) has a very low reaction rate. Anyway steam still influences the evolution of the oxidation process limiting the rate of reaction 12) and enhancing the reaction rate of reaction 16) \( \text{OH} + \text{OH} = \text{H}_2\text{O} + \text{O} \).
Methane conversion and acetylene yield

In order to understand the methane conversion as function of the steam concentration and of the temperature the net rate of consumption has been considered.

Figure 6.57 plots the net consumption rate of methane for a system diluted \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \) diluted with nitrogen and steam up to 90% with various water percentages at 1200K.

![Graph showing net consumption rate of methane](image)

**Figure 6.57** Net consumption rate of methane for a system diluted \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \) with various water percentages at 1200K.

The figure clearly shows that as the steam concentration increases, the net rate of production decreases, hence the methane conversion decreases.

Figure 6.58 plots the net consumption rate of methane for a system \( \text{CH}_4/\text{O}_2/\text{N}_2-\text{H}_2\text{O} \) diluted with nitrogen and steam up to 90% with various water percentages at 1650K.

In this figure it is shown that as the steam concentration increases, the net rate of production firstly slightly decreases but then increases. For the systems diluted in water up to 50% and 100% the net rate of consumption is significantly higher than in the other cases hence the methane conversion increases.

In order to understand the shift of the maximum acetylene production towards lower
inlet temperatures the modified Arrhenius expression $K = A * T^b * (-E/RT)$ for some important reactions has been plotted as function of the temperature.

![Figure 6.58](Net consumption rate of methane for a system diluted CH$_4$/O$_2$/N$_2$-H$_2$O with various water percentages at 1650K.)

The reactions of the recombination channel by means of radicals species of the system H$_2$-O$_2$ have been considered. The reactions and the relative kinetic constants have been reported in tab. 6.1

The dimensions of the kinetic constants are expressed in cm, mol, s, and E in Joules/mol.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>$A$ (mol/sec cm$^6$)</th>
<th>$b$</th>
<th>$E_a$ (Joules/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$_2$H$_4$+H=C$_2$H$_3$+H$_2$</td>
<td>5,40E+14</td>
<td>0</td>
<td>62900</td>
</tr>
<tr>
<td>C$_2$H$_4$+O=CH$_2$CHO+H</td>
<td>1,02E+06</td>
<td>2,1</td>
<td>0</td>
</tr>
<tr>
<td>C$_2$H$_4$+O=CHO+CH$_3$</td>
<td>2,42E+06</td>
<td>2,1</td>
<td>0</td>
</tr>
<tr>
<td>C$_2$H$_4$+OH=C$_2$H$_3$+H$_2$O</td>
<td>2,20E+13</td>
<td>0</td>
<td>24900</td>
</tr>
<tr>
<td>C$_2$H$_6$+H=C$_2$H$_5$+H$_2$</td>
<td>1,40E+09</td>
<td>1,5</td>
<td>31100</td>
</tr>
<tr>
<td>C$_2$H$_6$+O=C$_2$H$_5$+OH</td>
<td>1,00E+09</td>
<td>1,5</td>
<td>24400</td>
</tr>
<tr>
<td>C$_2$H$_6$+OH=C$_2$H$_5$+H$_2$O</td>
<td>7,20E+06</td>
<td>2</td>
<td>3600</td>
</tr>
</tbody>
</table>

Table 6.1  Reactions and relative kinetic constants
Figure 6.59 shows the Arrhenius law as function of temperature for several ethane reactions. It is clear that OH radicals mainly dehydrogenate ethane. The depletion of O and H atoms and the enhancement of OH radicals, as shown earlier in the previous paragraph, make the consumption of ethane to be faster as the water concentration increases.

The Arrhenius expression for several ethene reactions is reported as function of temperature in figure 6.60.

The curves relative to the reaction of C\textsubscript{2}H\textsubscript{4} with H and OH radicals intersect for an inlet temperature of about 1450K. Hence for a lower temperature respect to this value the reaction C\textsubscript{2}H\textsubscript{4} + H → C\textsubscript{2}H\textsubscript{3} + H\textsubscript{2} is less fast than the reaction C\textsubscript{2}H\textsubscript{4} + OH → C\textsubscript{2}H\textsubscript{3} + H\textsubscript{2}O, while for higher temperature their relative importance inverts. Anyway the most influential reaction of ethene should be the dehydrogenation by means of O radicals.

The depletion of H and O radicals and the enhancement of OH concentration induce to a higher consumption of this species.

Hence during the oxidation of methane in Mild conditions in system diluted in nitrogen and water, as the percentage of steam increases, the recombination channel plays
a role always less relevant and all the methyl radicals, that pass through the recombination pathway, form ethane that more rapidly is dehydrogenated to acetylene. Hence the concentration of C₂H₂ increases as the steam concentration increases. At the same time acetylene mainly consumes reacting with O and H atoms. Since the amount of this species is suppressed by steam it cannot react and accumulates.

From the rate of production analysis as function of the steam concentration and of the temperature it has emerged that methyl radicals prefer reacting with OH radicals more then forming ethane, thus they do not feed the recombination channel as the steam concentration or the temperature increases.

Hence the maximum of acetylene shift towards lower temperatures in dependence of steam concentration.

This is a possible explanation of the shift of the acetylene maximum towards lower temperature, but numerical integrations and experimental sampling should support this idea. This was not the aim of the thesis, hence this aspect has not been thoroughly investigated.
Mixing configuration efficiency: Experimental and Numerical Results

Comparison between the configurations with 6 injectors located on the wall or protruded 1mm in the cylindrical duct

The mixing efficiency has been evaluated on the basis of fluorescence measurements, as reported in chapter IV. For any considered geometry, it has been calculated the Standard Deviation of the fluorescence intensity profiles along a diameter of the duct. This statistic tool gives an indication on the uniformity of fluorescence signal along the reactor diameter and hence of the mixing. The comparison among the mixing efficiencies of the several studied configurations has been realized on the basis of this statistical parameter.

The non-uniformity of mixing, hence the standard deviation of the normalized fluorescence intensity signal along a diameter of the duct sited in cross sections at different axial positions, has been used to compare the configurations analyzed in this chapter.

The comparison between the configuration with 6 injectors located on the wall of the cylindrical duct and the configuration with 6 injectors protruded 1mm inside the duct is presented in fig. 6.61. In both the configurations the diameter of the nozzles is equal to 0.9mm. Hence, since the geometry of the injectors, the lateral and the main flow rates are the same, the values of the parameter $J$ in both the cases will be equal. For both the systems the optimum value of $J$, according to Holdeman equation, is $J_{opt}=11$.

Therefore the StD has been plotted as function of the momentum of the jet to main stream ratio $J$ on curves parametric in the axial coordinate (x=1mm, 1cm and 2 cm).

In the figure the continuous lines are relative to the configuration with no protrusion ($p=0$) of the injectors whereas the dashed lines to the system with injectors protruded 1mm inside the duct ($p=1mm$).
The first relevant difference is that for the system with \( p=0 \), the \( StD \) decreases monotonically for any axial distance from the convergent, whereas in the other case it decreases monotonically just for \( x=1\text{mm} \) but for the other two axial considered positions it firstly decreases, then it reaches a minimum value and than it increases.

For \( J=0.5 \) the values of the \( StD \) for the system \( p=0 \) are higher than the ones relative to the system with \( p=1 \). As matter of fact, for \( J=0.5 \) the \( StD \) is equal to 0.89 at \( x=1\text{mm} \), 0.78 at \( x=1\text{cm} \) and 0.68 at \( x=2\text{cm} \) for the system with no protrusion, whereas it is 0.66 at \( x=1\text{mm} \), 0.47 at \( x=1\text{cm} \) and 0.39 at \( x=2\text{cm} \) for the system with 1mm of protrusion.

At \( x=1\text{mm} \) and for \( J>3 \) the \( StD \) values become very similar, even if for \( J=17 \) the system with no protrusion allows for a better mixing, in fact the system non-uniformity is 0.14 for \( p=0 \) and 0.23 for \( p=1 \).

At \( x=1\text{cm} \) the system with no protrusion has standard deviation values higher than the other system until \( J=6 \). As matter of fact, for \( J>6 \) the \( StD \) of the system with \( p=1 \) starts increasing and overcomes the values that compete to the system with the nozzles located on the wall of the duct.

Similar considerations apply for the mixing non-uniformity of the cross section located at \( x=2\text{cm} \). In particular the system with protruded nozzles, has a minimum value of the \( StD \) at \( J=3 \), afterwards it increases and becomes higher than the \( StD \) values that compete to the system with \( p=0 \).

The \( StD \) is lower than 0.2 just for \( J=3 \) and 4 at an axial distance from the convergent equal to 2cm for the system with protrusion of the injectors, while for the other system for \( J>6 \) and \( x=2\text{cm} \).

In general it is possible to assess that the system with no protrusion allows to reach the best mixing since it provides the lowest \( StD \) values in the comparison between this two configurations, but for \( J<5 \) the configuration with protrusion is to be preferred. The higher
penetration of the jets, induced by the protrusion of the injectors, becomes useful for low values of $J$, but for high $J$ it is not the best configuration since the tracer penetrates too much inside the duct and form a central core rich in acetone that persists for a meaningful axial distance and a near-wall region with no acetone. This acetone distribution causes the lowering of the mixing degree.

![Graph showing comparison between Standard Deviations for geometries with 6 holes and $d=0.9\text{mm}$ located on the wall ($p=0$) and protruded 1mm ($p=1$) inside the cylindrical duct.]

**Figure 6.61** Comparison between the Standard Deviations for the geometries with 6 holes and $d=0.9\text{mm}$ located on the wall ($p=0$) and protruded 1mm ($p=1$) inside the cylindrical duct.

Another parameter that has been used in the analysis of the mixing degree is the diameter $D$ of the inner zone where a low or no fluorescence intensity signal has been measured by mean of the optical set-up. The trend of this new parameter has been reported in fig. 6.62 as function of $J$.

At $x=1\text{mm}$ the values of $D$ are very similar but it is evident that in the system with $p=0$ the central region needs an higher $J$ to fade, in fact the diameter $D$ goes to zero for $J=8$, while in the system with $p=1$ the same condition is respected for $J=5$. This is again due to the higher penetration of the jets induced by the protrusion of the injectors in the main duct. For $x=1\text{cm}$ and $x=2\text{cm}$ the values of the parameter $D$ are very similar.
The same analysis has been performed for the configuration with 6 injectors located on the wall of the cylindrical duct and the configuration with 6 injectors protruded 1mm inside the duct but with a diameter of the nozzles equal to 0.9mm.

![Diagram showing comparison between geometries](image)

**Figure 6.62** Comparison between the diameter $D$ of the zone with a low intensity signal for the two geometries with 6 holes and $d=0.9\text{mm}$ located on the wall ($p=0$) and protruded 1mm ($p=1$) inside the cylindrical duct.

Since the geometry of the injectors, the lateral and the main flow rates are the same, the values of the parameter $J$ in both the cases will be equal. For both the systems the optimum value of $J$, according to Holdeman equation, is $J_{\text{opt}}=11$. 


Fig. 6.63  Comparison between the Standard Deviations for the geometries with 6 holes and $d=0.8\text{mm}$ located on the wall ($p=0$) and protruded 1mm ($p=1$) inside the cylindrical duct.

The comparison has always been realized on the basis of the mixing non-uniformity values. They are reported in fig. 6.63 as function of the parameter $J$ on curves parametric in the axial coordinate.

The results are analogous to the ones presented in the previous case.

Fig. 6.64  Comparison between the diameter $D$ of the zone with a low intensity signal for the two geometries with 6 holes and $d=0.8\text{mm}$ located on the wall ($p=0$)
and protruded 1mm (p=1) inside the cylindrical duct.

It is evident that for $J$ values up to 6, the configuration with protruded injectors is better than the other one, but for $J>8$ the system with no protrusion is more efficient.

In fig. 6.64 the trend of the dimension of the central core with a low signal of fluorescence is reported for the case of 6 holes with a diameter of 0.8mm not protruded and protruded of 1mm inside the duct on curves parametric in the axial coordinate.

Also in this case it is evident that such a diameter decreases with an higher gradient in the system with $p=1$. Anyway the values are comparable among than once the $J$ and the axial position is fixed.

**Comparison between the geometries with 6 and 10 injectors sited on the wall of the cylindrical duct**

The comparison between the mixing efficiency of the systems with injectors sited in the wall of the cylindrical duct has been performed on the basis of the standard deviation of the normalized fluorescence intensity profiles along a diameter of the cross sections located at $x=1$mm, 1cm and 2cm. The $StD$ has been plotted both as function of the momentum of the jet to the main flow stream $J$ and of the helium and acetone flow rate $Q_{He+C_3H_6O}$. In fact, since the global lateral flow is the same but it is distributed among a different number of injectors the velocity of the lateral flow is different in the two configurations, it means that the momentum of the jet to the main flow stream $J$ will be different. Hence, to compare the results on the basis of the same axial coordinate the $StD$ has been plotted also as function of $Q_{He+C_3H_6O}$.

For the system with 6 holes ($n=6$) the $J_{Hopt.}$ is equal to 11 while the for the system with 10 injectors $J_{Hopt.}$ is 32.

Fig. 6.65 shows the mixing non-uniformity as function of $J$ on curves parametric in
the axial coordinate for the two systems taken in consideration.

For any axial distance it is clear that the StD that competes to the system with 6 nozzles is lower respect to the system with 10 injectors.

In particular it is meaningful the difference of the standard deviation for low values of \( J \). In fact for the system with \( n=10 \) at \( x=1\text{mm} \) for \( J=2 \) the StD is 1.2 while for the system with \( n=6 \) for \( J=0.5 \). This huge difference also for the other axial system. For \( J_{\text{Hopt.}} \) and \( x=2\text{cm} \) the values of the standard deviation is for the system with \( n=6 \) is 0.16 whereas it is 0.15 for the other system. Hence both the systems ensure a good mixing degree.

![Figure 6.65](image)

**Figure 6.65**  Comparison between the Standard Deviations as function of \( J \) for the geometries with 6 holes and \( d=0.8\text{mm} \) located on the wall \( (p=0) \) geometries with 10 holes and \( d=0.5\text{mm} \) located on the wall \( (p=0) \).

To get more information it is convenient to plot the parameter index of the mixing non-uniformity as function of \( Q_{\text{He+C,H,O}} \). The global lateral flow rate changes from 600NI/h a 3900NI/h (Fig. 6.66).

Also in this case, it is evident that at \( x=1\text{mm} \) the lowest StD competes to the system with 6 hole while only for the \( Q_{\text{He+C,H,O}}=3900\text{NI/h} \) the two configuration are equivalent. At \( x=1\text{cm} \) the same situation is proposed but the mixing non-uniformity becomes higher.
for the system with \( n=6 \) respect to the system with \( n=10 \) for \( Q_{\text{He+C,H,O}} > 2700 \text{Nl/h} \). At \( x=2\text{cm} \) this switch is realized for \( Q_{\text{He+C,H,O}} > 2500 \text{Nl/h} \).

It is worth noting again that for very low value of the lateral flow rate it is the system with 6 holes to provide for the best mixing. In fact the biggest difference between the mixing of the two systems are reached for \( Q_{\text{He+C,H,O}} < 2500 \text{Nl/h} \) for \( x=1\text{mm} \) and 1 cm. For \( x=2\text{cm} \) the StD are not so different.

**Figure 6.66** Comparison between the Standard Deviations as function of \( Q_{\text{He+C,H,O}} \) of for the geometries with 6 holes and \( d=0.8\text{mm} \) located on the wall \((p=0)\) geometries with 10 holes and \( d=0.5\text{mm} \) located on the wall \((p=0)\).

The comparison between the two configurations can be done also on the basis of the diameter \( D \) of the inner zone where a low or no fluorescence signal is visible.

Fig.6.67 shows how the parameter \( D \) changes as function of \( J \) on curves parametric in the axial distance. In fig 6.68 \( D \) is plotted as function of the lateral flow rate. In both the cases it is possible to see that the internal zone dimension decreases more slowly in the system with 10 holes respect to the system with 6 holes.

In general the more the number of jets, the lower the jets penetration is but the more
merged they are.

In other words, an increase of the number of jets, keeping constant the whole lateral flow, means that the velocity is lower, hence the jets penetrate for a inferior radial distance towards the centre of the duct. Hence, the internal zone with no acetone increases. At the same time, a higher number of injectors ensures an higher distribution of the tracer, hence the jets will merge among them but they will not penetrate so much.

In any case, the configuration with 6 holes seems to be more efficient.

![Figure 6.67](image.png)

**Figure 6.67** Comparison between the diameter $D$ of the zone with a low intensity signal as function of $J$ for the geometries with 6 holes and $d=0.8\text{mm}$ located on the wall ($p=0$) geometries with 10 holes and $d=0.5\text{mm}$ located on the wall ($p=0$).
Figure 6.68  Comparison between the diameter $D$ of the zone with a low intensity signal as function of $Q_{He+C_3H_6O}$ for the geometries with 6 holes and $d=0.8mm$ located on the wall ($p=0$) geometries with 10 holes and $d=0.5mm$ located on the wall ($p=0$).

Comparison between the geometries with 6 injector with a diameter equal to 0.8 mm and 0.9 mm located on the wall of the cylindrical duct

The comparison between the mixing efficiency of the systems with 6 injector with a diameter equal to 0.8 mm and 0.9 mm located on the wall of the cylindrical duct has been performed on the basis of the standard deviation of the normalized fluorescence intensity profiles along a diameter of the cross sections located at $x=1mm$, 1cm and 2cm. The $StD$ has been plotted both as function of the momentum of the jet to the main flow stream $J$ and of the helium and acetone flow rate ($Q_{He+C_3H_6O}$). In fact, since the global lateral flow is the same but the dimension of the injectors are different, the velocities of the jets, as well as the momentum of the jet to the main flow stream $J$, will be different. Hence, to compare the results on the basis of the same axial coordinate the $StD$ has been plotted also as function
of $Q_{He+C_3H_6O}$.

For both the system the $J_{Hopt}$ is equal to 11.

**Figure 6.69** Comparison between the Standard Deviations as function of J for the geometries with 6 holes and $d=0.8\text{mm}$ $d=0.9\text{mm}$ located on the wall $(p=0)$ of the cylindrical duct.

Fig. 6.69 shows the mixing non-uniformity as function of the momentum of the jet to the main flow stream $J$ on parametric curves in the axial position. The dashed line are relative to the configuration with 6 holes with an inner diameter equal to 0.9mm, while the continuous lines are relative to the system with the same number nozzles but with an inner diameter equal to 0.8mm.

For $J=J_{Hopt}=11$ and $x=2\text{cm}$ the systems seem to be equivalent.

Fig 6.70 shows the mixing non-uniformity as function of the helium and acetone flow rate $Q_{He+C_3H_6O}$. It is worthwhile noting that for $x=1\text{mm}$, $x=1\text{cm}$ and $x=2\text{cm}$ the $StD$ for the system with $d=0.9\text{ mm}$ is always higher than the ones relative to the other system, even if this difference is not so relevant. In fact, the values of the $StD$ slightly differ from each other for a fixed axial position and for a fixed value of the lateral flow rate $Q_{He+C_3H_6O}$.

At $x=2\text{cm}$ for the system with $d=0.9\text{mm}$ the **Standard Deviation (StD)** is lower than
0.2 from $Q_{He+C_3H_6O}>1500\text{Nl/h}$, while for the other system from $Q_{He+C_3H_6O}>2200\text{Nl/h}$.

![Figure 6.70](image)

**Figure 6.70**  *Comparison between the Standard Deviations as function of $Q_{He+C_3H_6O}$ of for the geometries with 6 holes and $d=0.8\text{mm}$, $d=0.9\text{mm}$ located on the wall ($p=0$) of the cylindrical duct.*

A further paragon between the two chosen configurations can be realized considering the diameter $D$ of the inner zone where a low or no fluorescence signal is detectable. In fig 6.71 $D$ is plotted as function of the lateral flow rate.

In is possible to note that to the configuration with injectors with an inner diameter (ID) equal to 0.9mm competes the highest values of the parameter $D$.

In particular at $x=1\text{mm}$, the zone where the fluorescence intensity is very low disappears for $Q_{He+C_3H_6O}=2500\text{Nl/min}$ for the system with an inner diameter equal to 0.9, while in the other system the same condition is respected for $Q_{He+C_3H_6O}=1800\text{Nl/h}$.
Figure 6.71  Comparison between the diameter $D$ of the zone with a low intensity signal as function of $Q_{He+C_3H_6O}$ for the geometries with 6 holes with $d=0.8\text{mm}$ and $d=0.9\text{mm}$ located on the wall ($p=0$) of the cylindrical duct.

Therefore, the configuration with an inner diameter equal to 0.8mm results to provide for a better mixing in comparison with the configuration with holes with an inner diameter equal to 0.9mm. As matter of fact, the jet velocity that competes to the former system is higher since the dimension of the nozzles is smaller. This results in an higher values of $J$ and in a better penetration. Thus the jets penetrate further in the main duct and allows the tracer to be spread out on all the cross section, whereas in the configuration with diameters of 0.9mm, the jets penetrate for a smaller distance towards the central of the duct respect to the other case considered, and there forms a wider central region where acetone does not concentrate.

This leads to an increase of the non-uniformity of the mixing.

The numerical results were compared on the basis of the standard deviations of the acetone concentration profiles along a diameter of the duct at several cross section for any configuration considered in the numerical integrations. Comparisons are presented in the
Comparison between the configuration with 6 and 10 injectors located on the wall of the cylinder duct

The aim in this paragraph is to compare the geometries analyzed. In particular the configurations with 6 and 10 injectors, located on the wall of the cylindrical duct with no protrusion, have been considered. Before performing this analysis, it is important to underline than the main flow and the lateral flow, injected by the nozzles inside the main duct in the two systems considered, are the same. The different dimension and number of injectors entail that the values of the momentum of the jet to man stream ratio $J$ is unequivocally different. Hence the comparison will be realized as function of parameter $J$ but also as function of the total lateral flow rate ($Q_{He+C3H6O}$).

Fig. 6.72 show the mixing dis-uniformity as function of the parameter $J$, for the two chosen configurations, at different axial position from the convergent (respectively 1mm, 1cm and 2cm). It is possible to note that for any axial distance the value of the $StD$ that competes to the system with 6 holes is always lower respect to the geometry with 10 holes.

Fig. 6.73 show the mixing dis-uniformity as function of the parameter $Q_{He+C3H6O}$, for the two chosen configurations at different axial position from the convergent (respectively 1mm, 1cm and 2cm). The value of the parameter $Q_{He+C3H6O}$ goes from 1200NI/h to 4000NI/h. It is evident that the configuration with 6 hole ensure a best mixing respect to the other geometry, in fact for any axial distance and for the most of the $Q_{He+C3H6O}$ values, the value of the $StD$ is lower in the first configuration.
Comparison between the Standard Deviation as function of the parameter $J$ at different axial position for the geometries with 10 and 6 injectors located on the wall of the cylindrical duct.

Comparison between the configuration with 6 injectors located on the wall of the cylinder duct and the configuration with 6 holes and a protrusion inside the cylinder duct.
equal to 1 mm.

The comparison between the configuration with 6 injectors located on the wall of the cylinder duct and the configuration with 6 holes and a protrusion inside the cylinder duct equal to 1 mm is reported in fig. 4.5.12.

The mixing dis-uniformity is reported as function of the parameter \( J \), for the two chosen configurations, at different axial position from the convergent (respectively 1 mm, 1 cm and 2 cm).

Since in this case the number and dimension of holes is the same there is no need to have two different diagrams. In fact the values of the parameters \( J \) and \( Q_{He+C_{3}H_{6}O} \) are the same in the two analyzed configuration.

In fig. 6.73 it is possible to note that the values of the \( StD \) are very different. The trend of the mixing disuniformity is always decrescent as function of \( J \) for any axial distance from the convergent for the system with no protrusion. The other configuration shows a minimum value of the mixing disuniformity for \( J=9 \) than it starts increasing.

For any axial distance and for \( J \) from 3.5 to 11 the configuration with the protrusion inside the duct allows for a best mixing of the different species. For \( J>11 \) the same configuration does not provide for the best solution. For instance, for \( J=13 \) and \( x=1 \) cm the value of the \( StD \) is higher in the case of the 6 injector protruded inside the duct. At \( x=1 \) cm and \( x=1 \) mm this inversion is detectable for \( J=16 \) and 19.

The worsening of the mixing for high \( J \) becomes evident at \( J \) equal to about 25 where the value of the \( StD \) in the case of the system with the protrusion at the axial coordinate \( x=1 \) cm becomes equal to \( StD \) without protrusion but at an axial distance from the convergent equal to 1 mm.
Figure 6.73 Comparison between the Standard Deviation as function of the parameter J at different axial position for the geometries with 6 injectors located on the wall of the cylindrical duct and 6 injectors protruded inside the cylindrical duct of 1mm.

Therefore, the geometry with 6 holes and a protrusion inside the main duct of 1 mm results to provide a better mixing for low values of J in comparison with the other geometry. In fact the protrusion of injectors inside the duct leads the jets to penetrate further towards the center of the duct. Hence for low values of $J$, it results in an improvement of the mixing. On the contrary when the values of $J$ are enough high to guarantee a good penetration of the jets, the protrusion causes on over-penetration of the jet, hence they tend to form a central core and the acetone is accumulated in this region. It causes and increase of the StD value and hence a worsening of the mixing.

Anyway these results suggest that the radial position of injection tubes is an important parameter in order to achieve an efficient mixing of reactants for experiment in the tubular reactor.
Discussion

Both the experiments and the numerical simulations clearly indicates that the best mixing is reached in the case of six holes with a inner diameter equal to 0.8. In fact the $StD$ reaches a value lower than 0.15 earlier than the other configurations. The analyses anyway show that an important parameter to shorten the mixing time is the position of tube inside the main duct.

Therefore the mixing configuration and the reactor have been dimensioned.

The reactor that will be used at high temperature has been designed and realized. It is shown in Fig.6.74. The first part is the mixing section. Six round, equally spaced, holes are displaced on the perimeter of the first cylindrical duct at a radius distance to the convergent. They house alumina tubes for lateral injection with an inner diameter equal to orifice diameter computed from $J_{Hopf}$, sizable on request. The reactor is divided into ten modules. A 10 cm sapphire tube and an alumina disk form each module. Adjacent modules will be connected by two alumina threaded rods and bolts. Disks are provided of an admission in order to allow for species or temperature sampling. In order to avoid possible leakages a special ceramic sealer with a high content of alumina will be used. Sapphire has been also chosen because of its high transparency in the visible and ultraviolet wavelength range. The chosen materials are alumina and sapphire for their physic properties: high thermal resistance, low conductibility and low thermal expansion coefficient, inert and resistant in oxidant environment. Unfortunately alumina is fragile, hard and not easily machinable. Alumina is used for the injection part, threaded rods and disks.

These properties should allow the exploitation of elastic and anelastic light
scattering diagnostic techniques. These techniques are the most effective diagnostic tools for the non-intrusive, space and time resolved characterization of the combustion processes. The transparency of the reactor will also allow temperature profiles measurement along the reactor by means of a thermograph camera.

![Image of reactor and mixing section](image)

*Figure 6.74  Reactor and mixing section.*
CONCLUSIONS

The thesis has concerned the study of the behavior of model reactors in working conditions typical of a Mild Combustion process and has given a fundamental contribution for the comprehension of the oxidation process of small paraffins in “mild” operative conditions and also for the resolution of problems correlated to the difficulty to set-up a lab scale facility able to work with high inlet temperatures typical of the Mild combustion. This new combustion “mode” forecasts the use of a high dilution degrees and a high pre-heating of reactants. These operative conditions are very promising in the framework of the development of new combustion technologies aimed to enhance the efficiency and reduce the environmental impact of combustion systems. In fact they allow for a reducing of pollutants formation and save energy.

The first step has been the identification of model reactors that can allow for an accurate and exhaustive analysis of the chemistry and the dynamic evolution of the combustion process. The choice has fallen on the continuous stirred reactor (CSTR) and on the plug flow configurations. Both reactors allow for studying the evolution of the oxidation process as a succession of steady states as function of an unique parameter, which is in the case of the CSTR, the time and, in the case of the plug flow reactor the axial coordinate, or equivalently the time.

In literature there is not a consistent number of works on Mild processes in tubular flow reactors since the very high inlet temperatures imply very strict requirements on the materials to employ and on the efficiency of mixing devices. As matter of facts diluent and comburent have to be fed separately from the fuel in order to avoid undesired reactions in the pre-mixing section. At the same time they have to mix in a time relatively short in comparison with the ignition time of any mixtures that forms during the mixing process.
This constrain is very severe because the very high inlet temperatures enhance the oxidation reaction rates.

All these problems have properly faced, thus the contribution of this thesis to Mild combustion studies has been the designing and the setting up a tubular flow reactor that will be employed to characterize the Mild combustion as clean and cleaning technology.

The design of the tubular reactor has been realized by means of the classical equations of a plug flow reactor. Several parameters have been fixed in order to achieve a high-resolution time of the oxidation process, i.e. the residence time, and to satisfy safety (power plant) and space (axial length of the reactor) requirements. The dimensioning of the reactor responds to the requirement of achieving a full-developed motion of the fluid inside the reactor, in order to avoid velocity, temperature and species concentrations gradients in the radial coordinate of the system. In fact this condition guarantees that the evolution of the oxidation process can be easily studied as function of the axial coordinate of the reactor. From analytical calculations and the use of a computational commercial fluid-dynamic code (Fluent), with the aim to characterize the fluid-dynamic field, all the geometric parameters of the reactor have been assessed.

Furthermore the configuration has been designed in view of optical diagnostic analyses, species samplings and temperature measurements, in order to characterize the evolution of the oxidation process in terms of species production and concentration and temperature trend along the axial coordinate of the reactor. The reactor in fact has a modular structure. A 10-cm sapphire tube and an alumina disk form each module. Disks are provided of an admission in order to have species or temperature samplings and the sapphire will allow for optical diagnostic analyses.

The second step has concerned the choice and the dimensioning of the mixing section of reactants.
The selection of the mixing configuration has derived from a thorough study of mixing devices used in combustion systems. Mixing is realized with jets in cross flow configuration. Fuel is hence injected inside the main duct trough nozzles orthogonal to the directions of the main flow, which is composed by diluent and comburent at high temperature. The mixing efficiency has been evaluated as function of the parameters characteristic of this configuration by means of numerical simulations, using a computational fluid-dynamic commercial code (Fluent software) and experimental tests based on fluorescence measurements on a simplified configuration working at room temperature. Several geometries have been tested and finally the mixing section has been designed. The tubular reactor, the mixing section and the whole plant have been realized.

In the case of the CSTR configuration, it has been possible to carry out a thorough experimental campaign since the reactor and the plant were already present in a laboratory of the institute. Firstly the experimental facility has been modified in dependence of our needs and all the problems, related to the choice of the reactor, i.e. the mixing, and to the operative Mild conditions, i.e. high temperatures, have been faced. The experimental tests were realized to characterize the combustion regimes that establish during the oxidation of the system \( \text{CH}_4/\text{O}_2 \) diluted with nitrogen up to 90% as function of inlet temperatures and of the mixture compositions. The framework outlined by the experimental analyses underlines that extreme working conditions very different from the ones used in traditional combustion processes, can lead to a very complex system behavior. Several thermo-kinetic regimes corresponding to static and dynamic conditions were recognized. The efforts have been hence focused on the characterization of the new behavior. As matter of fact oscillations have been detected for paraffins with high molecular weights, but this is the first time they have been experimentally recognized for methane. Hence an accurate characterization of the dynamic region has been performed and several temperature
Conclusion

oscillation typologies have been identified. Results have been reassumed in a stability or ignition map (C/O feed ratio-T_{inlet}). On this plane it has been clearly identified a region where oscillation take place. The dynamic region extends for mixtures with a carbon/oxygen feed ratio lower than twice the stoichiometric ratio and for inlet temperatures comprised between 1050K and 1275K. Experimental tests has put in result another meaningful behavior of the system in discussions, in fact for high feed ratios, outside the dynamic region, and for inlet temperatures higher than 1175K a decrease of the reactivity of the system has been detected. In fact the reactor temperature increase was relatively low and assumed a constant value for further inlet temperatures increase.

The dynamic behavior and the exothermicity damping of the system have been investigated as function of the main parameters of the systems, i.e. residence time, and dilution degree of the system. They affect sensibly the insurgence of the dynamic behavior, in fact a decrease of the dilution decrease and an increase of the residence time imply a reduction of the extension of the dynamic region and an anticipation of the temperature decrease towards lower temperatures. Further experimental analyses have been performed in order to assess the effect of hydrogen addiction and of the nature of the diluent on the dynamic behavior. It has been shown that hydrogen oxidation kinetic significantly interacts with methane Mild Combustion process, in fact hydrogen addition decreases the characteristic kinetic times of the system and reduces the zone where dynamic behaviors occur, furthermore it provokes a shift of the reduction of the reactivity of the system towards lower inlet temperatures. Results suggest that the system is very sensible to the presence of hydrogen but not to its relative concentration. It implies that just small amount of hydrogen can be added to the system to influence the insurgence of oscillations. Similar effects have been achieved whether part of the diluent is substituted with steam water, while keeping constant the overall dilution degree. The results show that the reactivity of
the system slightly increases for low temperatures and the exothermicity of the system damps for lower temperatures respect to the system completely diluted in nitrogen. Furthermore steam water limits the insurgence of oscillations for rich mixtures and high temperatures. Numerical simulations have then shown that steam water interacts with the methane oxidation mechanism-giving rise to breakdown reactions thus enhancing the radical amount and the reactivity of the system.

From the study on the evolution of the dynamic phenomenology as function of the parameters of the system appear clear a common trend: the decreases of the dilution level, the decrease of the residence time, the hydrogen addiction and the dilution in steam water act enhancing thermally or kinetically the reactivity of the system inducing a reduction of the extension of the dynamic region and a shifts towards lower inlet temperature of the exothermicity damping recognized for high temperatures and rich mixtures in the stable combustion region.

The availability of kinetic oxidation mechanisms has suggested the possibility to go deep inside this new phenomenology by means of numerical simulations. Firstly it has been verified whether models were able to reproduce of the dynamic behavior detected experimentally. At the light of the good results obtained, kinetic models have been used to perform further simulations in order to understand what are the reactions responsible of the insurgence of the dynamic phenomenology and the exothermicity-damping of the system.

On the basis of comparison between experimental (C₂ species gas chromatographic samplings) and numerical results (species rate of production analysis) it has been supposed that the dynamical behavior evidenced during methane oxidation is due to the interaction between the kinetic of the methane oxidation and the thermal exchange between the reactor and the environment. Although the chain branching of the CH₄ reaction mechanism is basically due to the H₂/O₂ system, methane evolves according two main pathways that are
the oxidation and the recombination channels respectively. The rate of production analysis showed that recombination channel acts subtracting CH\(_3\) radicals from the oxidation channel, storing them as C\(_2\) compounds. In particular ethane can be dehydrogenated until the formation of the vinyl radical (C\(_2\)H\(_3\)). It can be further dehydrogenated to acetylene or oxidized to acetaldehyde.

When the chain branching starts, the recombination channel releases the CH\(_3\) radicals through the formation of acetaldehyde and its dehydrogenation until the formation of CH\(_3\)CO radicals. These, in turn, are thermally decomposed, producing CH\(_3\) radicals and CO that feed the oxidation channel enhancing the reactivity of the system and causing the temperature increase. If the recombination channel releases these radicals the system can evolve through an oscillation regime whereas if it stores them as C\(_2\)H\(_2\), the system evolves through a stable combustion regime characterized by a very low temperature increase.

Therefore, oscillations occur as result of the competition between the oxidation and recombination channels present in the kinetic mechanism of methane combustion while the exothermicity damping is linked to the prevalence of acetylene formation and its stabilization with respect to the oxidation of the recombination products with two carbon atoms when the rich mixture temperature is higher than a threshold value.

Therefore Mild Combustion conditions have been shown to significantly influence the fuel oxidation kinetic. The very high initial temperature and the very low concentration of reactants strongly modify the competitions among the different kinetic pathways thus stressing behavior that are usually hidden in traditional combustion conditions by very fast oxidation process both for high and low molecular weight hydrocarbons.

The information content of static and dynamic behavior can be useful to better understand the oxidation kinetic of small paraffins and to verify the effectiveness of kinetic models available in literature, focusing the attention to oscillation phenomenology and the
occurrence of the different thermo-kinetic regimes. In fact this experimental evidence represents a rigorous test for validation of kinetic models that must be able to predict the dynamic behaviors of reacting system, thus considering more stringent constraints.

From a practical point of view, the presence of such oscillatory regimes, due to thermo-kinetic behavior of the system, could induce a negative phenomenology. In fact, their coupling with physical processes could give rise to high frequency oscillations in combustion chambers, generally responsible of efficiency decrease and of serious damages in gas turbine burners. Such dynamic behavior is hidden in conventional processes involving methane by the relatively fast oxidation kinetic that characterizes traditional gaseous fossil fuels. Moreover, the activation of different kinetic pathways hypothetically responsible of oscillations could induce an increase of pollutant formation.

The results hence help to identify the operative condition in which a Mild Combustion process should be realized. The experimental results unambiguously show that the instability problems can be overcome by splitting the whole combustion process in two stages where the first one evolves in diluted rich conditions, i.e. C/O ratio where no oscillations were detected and second stage completes the oxidation process.

An alternative way to avoid these phenomenologies concerns the use of additive fuel that can act on oxidation kinetic improving the evolution of the system towards a static steady state. To this aim results suggest acting on the mixture composition or on the diluent. In fact small addiction of hydrogen to the system or the dilution of the system in steam water allows working with steady combustion for a larger number of operative conditions. Furthermore the highest reactivity induced by the presence of hydrogen suggests the possibility of using small amount of this clean fuel whether Mild combustion process has to be realized with low calorific power and less valuable fuels than methane.
APPENDIX
6 injectors with \( d=0.9\text{mm} \) located on the wall of the cylindrical duct

The second analyzed geometry presents 6 injectors with an inner diameter equal to 0.9 mm. They are equally displaced on the perimeter of the cylindrical duct at 60° of distance from each other.

In this case the optimal value of the *momentum of the jet to main stream ratio* \( J \) according to Holdeman equations is equal to 11 (\( J_{\text{Hopt}} \)). The numerical simulations have been run for a wide range of \( J \), from 0.5 to 17, in such a way it has been possible to analyzing the mixing in a wide range of conditions. If fact the analyses have been realized for \( J \) values lower and higher than the \( J_{\text{Hopt}} \).

The bi-dimensional implementation of the fluorescence measurements performed for this configuration is presented in figure 1.

The acetone distribution inside the system is represented by the intensity of the pixel of images collected by means of the optical diagnostic facility well described in the first paragraph.

The fluorescence intensity has been divided into 16 levels and colors, and the values have been normalized in comparison to the highest intensity value of all the images collected for the several configurations considered, in order to compare all the experimental results among them. The normalized pixel intensity values go from 0 to 1800. The images have been collected for three different cross sections located in the plane \( x=0 \) and at an axial distance equal to \( x=1\text{mm} \), \( x=1\text{cm} \) and \( x=2\text{cm} \). In the figure it is also reported the laser beam that hits the cylindrical duct. The figure allows the analysis of the acetone distribution as function of the parameter \( J \), once the axial position has been fixed, as well as the analysis of the acetone distribution as function of the axial position, if the value of the parameter \( J \) has been fixed.
Figure 1  Fluorescence Intensity images as function of the parameter J in curves parametric on the axial position for the configuration with 6 holes with a inner diameter equal to 0.9 mm positioned on the wall of the cylindrical duct.
APPENDIX

At the axial position equal to 1mm and for values of \( J \) from 0.5 to 6, there is a wide region where a low or no fluorescence signal is detectable. Acetone mainly accumulate in the near-wall region. For \( J=8 \) the intensity fluorescence begins to be consistent but the signal is not uniform. The same consideration applies for \( J=11 \) and \( J=14 \). For a value of the parameter \( J \) equal to 17 the signals appears more uniform in all the points of the cross section.

In section located at \( x=1cm \) the internal region with a concentration of acetone close to zero tends to fade as \( J \) is increased from 0.5 to 3 and it completely disappears for \( J \) equal to 4. from \( J=4 \) to \( J=11 \) the intensity signal is increasingly higher in the central region but the signal becomes uniform for \( J=14 \).

In the cross section located at \( x=2cm \), for \( J \) comprised between 0.5 and 2, the region where the intensity signal is not detectable is still present but it diminishes and disappears for \( J=3 \). For \( J=4 \) and 5 intensity I the center of the cross section increases and the signal seems to be uniform for \( J=6 \). For \( J>6 \) the tracer is spread out on all the surface and a good mixing degree is reached.

It is also possible to analyze the trend of the uniformity of the signal as function of the axial distance from the convergent once the parameter \( J \) is fixed.

For \( J=0.5, 1 \) and 2, at \( x=1mm \) the fluorescence signal comes from the near-wall region but in the center of the cross section the white color suggests the complete absence of acetone. As the axial distance increase the only difference is that the white region extension reduces.

For \( J=3 \) and at \( x=1mm \) and 1cm the region with no signal is still present but at \( x=2cm \) the acetone begins to spread out towards th center of the duct.

For \( J=4 \) and \( J=5 \) for \( x=1mm \) the acetone has a relatively low concentration in the center of the cross section but it accumulates in the near-wall region. For \( x=1cm \)
and 2cm the acetone spreads toward the internal area ut its concentration is still lower in comparison with the surroundings.

For $J=6$ and $x=1mm$ a low concentration nucleus is still evident but it fades for $x=1cm$ and the situation improves at $x=2cm$ where the signal begins to be more uniform.

For $J=8$ and $J=11$ at $x=1mm$ the acetone is present in all the area but it is not homogeneously distributed. The distribution improves at $x=1cm$ and at $x=2cm$ the tracer is uniformly spread out.

For $J=14$ and $J=17$ the segregated zone with a low signal is very narrow and for the other two axial position the acetone is well distributed in the whole cross section.

In fig.2 the fluorescence intensity signal is plotted along a diameter of the duct at the known axial distances for any $J$ value analyzed.

In these figures the fluorescence intensity has been normalized respect to its mean value for each working condition. In such a way the profiles have been made independent on the acetone concentration and they can be reasonably compared among them.

The same analyses and considerations can be realized taking into account the normalized fluorescence profiles reported in figure 2. In this case the uniformity of acetone distribution is reached when profiles becomes flat.

For $J=0.5$ and $J=1$ it is evident that the jets do not penetrate sufficiently in the first section of the simplified configuration and the tracer tends to accumulate in the region close to the wall of the third section of the system.

For value of $J>8$ the fluorescence intensity profiles at $x=1cm$ and $x=2cm$ almost coincide.
Figure 2: Fluorescence Intensity signal profiles as function of the parameter $J$ in curves parametric on the axial position for the configuration with 6 holes with a inner diameter equal to 0.9 mm positioned on the wall of the cylindrical duct.
In fig. 3 the non-uniformity of the mixing, calculated on the basis of the standard deviation, is presented as function of the parameter $J$ on curves parametric on the axial position. The $StD$ has been calculated considering the normalized pixel fluorescence intensity values presented in fig. 2.

The higher the momentum of the jet to mainstream ratio, the lower the $StD$ is for any axial distance. As matter of fact, the $StD$ decreases monotonically as the parameter $J$ is increased. For $x=2\text{cm}$ it mainly diminishes from $J=0.5$ to $J=6$, than for all the axial distances it seems to reach a constant value. At $x=1\text{mm}$ the $StD$ goes from 0.9 to 0.21, while for $x=1\text{cm}$ it goes from values very close to 78 to 0.16, and for $x=2\text{cm}$ it interests $J$ values from 0.68 to 0.14.

The $StD$ is never lower than 0.1 but for $x=2\text{cm}$ is lower than 0.2 for $J>6$. For $x=1\text{cm}$ it is lower than 0.2 for $J>14$ while at $x=1\text{mm}$ it always higher than this value.

![Figure 3](image)

**Figure 3**  
Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position.

**6 injectors with d=0.8 mm located on the wall of the cylindrical duct**

The third analyzed configuration has 6 injectors with an inner diameter equal to 0.8 mm. They are equally displaced on the perimeter of the first cylindrical duct at $60^\circ$ of distance from each other.
Also in this case, the optimal value of the *momentum of the jet to main stream ratio* $J$ according to Holdeman equations is equal to 11 ($J_{\text{opt}}$). The numerical simulations have been run for a wide range of $J$, from 1 to 34. These values change in comparison with the configuration considered in the previous paragraph since, although the lateral flow rate is the same, the velocity of the lateral jets increases because of the cross section of the injectors is smaller. It means that the numerator of the $J$ formula is higher respect to the one that competes to the geometry with the same number of holes but with an inner diameter equal to 0.9 mm. Anyway also in this case, the mixing efficiency has been studied in a significant range of working conditions. As matter of fact, the analyses have been realized for $J$ values lower and higher than the $J_{\text{opt}}$.

The figure 4 shows the bi-dimensional implementation of the fluorescence measurements realized for this configuration. The fluorescence intensity signal is reported in the three cross sections located at an axial position equal to 1mm, 1cm and 2 cm as function of the *momentum of the jet to main stream ratio* $J$.

The images allow the analysis of the acetone distribution as function of the parameter $J$, once the axial position has been fixed, and the analysis of the acetone distribution as function of the axial position, one time the value of the parameter $J$ has been fixed. The fluorescence intensity has been divided into 16 levels and colors, and the values have been normalized in comparison to the highest intensity value of all the images collected for the several configurations considered, in order to compare all the experimental results among them. Also in this case the normalized pixel intensity values range from 0 to 1800. At $x=1$mm from $J=1$ to $J=7$ there is a small central area where the fluorescence signal is very weak but as $J$ increases the extension of this area is significantly reduced.
Figure 4  Fluorescence Intensity images as function of the parameter J in curves parametric on the axial position for the configuration with 6 holes with a inner diameter equal to 0.8 mm positioned on the wall of the cylindrical duct.
The acetone concentrates in the near-wall region. For $J=9$ the tracer spreads out towards the center of the cross section but there is still a significant gradient of concentration along a radius of the duct.

The gradient of the acetone concentration diminishes as $J$ increases and for $J=34$ it is very close to zero. In other words, the acetone distribution seems to be almost homogeneous.

At $x=1\text{cm}$, from $J=1$ up to 5, the images clearly show an internal region where the fluorescence signal is very low. Once again the acetone accumulates in the periphery of the cross section. From $J=7$ to $J=11$ the acetone from the near-wall region goes towards the center of the cross section and from $J=16$ to $J=34$ the mixing appears to be uniform.

In the last cross section considered, for $J=1$ and 2 there still exists a central zone where the signal is very low but it disappears for $J=3$. For $J=5$ the acetone concentration is lower in comparison with the surrounding area but for $J>7$ the signal becomes uniform. Hence it is possible to assume that the system has reached a good mixing degree. The second analysis leads to similar results. It consists in the discussion of the mixing uniformity trend as function of the axial position once the parameter $J$ is mixed. For $J=1$ and $J=2$ the images in all the three axial positions show that the signal is relatively low in the center of the duct but it is concentrated in the near-wall region. The extension of this area tends to reduce but it does not disappear as the axial position is moved from 1mm to 2 cm. For $J=2$, 3 and 5 the situation is the same except for the axial distance equal to 2cm where the jets sufficiently penetrate inside the main duct to ensure a significant presence of acetone also in the central region. The system reaches a uniformity in the fluorescence signal at $x=2\text{cm}$ for a value of the parameter $J$ equal to 7.
Figure 5  
Fluorescence Intensity signal profiles as function of the parameter $J$ in curves parametric on the axial position for the configuration with 6 holes with a inner diameter equal to 0.8 mm positioned on the wall of the cylindrical duct.

From $J=9$ the central zone with a low fluorescence signal is very small, it is
smaller at \(x=1\text{cm}\) and it fades at \(x=2\text{cm}\). From \(J=16\) up to 34 the system presents a good mixing degree for \(x=1\text{cm}\) and for \(x=2\text{cm}\) the images seem to be very similar among them. In any case, at this axial distance, the acetone distribution appears to be uniform.

The results, obtained considering the fluorescence intensity images collected at different axial positions from the convergent, can be done also taking into account the profiles of fluorescence intensity along a diameter of the three cross sections at \(x=1\text{mm}\), \(x=1\text{cm}\) and \(x=2\text{cm}\). The profiles are shown in fig.5. In these figures the fluorescence intensity has been normalized respect to its mean value for each axial position and \(J\). In such a way profiles have been made independent on the acetone concentration and they can be reasonably compared among them. The unit of fluorescence intensity is arbitrary.

For \(J=1\) and \(J=2\), it is evident that the jet penetration is low in fact the normalized intensity profile is high in the near-wall region but zero in the center for \(x=1\text{mm}\) and \(x=1\text{cm}\). For \(x=2\text{cm}\) it grows and becomes equal to 0.4. From \(J>16\) the profile at \(x=1\text{cm}\) and 2 cm are similar. For \(J=34\) all the fluorescence signal values
seem to coincide for any radial position.

In fig. 6 the non-uniformity of mixing is plotted as function of the $J$ value at the three axial distance $x=1\text{mm}$, $x=1\text{cm}$ and $x=2\text{cm}$. The standard deviation is calculated on the basis of the normalized fluorescence profile reported in figure 5.3.8.

For $x=1\text{cm}$ the StD becomes lower than 0.2 for $J=16$, while for $x=2\text{cm}$ for $J=7$. For this axial distance it reaches the minimum value for $J=11$ and than it is constant for higher value of $J$. For $x=1\text{mm}$ the lowest value is 0.26 and it competes to the highest value of $J$ here analyzed.

6 injectors with $d=0.9\text{ mm}$ protruded 1mm inside the cylindrical duct

The fourth analyzed geometry has 6 injectors with an inner diameter equal to 0.9 mm. They are equally displaced on the perimeter of the cylindrical duct at 60° of distance from each other. This configuration has already been analyzed in the paragraph 5.3.b but in this case the injectors are protruded 1mm inside the main duct ($p=1\text{mm}$). The optimal value of the momentum of the jet to main stream ratio $J$, according to Holdeman equations, is equal to 11 ($J_{\text{Hopt}}$). The numerical simulations have been run for a wide range of $J$, from 0.5 to 17. Hence, the analyses have been realized for $J$ values both lower and higher than the $J_{\text{Hopt}}$. The fig. 7 shows the bi-dimensional implementation of the fluorescence measurements realized for this configuration. As in the previous cases, the fluorescence intensity has been normalized respect to the highest of the intensity signal of all the fluorescence measurements realized and it has been subdivided in 16 levels. It goes from 0 to 1800. The acetone concentration is considered to be significant from values of the normalized fluorescence intensity higher than the fourth level hence higher than 450.
Figure 7  Fluorescence Intensity images as function of the parameter J in curves parametric on the axial position for the configuration with 6 holes with an inner diameter equal to 0.9mm protruded 1mm inside the cylindrical duct.
APPENDIX

The signal is shown as function of the radial position (x=1mm,1cm and 2cm) and the momentum of the jet to main stream flow J.

At x=1mm from J=0.5 up to J=4 it is present a central nucleus where the acetone concentration is lower than 450. Enhancing the lateral flow rate, hence the parameter J, the area with a fluorescence signal lower than 450 reduces significantly its extension. From J=0.5 up to J=2 it is possible to see the single jets since they do not completely merge.

From J=5 there is a gradient of acetone from the near-wall region towards the center of the cross section but it tends to zero as J increases. For J=14 and J=17 the acetone concentration in the central area and in the near-wall area is equal but there still exists a zone intermediate between the last two cited zones where the concentration is higher.

From J comprised among 5 and 14 a new condition delineates. As matter of fact, the signal is not detectable in the region very close to the wall of the duct. This is due to the jets over-penetration in the main cylindrical duct. The tracer accumulates in the region of the cross section between the central and the near-wall region.

At an axial distance from the convergent equal to 1cm, from J=0.5 to J=3 there is a zone with a low fluorescence signal. For J=4 and J=5 the acetone spreads out towards the central zone but there still exist a significant concentration gradient along the radius of the duct. From J>5 the uniformity of the signal becomes increasingly better.

At x=2cm and J=0.5 and 1 the signal is lower than 450 in the central zone. From J=2 the signal is detectable in any point of the area of the cross section but it is not uniform. From J>5 the mixing improves and the system reaches a good degree.

The second analysis concerns the study of the mixing uniformity as function of
the axial position of the cross section of the second cylindrical duct, once \( J \) has been fixed.

In the cross sections located at \( x=1\text{mm} \) and \( x=1\text{cm} \) for \( J \) from 0.5 up to 3, there exist a zone where the fluorescence intensity signal is lower than 450. This area is located in the center of the duct and its extension reduces as the axial position changes from 1\( \text{mm} \) to 1\( \text{cm} \). At \( x=2\text{cm} \), for \( J=0.5 \), 1 and 2 the acetone does not spread out towards the center of the duct but the region where acetone is not present diminishes. At \( x=2\text{cm} \) this region disappears but the signal is not uniform.

For \( J=4 \) and \( x=1\text{mm} \) the internal core with a low fluorescence signal is very narrow but it disappears for \( x=1\text{cm} \). For \( J=6 \) and \( x=1\text{mm} \) the signal is detectable for any pixel of the image but it is not uniform in fact the acetone concentration in the near-wall region is lower than the ones of the intermediate zone and of the center. The uniformity condition is gained at \( x=1\text{cm} \).

For \( J>6 \) the system reaches a good mixing degree even if it is evident at \( x=1\text{mm} \) the jets over-penetrated and the tracer is not present in the region near the wall.

In fig. 8 it is shown the fluorescence intensity signal along a diameter of the duct on the cross section at \( x=1\text{mm} \), \( x=1\text{cm} \) and \( x=2\text{cm} \). In these figures the fluorescence intensity has been normalized respect to its mean value for each axial position and \( J \). In such a way profiles have been made independent on the acetone concentration and they can be reasonably compared among them. The unit of fluorescence intensity is arbitrary.

In any sequence of the fluorescence intensity profiles, it is worth noting that there is an intermediate zone comprised between the near-wall region and the center of the duct where the acetone concentration reaches its highest values.
Figure 8  Fluorescence Intensity signal profiles as function of the parameter $J$ in curves parametric on the axial position for the configuration with 6 holes with a inner diameter equal to 0.9 mm protruded 1mm inside the cylindrical duct.
It happens that when $J$ is increased the signal becomes more and more uniform in the center and in the middle section but not in the near-wall region. Also for $J=17$ the fluorescence gradient is zero in the middle and central area but not in the surrounding area.

It happens that when $J$ is increased the signal becomes more and more uniform in the center and in the middle section but not in the near-wall region. Also for $J=17$ the fluorescence gradient is zero in the middle and central area but not in the surrounding area.

Furthermore the concentration of the tracer in the near-wall region as $J$ increases becomes always lower. It depends on the too high jet penetration that does not allow the tracer to spread out towards the lateral region.

The results, obtained considering the fluorescence intensity images collected at different axial positions from the convergent, can be done also taking into account the profiles of fluorescence intensity along a diameter of the three cross sections at $x=1\text{mm}$, $x=1\text{cm}$ and $x=2\text{cm}$. The profiles are shown in fig.9. In these figures the fluorescence intensity has been normalized respect to its mean value for each axial position and $J$. In such a way profiles have been made independent on the acetone concentration and they can be reasonably compared among them. The unit of fluorescence intensity is arbitrary.

In the case of $x=1\text{mm}$, the Standard deviation decreases monotonically but in at $x=1\text{cm}$ and $x=2\text{cm}$ it presents a minimum value respectively for $J=6$ and $J=3$. As matter of fact, the non-uniformity of the mixing increases after these values increase and the $StD$ is lower than 0.2 just for $J=3$. 

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Figure 9  
*Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position.*

6 injectors with $d=0.8$ mm protruded 1mm inside the cylindrical duct

The last analyzed geometry has 6 injectors with an inner diameter equal to 0.8 mm. They are equally displaced on the perimeter of the cylindrical duct at 60° of distance from each other. This configuration has already been analyzed but in this case the injectors are protruded 1mm inside the main duct ($p=1$mm).

The study has been realized for a wide range of $J$, from $J=4$ to $J=37$, in such a all the possible penetration (under- and over-penetration) conditions of jets are represented.

The fig. 10 shows the bi-dimensional implementation of the fluorescence measurements realized for this configuration. As in the previous cases, the fluorescence intensity has been normalized respect to the highest of the intensity signal of all the fluorescence measurements realized and it has been subdivided in 16 levels. It goes from 0 to 1800. The acetone concentration is considered to be significant from values of the normalized fluorescence intensity higher than the fourth level hence higher than 450.
Fluorescence Intensity images as function of the parameter J in curves parametric on the axial position for the configuration with 6 holes with an inner diameter equal to 0.8mm protruded 1mm inside the cylindrical duct.

Figure 10
At \( x=1\text{mm} \) and for \( J=1 \) and \( J=2 \) there is a central area where any fluorescence intensity signal is detectable. For \( J=3 \) up to \( J=9 \) the signal is not zero but anyway lower than 450 in the central area while in it becomes increasingly higher in the surrounding area. From \( J=11 \) the tracer spreads out towards the center of the system and the fluorescence intensity signal becomes meaningful in any point of the cross section. From \( J=16 \) the intensity of the fluorescence signal from the center becomes higher and higher and for \( J=34 \) it is reaches the highest values.

Likewise, at \( x=1\text{cm} \) from per \( J=1 \) up to \( J=3 \) the system there exists a zone where the signal is low or zero, it fades completely for \( J=7 \) and the signal intensity is always higher in the area comprised between the near-wall region and in the central area.

For \( J=11 \) the acetone is present in all the section almost uniformly but in the near wall region. For \( J=21 \) and \( J=27 \) the system seems to be well-mixed but at \( J=35 \) the acetone concentration in the center zone reaches its highest values. In all these conditions, it is visible that the jets over-penetrates in fact the acetone concentration in the near-wall region is lower in comparison with points of the remaining region.

In the last cross section analyzed, located at \( x=2\text{cm} \), from \( J=1 \) up to \( J=7 \) is still visible a central core with a low acetone concentration but it becomes smaller and smaller as \( J \) is increased. For \( J=9 \) it completely disappears and the fluorescence signal suggests the system is well mixed. The situation improves for \( J>9 \) up to 27 where it seems that the concentration in the central area becomes to high in comparison with the surrounding area. Although the signal seems to be uniform the acetone does not properly spread out towards the near wall region since the jets over-penetrates and form a central core rich of acetone.

The second analysis concerns the study of the mixing uniformity as function of the axial coordinate once the \textit{momentum of the jet to main stream ratio} \( J \) has been
For $J=1$ at $x=1\text{mm}$ it is visible a central core where no signal is measurable. This situation persists for $x=1\text{cm}$ and $x=2\text{cm}$. The same trend is clearly shown in the sequence of images for $J=2$, 3, 5 and 7 as function of the axial coordinate.

For $J=9$ the situation slightly change, in fact at $x=2\text{cm}$ the signal appears to be almost uniform. For $J=11$ at $x=1\text{mm}$ the acetone concentrates in the intermediate area and it starts to significantly accumulate in the central region. At $x=1\text{cm}$ the signal become more uniform, in fact the signal relative to the central area has the same intensity of the one coming from the intermediate area. At $x=2\text{cm}$ the signal is uniform but it is lower in the near-wall area respect to the remaining section. The same situation is proposed for $J=16$ and 21 as function of the axial direction.

For $J=27$ the signal is sufficiently uniform in the central and intermediate region but it is lower in the near-wall region at $x=1\text{mm}$, it slightly improves at $x=1\text{cm}$ but at $x=2\text{cm}$ the central core becomes very high and there is a gradient from the center towards the wall. For $J=34$ the acetone is always higher in the central region in comparison with the remaining section for any value of $x$.

In fig.11 it is shown the fluorescence intensity signal along a diameter of the duct on the cross section at $x=1\text{mm}$, $x=1\text{cm}$ and $x=2\text{cm}$. In these figures the fluorescence intensity has been normalized respect to its mean value for each axial position and $J$. In such a way profiles have been made independent on the acetone concentration and they can be reasonably compared among them. The unit of fluorescence intensity is arbitrary. It is possible to get the same information analyzing the intensity profiles as function of $J$ or as function of $x$. In particular the jet over-penetration causes the insurgence of an intermediate area where acetone concentrates.
Figure 11  Fluorescence Intensity signal profiles as function of the parameter J in curves parametric on the axial position for the configuration with 6 holes with a inner diameter equal to 0.8 mm protruded 1mm inside the cylindrical duct.
For $J>11$ the profiles are more uniform and they almost coincide. It is possible to note that the normalize intensity signals is always lower in the near-wall region respect to the remaining region. In fig.12 it is shown the non-uniformity, hence the standard deviation of the fluorescence signal along a diameter of the duct, in the cross section located at $x=1\text{mm}$, 1cm and 2cm. For $x=1\text{mm}$ the StD decreases monotonically. It goes from 0.78 to 0.27. It firstly diminishes abruptly from $J=1$ to $J=11$ and than it almost reaches a constant value. For $x=1\text{cm}$ and $x=2\text{cm}$ the standard deviation first decreases and than slowly increases. In particular at $x=1\text{cm}$ the minimum StD value is reached for $J=11$, and at $x=2\text{cm}$ for $J=3$. For $x=1\text{cm}$ the StD goes from 0.55 to 0.27, and for $x=2\text{cm}$ it is 0.323 for $J=1$ and 0.27 for $J=34$.

From $J=11$ the StD values at $x=1\text{cm}$ and $x=2\text{cm}$ are very similar at any $J$ value and the for $J=34$ the system presents always the same non-uniformity distribution degree. The system reaches an acceptable mixing for $J$ comprised between 2 and 11 for $x=2\text{cm}$, while in the cross section located at $x=1\text{cm}$ just for $J=11$, hence just in these conditions the StD is lower that 0.2.

![Figure 12](image_url)

*Figure 12* Standard Deviation of the fluorescence intensity signal along a diameter of the duct as function of the parameter $J$ on curves parametric in the axial position.
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